## Modelling Fault Dependencies when Execution Time Budgets are Exceeded

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# Introduction

- When we test out analyses, we make a lot of assumptions
  - We have representative data (Statistical methods)
  - A uniform distribution represents all possible inputs (Scheduling algorithms)
- Mostly, these assumptions are OK
  - Pragmatic assumptions which simplify our problems from impossible to doable





# Introduction

- But what about this one?
  - Job Execution Times are Independent
- It's made in a lot of places
  - Testing scheduling, early versions of MBPTA
- Problem:
  - It is completely unrealistic





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## Dependencies of Job Execution Times

- Regardless of any intelligent processor design, the job still performs a task
- Presumably, the inputs to the job effect what the job will do
- So if there are dependencies in Job inputs, there are also dependencies in Job execution times
- Is there any realistic system where Job inputs are I.I.D random variables?





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## Dependencies of Job Execution Times

- FFMPEG Decoding video frames under Valgrind
  - FFMPEG provides a lot of 'real world' data
  - Valgrind instruction counts give exact instrumentation
- Inputs Video frame data, current decoder state
- Very good indicator of job execution time is previous job execution time



# Dependencies of Job Failures

- Given that Job execution times are dependent, Job failures due to budget overruns are also dependent
- Which means that they are definitely not I.I.D.





# Is this a problem?

- Potentially a lot of places make the assumption that execution times are independent
- For example, mixed criticality systems how do these fare if overall the low-crit failure rate is 10-4, but all those failures happen one after the other?
- Not something that has been tested currently





# Problems

- Can't directly model failure durations
- Why?

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- Deadline overrun failures are rare events by definition
- Won't get enough data
- Need to predict failure durations from data gathered in testing





# Solution

- Forecasting
- Take data from normal case, generate a model, use model to predict behaviour under extreme circumstances
  - Works around scarcity of actual data





# Solution (Part 2)

- How to do forecasting?
- For this case, using Model Extrapolation
- Given a set of models with the same structure, fit curves to the model parameters and extrapolate
- To get models, using Markov Chains and Lossy Compression





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# Markov Chain Models

- Set of states corresponding to duration of overruns
- Each state has probability to change to any other state
- Simply trained on test data
  - Other ways to generate models being explored





# Compressed Markov Models

- Don't want to accept models which don't have enough data to back up each point
- Solution is to permit compressing the model
- Compression combines states/transitions which have a low amount of data behind each point
- Various methods of compression





#### **Compressed Markov Models**



**Combine States** 



**Combine Transitions** 



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### **Compressed Markov Models**



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**Combine States** 

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**Combine Transitions** 

One catch: Will want the user to tell us what intervals we're Interested in RTS York



## Forecasting

- Outline of method
  - Set multiple exceedance thresholds where there is sufficient data
  - Create models, using compression as needed
  - Find the most common shape of compressed model
  - Fit curves and extrapolate to the desired failure rate





# Evaluation

- Method
- Get a large amount of data from target system
  - FFMPEG decoding videos under Valgrind
- Create a forecast model based on a subset of the data
  - Subset of data does not have enough data to reliably model at desired confidence levels
- Compare results from forecast model with what actually happened





#### Results





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## Results





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## Results



5% has very low accuracy, but first 5% of input data is not representative

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# DepET – A dependent execution time generator

- Have a way to generate exceedance durations at an arbitrary threshold
- DepET is an algorithm to utilise this to generate dependent execution times
- So as UUniFast generates a useful spread of realistic task utilisations, DepET generates realistic task execution times





# DepET Algorithm

- Divide execution time into a series of bands
- Each invocation has a probability of exceeding it's current band
- An exceedance model governs the duration of this exceedance
- Otherwise, randomly move about inside the band





# **DepET Evaluation**

- Compared against SimSO ACET method and observations
- SimSO ACET method implemented as normal distribution with parameters derived from training data
- Useful comparison as it attempts to be realistic
- Note: Other methods of execution time generation are few in number, and may not be trying to be realistic to compare against
  - e.g. SimSO WCET method





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# **DepET Overall Distribution**





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## **DepET Overall Distribution**



Both methods give a good overall fit





#### **Evaluation - Overall Distribution**



#### **Evaluation - Dependencies**







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#### **Evaluation - Dependencies**







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### **Evaluation - Dependencies**



Is previous job execution time

# Conclusions

- Need to do better on dependencies between job execution times
  - Independence is not a realistic assumption
- Forecasting can be used to determine the expected duration of faults with reasonable accuracy
- Possible to use forecast models to generate dependent execution times using the new DepET algorithm















