INTRODUCTION TO GENETIC PROGRAMMING

TUTORIAL

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THE CHALLENGE

"How can computers learn to solve problems without being explicitly programmed? In other words, how can computers be made to do what is needed to be done, without being told exactly how to do it?"

— Attributed to Arthur Samuel (1959)

CRITERION FOR SUCCESS

"The aim [is] ... to get machines to exhibit behavior, which if done by humans, would be assumed to involve the use of intelligence."

— Arthur Samuel (1983)

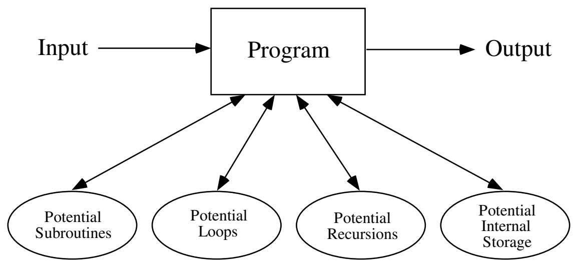
MAIN POINTS

- Genetic programming now routinely delivers high-return human-competitive machine intelligence.
- Genetic programming is an automated invention machine.
- Genetic programming can automatically create a general solution to a problem in the form of a parameterized topology.

VARIOUS REPRESENTATIONS USED TO TRY TO ACHIEVE ARTIFICIAL INTELLIGENCE (AI) AND MACHINE LEARNING (ML)

- Decision trees
- If-then production rules (e.g., expert systems)
- Horn clauses
- Neural nets (matrices of numerical weights)
- Bayesian networks
- Frames
- Propositional logic
- Binary decision diagrams
- Formal grammars
- Numerical coefficients for polynomials
- Tables of values (reinforcement learning)
- Conceptual clusters
- Concept sets
- Parallel if-then rules (e.g., learning classifier systems)

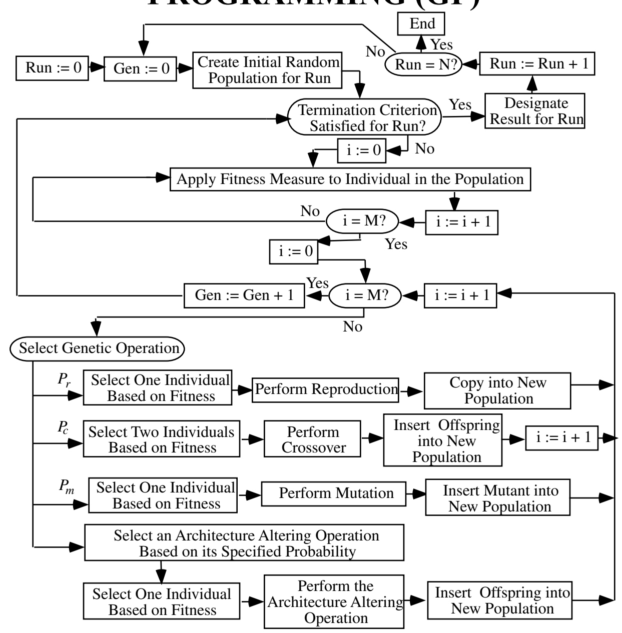
A COMPUTER PROGRAM



REPRESENTATION

- **"Our view is that computer programs are the best representation of computer programs."**

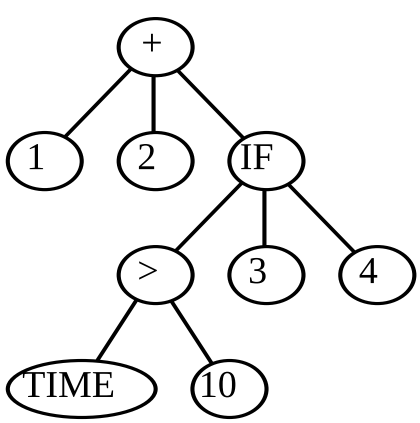
FLOWCHART FOR GENETIC PROGRAMMING (GP)



COMPUTER PROGRAM =PARSE TREE=PROGRAM TREE =PROGRAM IN LISP=DATA=LIST

```
(+ 1 2 (IF (> TIME 10) 3 4))
```

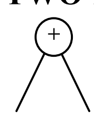
- **Terminal set T** = {`1, 2, 10, 3, 4, TIME`}
- **Function set F** = {`+, IF, >`}



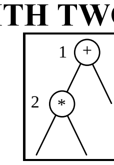
EXAMPLE OF RANDOM CREATION OF A PROGRAM TREE

- **Terminal set T** = {`A`, `B`, `C`}
- **Function set F** = {`+`, `-`, `*`, `%`, `IFLTE`}

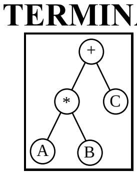
BEGIN WITH TWO-ARGUMENT `+`



CONTINUE WITH TWO-ARGUMENT `*`



FINISH WITH TERMINALS `A`, `B`, AND `C`

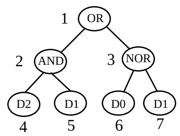


- **The result is a syntactically valid executable program (provided the set of functions is closed)**

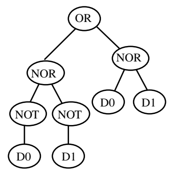
MUTATION OPERATION

- Select parent probabilistically based on fitness
- Pick point from 1 to `NUMBER-OF-POINTS`
- Delete subtree at the picked point
- Grow new subtree at the mutation point in same way as generated trees for initial random population (generation 0)
- The result is a syntactically valid executable program

ONE PARENTAL PROGRAM

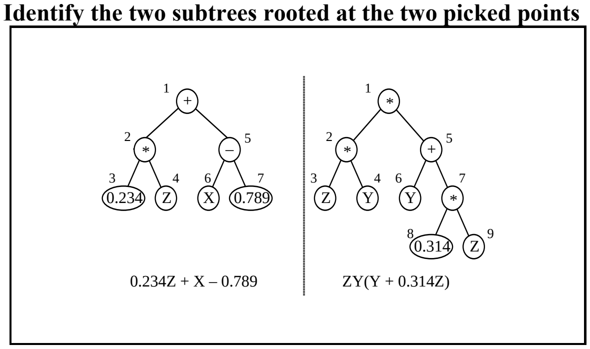


OFFSPRING PRODUCED BY MUTATION



CROSSOVER (SEXUAL RECOMBINATION) OPERATION FOR COMPUTER PROGRAMS

- Select two parents probabilistically based on fitness
- Randomly pick a number from 1 to `NUMBER-OF-POINTS` – independently for each of the two parental programs
- Identify the two subtrees rooted at the two picked points



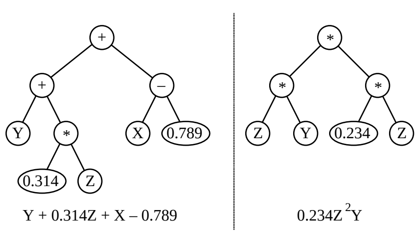
Parent 1:

```
(+ (* 0.234 Z) (- X 0.789))
```

Parent 2:

```
(* (* Z Y) (+ Y (* 0.314 Z)))
```


THE CROSSOVER OPERATION (TWO OFFSPRING VERSION)



Offspring 1:

```
(+ (+ Y (* 0.314 Z))
   (- X 0.789))
```

Offspring 2:

```
(* (* Z Y) (* 0.234 Z))
```

- The result is a syntactically valid executable program

FIVE MAJOR PREPARATORY STEPS FOR GP

- Determining the set of terminals
- Determining the set of functions
- Determining the fitness measure
- Determining the parameters for the run
  - population size
  - number of generations
  - minor parameters
- Determining the method for designating a result and the criterion for terminating a run

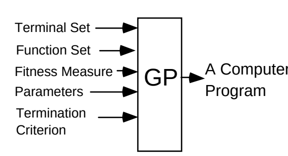
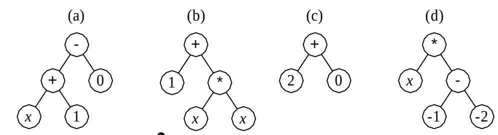


TABLEAU FOR SYMBOLIC REGRESSION OF QUADRATIC POLYNOMIAL $X^2 + X + 1$

	Objective:	**Find a computer program with one input (independent variable *x*), whose output equals the value of the quadratic polynomial $x^2 + x + 1$ in range from -1 to +1.**
1	**Terminal set:**	`T = {X, Constants}`
2	**Function set:**	`F = {+, -, *, %}` **NOTE: The protected division function % returns a value of 1 when division by 0 is attempted (including 0 divided by 0)**
3	**Fitness:**	**The sum of the absolute value of the differences (errors), computed (in some way) over values of the independent variable *x* from –1.0 to +1.0, between the program's output and the target quadratic polynomial $x^2 + x + 1$.**
4	**Parameters:**	**Population size $M = 4$.**
5	**Termination:**	**An individual emerges whose sum of absolute errors is less than 0.1**

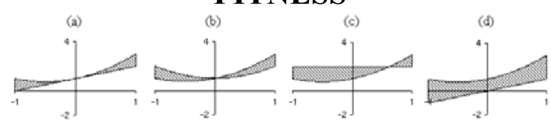
SYMBOLIC REGRESSION OF QUADRATIC POLYNOMIAL $X^2 + X + 1$

INITIAL POPULATION OF FOUR RANDOMLY CREATED INDIVIDUALS OF GENERATION 0



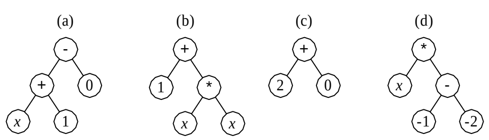
$X + 1$ $\quad$ $X^2 + 1$ $\quad$ 2 $\quad$ X

FITNESS

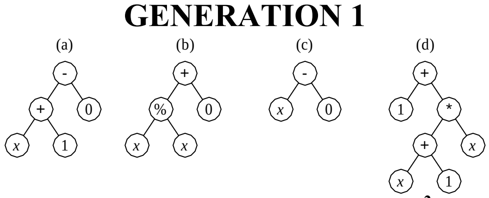


0.67 $\quad$ 1.00 $\quad$ 1.70 $\quad$ 2.67

SYMBOLIC REGRESSION OF QUADRATIC POLYNOMIAL $X^2 + X + 1$



GENERATION 1



$x + 1$	**1**	X	$x^2 + x + 1$
Copy of (a)	**Mutant of (c) —picking "2" as mutation point**	**First offspring of crossover of (a) and (b) —picking "+" of parent (a) and left-most "x" of parent (b) as crossover points**	**Second offspring of crossover of (a) and (b) —picking "+" of parent (a) and left-most "x" of parent (b) as crossover points**

SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$ (WITH 21 FITNESS CASES)

Independent variable X (Input)	Dependent Variable Y (Output)
-1.0	0.0000
-0.9	-0.1629
-0.8	-0.2624
-0.7	-0.3129
-0.6	-0.3264
-0.5	-0.3125
-0.4	-0.2784
-0.3	-0.2289
-0.2	-0.1664
-0.1	-0.0909
0	0.0
0.1	0.1111
0.2	0.2496
0.3	0.4251
0.4	0.6496
0.5	0.9375
0.6	1.3056
0.7	1.7731
0.8	2.3616
0.9	3.0951
1.0	4.0000

TABLEAU—SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

Objective:	**Find a function of one independent variable, in symbolic form, that fits a given sample of 21 (x_i, y_i) data points**
Terminal set:	**x (the independent variable).**
Function set:	`+, -, *, %, SIN, COS, EXP, RLOG`
Fitness cases:	**The given sample of 21 data points (x_i, y_i) where the x_i are in interval [–1,+1].**
Raw fitness:	**The sum, taken over the 21 fitness cases, of the absolute value of difference between value of the dependent variable produced by the individual program and the target value y_i of the dependent variable.**
Standardized fitness:	**Equals raw fitness.**
Hits:	**Number of fitness cases (0 – 21) for which the value of the dependent variable produced by the individual program comes within 0.01 of the target value y_i of the dependent variable.**
Wrapper:	**None.**
Parameters:	**Population size, M = 500. Maximum number of generations to be run, G = 51.**
Success Predicate:	**An individual program scores 21 hits.**

SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

WORST-OF-GENERATION INDIVIDUAL IN GENERATION 0 WITH RAW FITNESS OF 10^{38}

```
(EXP (- (% X (- X (SIN X)))
(RLOG (RLOG (* X X)))))
```

Equivalent to

$$e^{x/(x-\sin x) - \log \log x*x}$$

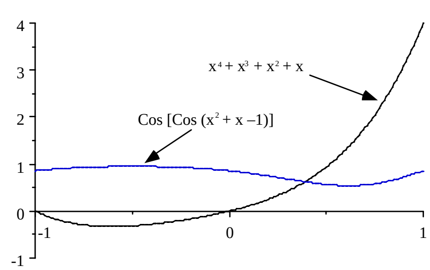
SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

MEDIAN INDIVIDUAL IN GENERATION 0 WITH RAW FITNESS OF 23.67 (AVERGAGE ERROR OF 1.3)

```
(COS (COS (+ (- (* X X) (% X
X)) X)))
```

Equivalent to

$$\mathrm{Cos}\,[\mathrm{Cos}\,(x^2 + x - 1)]$$



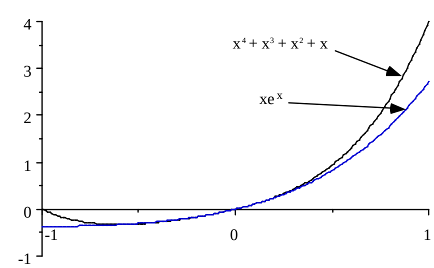
SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

BEST-OF-GENERATION INDIVIDUAL IN GENERATION 0 WITH RAW FITNESS OF 4.47 (AVERGAGE ERROR OF 0.2)

```
(* X (+ (+ (- (% X X) (% X X))
(SIN (- X X))) (RLOG (EXP (EXP
X)))))
```

Equivalent to

$$xe^x$$



SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

CREATION OF GENERATION 1 FROM GENERATION 0

- **In the so-called "generational" model for genetic algorithms, a new population is created that is equal in size to the old population**
  - **1% mutation (i.e., 5 individuals out of 500)**
  - **9% reproduction (i.e., 45 individuals)**
  - **90% crossover (i.e., 225 pairs of parents — yielding 450 offspring)**

- **All participants in mutation, reproduction, and crossover are chosen from the current population <u>PROBABILISTICALLY, BASED ON FITNESS</u>**
  - **Anything can happen**
  - **Nothing is guaranteed**
  - **The search is heavily (but not completely) biased toward high-fitness individuals**
  - **The best is not guaranteed to be chosen**
  - **The worst is not necessarily excluded**
  - **Some (but not much) attention is given even to low-fitness individuals**

SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

BEST-OF-GENERATION INDIVIDUAL IN GENERATION 2 WITH RAW FITNESS OF 2.57 (AVERGAGE ERROR OF 0.1)

```
(+ (* (* (+ X (* X (* X (% (% X
X) (+ X X))))))
          (+ X (* X X))) X) X)
```

Equivalent to...

$$x^4 + 1.5x^3 + 0.5x^2 + x$$

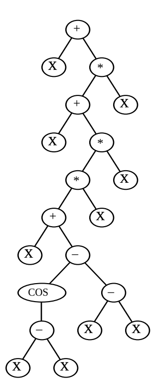
SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

BEST-OF-RUN INDIVIDUAL IN GENERATION 34 WITH RAW FITNESS OF 0.00 (100%-CORRECT)

```
(+ X (* (+ X (* (* (+ X (- (COS
(- X X)) (- X X))) X) X)) X))
```

Equivalent to

$$x^4 + x^3 + x^2 + x$$

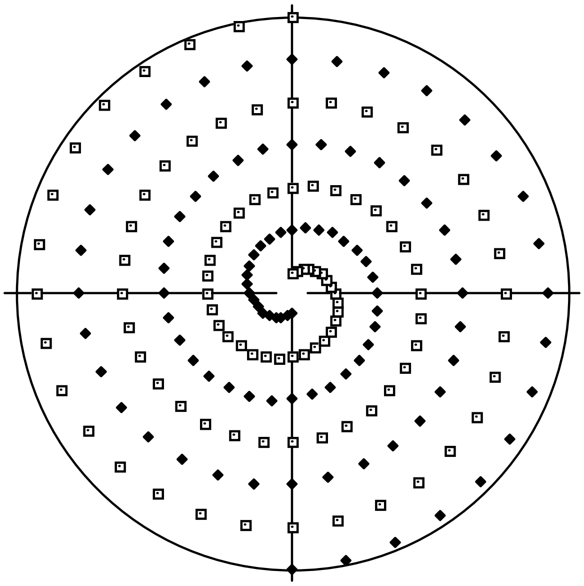


SYMBOLIC REGRESSION OF QUARTIC POLYNOMIAL $X^4+X^3+X^2+X$

OBSERVATIONS

- **GP works on this problem**
- **GP determines the size and shape of the solution**
  - **number of operations needed to solve the problem**
  - **size and shape of the program tree**
  - **content of the program tree (i.e., sequence of operations)**
- **GP operates the same whether the solution is linear, polynomial, a rational fraction of polynomials, exponential, trigonometric, etc.**
- **It's <u>*not*</u> how a human programmer would have done it**
  - ***Cos (X - X)* = 1**
  - **Not parsimonious**
- **The extraneous functions – `SIN`, `EXP`, `RLOG`, and `RCOS` are absent in the best individual of later generations because they are detrimental**
  - ***Cos (X - X)* = 1 is the exception that proves the rule**
- **The answer is algebraically correct (hence no further cross validation is needed)**

CLASSIFICATION PROBLEM
INTER-TWINED SPIRALS

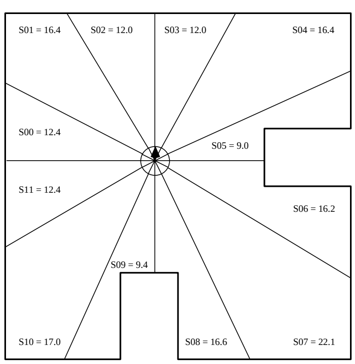


GP TABLEAU – INTERTWINED SPIRALS

Objective:	**Find a program to classify a given point in the *x*-*y* plane to the red or blue spiral.**
Terminal set:	`X`, `Y`, $\Re$, **where** $\Re$ **is the ephemeral random floating-point constant ranging between –1.000 and +1.000.**
Function set:	`+, -, *, %, IFLTE, SIN, COS.`
Fitness cases:	**194 points in the *x*-*y* plane.**
Raw fitness:	**The number of correctly classified points (0 – 194)**
Standardized fitness:	**The maximum raw fitness (i.e., 194) minus the raw fitness.**
Hits:	**Equals raw fitness.**
Wrapper:	**Maps any individual program returning a positive value to class +1 (red) and maps all other values to class –1 (blue).**
Parameters:	***M* = 10,000 (with over-selection). *G* = 51.**
Success predicate:	**An individual program scores 194 hits.**

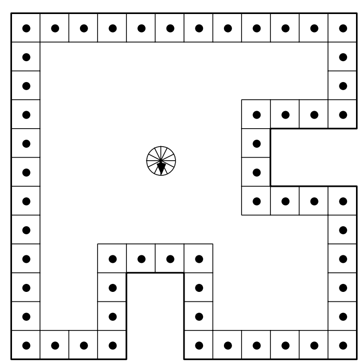
WALL-FOLLOWING PROBLEM

12 SONAR SENSORS



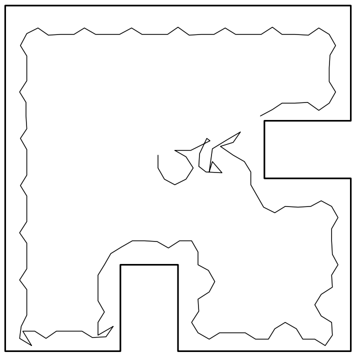
WALL-FOLLOWING PROBLEM

FITNESS MEASURE



WALL-FOLLOWING PROBLEM BEST PROGRAM OF GENERATION 57

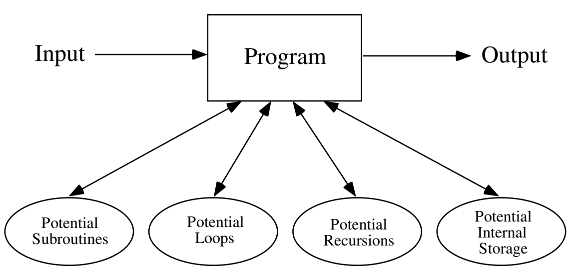
- Scores 56 hits (out of 56)
- 145point program tree



24 PROBLEMS SHOWN IN 1992 VIDEOTAPE *GENETIC PROGRAMMING: THE MOVIE* (KOZA AND RICE 1992)

- Symbolic Regression
- Intertwined Spirals
- Artificial Ant
- Truck Backer Upper
- Broom Balancing
- Wall Following
- Box Moving
- Discrete Pursuer-Evader Game
- Differential Pursuer-Evader Game
- Co-Evolution of Game-Playing Strategies
- Inverse Kinematics
- Emergent Collecting
- Central Place Foraging
- Block Stacking
- Randomizer
- 1-D Cellular Automata
- 2-D Cellular Automata
- Task Prioritization
- Programmatic Image Compression
- Finding 3√2
- Econometric Exchange Equation
- Optimization (Lizard)
- Boolean 11-Multiplexer
- 11-Parity–Automatically Defined Functions

AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)



- Subroutines provide one way to REUSE code — possibly with different instantiations of the dummy variables (formal parameters)
- Loops (and iterations) provide a 2nd way to REUSE code
- Recursion provide a 3rd way to REUSE code
- Memory provides a 4th way — to REUSE the results of executing code

AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)

10 FITNESS-CASES SHOWING THE VALUE OF THE DEPENDENT VARIABLE, *D*, ASSOCIATED WITH THE VALUES OF THE SIX INDEPENDENT VARIABLES, L_0, W_0, H_0, L_1, W_1, H_1

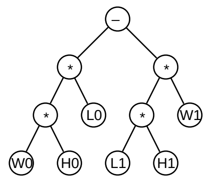
Fitness case	L_0	W_0	H_0	L_1	W_1	H_1	Dependent variable *D*
1	3	4	7	2	5	3	**54**
2	7	10	9	10	3	1	**600**
3	10	9	4	8	1	6	**312**
4	3	9	5	1	6	4	**111**
5	4	3	2	7	6	1	**–18**
6	3	3	1	9	5	4	**–171**
7	5	9	9	1	7	6	**363**
8	1	2	9	3	9	2	**–36**
9	2	6	8	2	6	10	**–24**
10	8	1	10	7	5	1	**45**

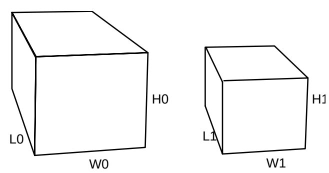
AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)

SOLUTION WITHOUT ADFS

```
(- (* (* W0 L0) H0)
   (* (* W1 L1) H1))
```

```
D = W0*L0*H0 - W1*L1*H1
```

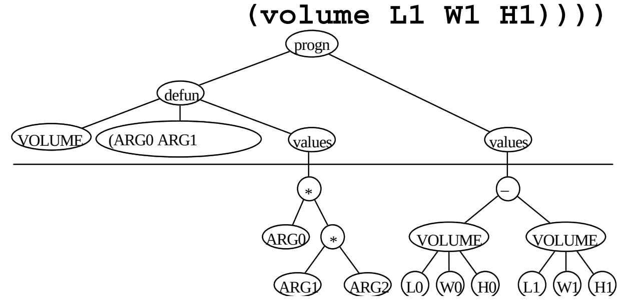




AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)

AN OVERALL COMPUTER PROGRAM CONSISTING OF ONE FUNCTION-DEFINING BRANCH (ADF, SUBROUTINE) AND ONE RESULT-PRODUCING BRANCH (MAIN PROGRAM)

```
(progn
 (defun volume (arg0 arg1 arg2)
    (values
       (* arg0 (* arg1 arg2))))
(values  (- (volume L0 W0 H0)
            (volume L1 W1 H1))))
```



AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)

IF WE ADD TWO NEW VARIABLES FOR VOLUME (V_0 AND V_1), THE 6-DIMENSIONAL NON-LINEAR REGRESSION PROBLEM BECOMES AN 8-DIMENSIONAL PROBLEM

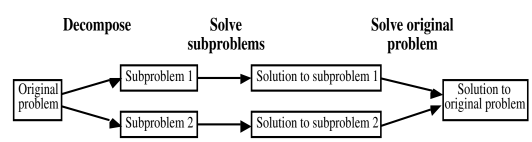
Fitness case	L_0	W_0	H_0	L_1	W_1	H_1	$\boldsymbol{V_0}$	$\boldsymbol{V_1}$	***D***
1	3	4	7	2	5	3	**84**	**30**	**54**
2	7	10	9	10	3	1	**630**	**30**	**600**
3	10	9	4	8	1	6	**360**	**48**	**312**
4	3	9	5	1	6	4	**135**	**24**	**111**
5	4	3	2	7	6	1	**24**	**42**	**–18**
6	3	3	1	9	5	4	**9**	**180**	**–171**
7	5	9	9	1	7	6	**405**	**42**	**363**
8	1	2	9	3	9	2	**18**	**54**	**–36**
9	2	6	8	2	6	10	**96**	**120**	**–24**
10	8	1	10	7	5	1	**80**	**35**	**45**

- **However, the problem can now be approached as a 2-dimensional LINEAR regression problem.**

AUTOMATICALLY DEFINED FUNCTIONS (ADFS, SUBROUTINES)

TOP-DOWN VIEW OF THREE STEP HIERARCHICAL PROBLEM-SOLVING PROCESS

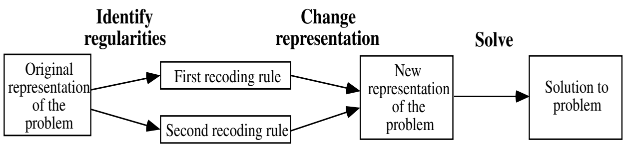
DIVIDE AND CONQUER



- **Decompose a problem into subproblems**
- **Solve the subproblems**
- **Assemble the solutions of the subproblems into a solution for the overall problem**

AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)

BOTTOM-UP VIEW OF THREE STEP HIERARCHICAL PROBLEM-SOLVING PROCESS



- **Identify regularities**
- **Change the representation**
- **Solve the overall problem**

AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)

- **In generation 0, we create a population of programs, each consisting of a main result-producing branch (RPB) and one or more function-defining branches (automatically defined functions, ADFs, subroutines)**
  - **Different ingredients for RPB and ADFs**
  - **The terminal set of an ADF typically contains dummy arguments (formal parameters), such as `ARG0`, `ARG1`, …**
  - **The function set of the RPB contains `ADF0`, …**
  - **ADFs are private and associated with a particular individual program in the population**
- **The entire program is executed and evaluated for fitness**
- **Genetic operation of reproduction is the same as before**
- **Mutation operation starts (as before) by picking a mutation point from either RPB or an ADF and deleting the subtree rooted at that point. As before, a subtree is then grown at the point. The new subtree is composed of the allowable ingredients for that point — so that the result is a syntactically valid executable program.**
- **Crossover operation starts (as before) by picking a crossover point from either RPB or an ADF of one parent. The choice of crossover point in the second parent is then restricted (e.g., to the RPB or to the ADF) — so that when the subtrees are swapped, the result is a syntactically valid executable program.**

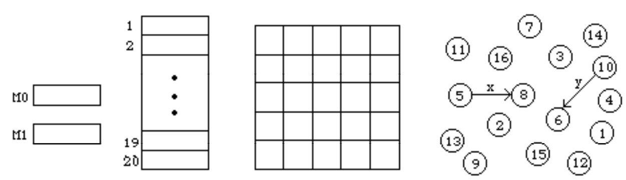
AUTOMATICALLY DEFINED FUNCTIONS (ADFs, SUBROUTINES)

8 MAIN POINTS FROM BOOK *GENETIC PROGRAMMING II: AUTOMATIC DISCOVERY OF REUSABLE PROGRAMS* (KOZA 1994)

- **ADFs work.**
- **ADFs do not solve problems in the style of human programmers.**
- **ADFs reduce the computational effort required to solve a problem.**
- **ADFs usually improve the parsimony of the solutions to a problem.**
- **As the size of a problem is scaled up, the size of solutions increases more slowly with ADFs than without them.**
- **As the size of a problem is scaled up, the computational effort required to solve a problem increases more slowly with ADFs than without them.**
- **The advantages in terms of computational effort and parsimony conferred by ADFs increase as the size of the problem is scaled up.**

REUSE

MEMORY AND STORAGE



(A) (B) (C) (D)

- **(A) Settable (named) variables (*Genetic Programming*, Koza 1992) using setting (writing) functions `(SETM0 X)` and `(SETM1 Y)` and reading by means of terminals `M0` and `M1`.**
- **(B) Indexed memory similar to linear (vector) computer memory (Teller 1994) using `(READ K)` and `(WRITE X K)`**
- **(C) Matrix memory (Andre 1994)**
- **(D) Relational memory (Brave 1995, 1996)**

LANGDON'S DATA STRUCTURES

- **Stacks**
- **Queues**
- **Lists**
- **Rings**

REUSE

AUTOMATICALLY DEFINED ITERATIONS (ADIS)

- **Overall program consisting of an automatically defined function `ADF0`, an iteration-performing branch `IPB0`, and a result-producing branch `RPB0`.**
- **Iteration is over a known, fixed set**
  - **protein or DNA sequence (of varying length**
  - **time-series data**
  - **two-dimensional array of pixels**

REUSE

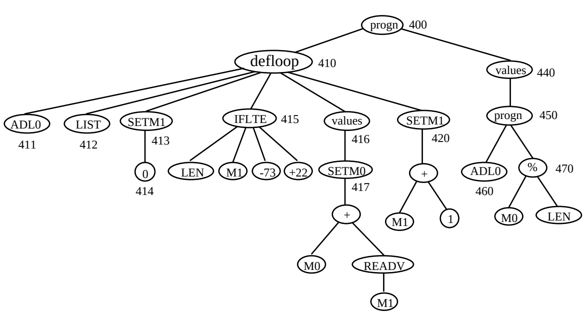
TRANSMEMBRANE SEGMENT IDENTIFICATION PROBLEM

- **Goal is to classify a given protein segment as being a transmembrane domain or non-transmembrane area of the protein**
- **Generation 20 — Run 3 — Subset-creating version**
  - **in-sample correlation of 0.976**
  - **out-of-sample correlation of 0.968**
  - **out-of-sample error rate 1.6%**

```
(progn

    (defun ADF0 ()
(ORN (ORN (ORN (I?) (H?)) (ORN (P?) (G?))) (ORN (ORN
(ORN (Y?) (N?)) (ORN (T?) (Q?))) (ORN (A?) (H?))))))

    (defun ADF1 ()
(values (ORN (ORN (ORN (A?) (I?)) (ORN (L?) (W?)))
(ORN (ORN (T?) (L?)) (ORN (T?) (W?))))))

    (defun ADF2 ()
(values (ORN (ORN (ORN (ORN (ORN (D?) (E?)) (ORN (ORN
(ORN (D?) (E?)) (ORN (ORN (T?) (W?)) (ORN (Q?)
(D?)))) (ORN (K?) (P?)))) (ORN (K?) (P?))) (ORN (T?)
(W?))) (ORN (ORN (E?) (A?)) (ORN (N?) (R?))))))

    (progn (loop-over-residues
       (SETM0 (+ (- (ADF1) (ADF2)) (SETM3 M0))))

    (values (% (% M3 M0) (% (% (% (- L -0.53) (* M0
M0)) (+ (% (% M3 M0) (% (+ M0 M3) (% M1 M2))) M2)) (%
M3 M0))))))
```


REUSE

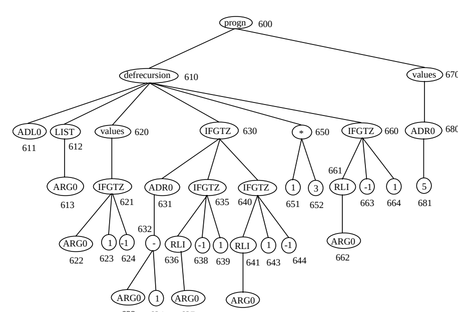
EXAMPLE OF A PROGRAM WITH A FOUR-BRANCH AUTOMATICALLY DEFINED LOOP (`ADL0`) AND A RESULT-PRODUCING BRANCH



REUSE

AUTOMATICALLY DEFINED RECURSION (`ADR0`) AND A RESULT-PRODUCING BRANCH

- **a recursion condition branch, `RCB`**
- **a recursion body branch, `RBB`**
- **a recursion update branch, `RUB`**
- **a recursion ground branch, `RGB`**



GP TECHNIQUES

- control structures involving multiple result-producing branches (Luke and Spector 1996a Bennett 1996a Svingen 1997)
- adaptive self-modifying ontogenetic genetic programming (Spector and Stoffel 1996a 1996b)
- cultural storage and transmission (Spector and Luke 1996a 1996b)
- hierarchical problem solving (Rosca and Ballard 1994a 1994b; Rosca 1995; Rosca 1997)
- modules (Angeline and Pollack 1993 1994; Angeline 1993 1994; Kinnear 1994b)
- logic grammars (Wong and Leung 1995a 1995b 1995c 1995d 1995e 1995f 1997)
- cellular encoding (developmental genetic programming) for evolving neural networks (Gruau 1992a 1992b 1993 1994a 1994b; Gruau and Whitley 1993; Esparcia-Alcazar and Sharman 1997)
- developmental methods for evolving finite automata using genetic programming (Brave 1996a)
- developmental methods for shape optimization (Kennelly 1997)
- evolving graphs and networks (Luke and Spector 1996b)
- using a grammar to represent bias and background knowledge (Whigham 1995a 1995b 1996)
- developmental methods for fuzzy logic systems (Tunstel and Jamshidi 1996)

GP TECHNIQUES — CONTINUED

- diploidy and dominance (Greene 1997a 1997b)
- Turing completeness of genetic programming (Teller 1994c; Nordin and Banzhaf 1995)
- evolution of chemical topological structures (Nachbar 1997 1998)
- interactive fitness measures (Poli and Cagnoni 1997;) and in particular in graphics and art (Sims 1991a 1991b 1992a 1992b 1993)
- variations in crossover operations (Poli and Langdon 1997)
- distributed processes and multi-agent systems (Haynes Sen Schoenefeld and Wainwright 1995; Ryan 1995; Luke and Spector 1996a; Iba 1996; Iba Nozoe and Ueda 1997; Qureshi 1996; Crosbie and Spafford 1995)
- complexity-based fitness measures using minimum description length (Iba Kurita de Garis and Sato 1993; Iba deGaris and Sato 1994)
- co-evolution (Reynolds 1994c)
- steady state genetic programming (Reynolds 1993 1994a 1994b)
- use of noise in fitness cases (Reynolds 1994d)
- balancing parsimony and accuracy (Zhang and Muhlenbein 1993 1994 1995; Blickle l997)
- automatically defined features using genetic algorithms in conjunction with genetic programming (Andre 1994a)
- grammatical evolution (Conor Ryan and Michael O'Neill)

GP TECHNIQUES — CONTINUED

- graphical program structures and neural programming (Teller and Veloso 1996, 1997; Teller 1998; Poli 1997a, 1997b)
- automatically defined macros (ADMs) for simultaneous evolution of programs and their control structures (Spector 1996)
- libraries (Koza 1990a; Koza and Rice 1991; Koza 1992a, section 6.5.4; Angeline and Pollack 1993, 1994; Angeline 1993, 1994; Kinnear 1994b)
- strong typing (Montana 1995; Montana and Czerwinski 1996; Janikow 1996; Yu and Clack 1997a) and constrained syntactic structures (Koza 1992a)
- explicit pointers (Andre 1994c)
- evolution of machine code (Nordin 1994, 1997) and linear genomes (Banzhaf, Nordin, Keller, and Francone 1998)

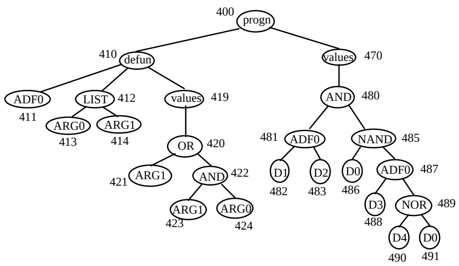
ARCHITECTURE-ALTERING OPERATIONS

PROTEIN ALIGNMENT OF "A" AND "B" PROTEINS

```
First.protein   MRIKFLVVLA VICLFAHYAS ASGMGGDKKP KDAPKPKDAP KPKEVKPV[illegible]
Second.protein  MRIKFLVVLA VICLLAHYAS ASGMGGDKKP KDAPKPKDAP KPKEVKPV[illegible]

First.protein   ESSEYEIEVI KHQKEKTEKK EKEKKTHVET KKEVKKKEKK QIPCSEKL[illegible]
Second.protein  DSSEYEIEVI KHQKEKTEKK EKEKKAHVEI KKKIKNKEKK FVPCSEIL[illegible]

First.protein   EKLDCETKGV PAGYKAIFKF TENEE-CDWT CDYEALPPPP GAKKDDKK[illegible]
Second.protein  EKLECEKNAT P-GYKALFEF KESESFCEWE CDYEAI---P GAKKDEKK[illegible]

First.protein   KTVKVVKPPK EKPPKKLRKE CSGEKVIKFQ NCLVKIRGLI AFGDKTKN[illegible]
Second.protein  KVVKVIKPPK EKPPKKPRKE CSGEKVIKFQ NCLVKIRGLI AFGDKTKN[illegible]

First.protein   KKFAKLVQGK QKKGAKKAKG GKKAAPKPGP KPGPK---Q ADKP---239
Second.protein  KKFAKLVQGK QKKGAKKAKG GKKAEPKPGP KPAPKPGPKP APKPVPKP[illegible]

First.protein   --KDAKK                                        244
Second.protein  KPKDAKK                                        253
```

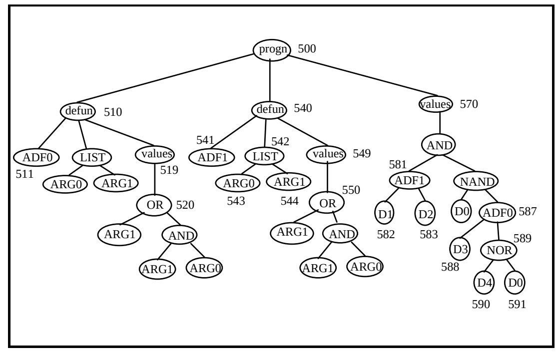
ARCHITECTURE-ALTERING OPERATIONS

PROGRAM WITH 1 TWO-ARGUMENT AUTOMATICALLY DEFINED FUNCTION (`ADF0`) AND 1 RESULT-PRODUCING BRANCH – ARGUMENT MAP OF {2}



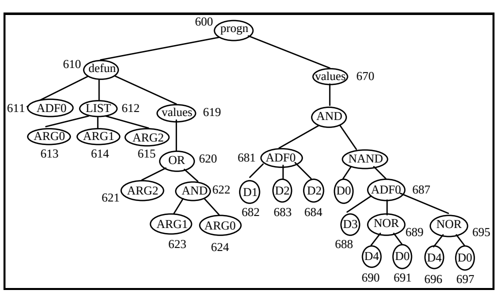
ARCHITECTURE-ALTERING OPERATIONS

PROGRAM WITH ARGUMENT MAP OF {2, 2} CREATED USING THE OPERATION OF BRANCH DUPLICATION



ARCHITECTURE-ALTERING OPERATIONS

PROGRAM WITH ARGUMENT MAP OF {3} CREATED USING THE OPERATION OF ARGUMENT DUPLICATION



ARCHITECTURE-ALTERING OPERATIONS

SPECIALIZATION – REFINEMENT – CASE SPLITTING

- **Branch duplication**
- **Argument duplication**
- **Branch creation**
- **Argument creation**

GENERALIZATION

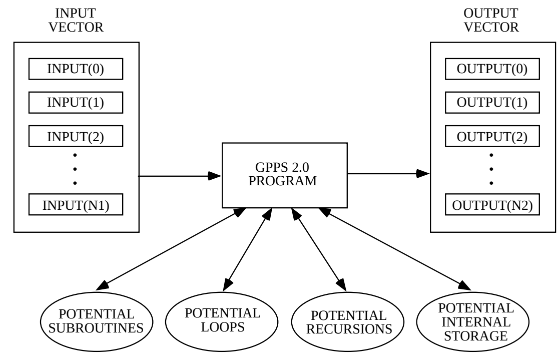
- **Branch deletion**
- **Argument deletion**

16 ATTRIBUTES OF A SYSTEM FOR AUTOMATICALLY CREATING COMPUTER PROGRAMS

1 — Starts with "What needs to be done"
2 — Tells us "How to do it"
3 — Produces a computer program
4 — Automatic determination of program size
5 — Code reuse
6 — Parameterized reuse
7 — Internal storage
8 — Iterations, loops, and recursions
9 — Self-organization of hierarchies
10 — Automatic determination of program architecture
11 — Wide range of programming constructs
12 — Well-defined
13 — Problem-independent
14 — Wide applicability
15 — Scalable
16 — Competitive with human-produced results

ARCHITECTURE-ALTERING OPERATIONS

GENETIC PROGRAMMING PROBLEM SOLVER (GPPS) — VERSION 2.0



IMPLEMENTATION OF GP IN ASSEMBLY CODE – COMPILED GENETIC PROGRAMMING SYSTEM (NORDIN 1994)

• Nordin, Peter. 1997. *Evolutionary Program Induction of Binary Machine Code and its Application*. Munster, Germany: Krehl Verlag.
• Opportunity to speed up GP that is done by slowly INTERPRETING GP program trees.
Instead of interpreting the GP program tree, EXECUTE this sequence of assembly code.
• Can identify small set of primitive functions that is useful for large group of problems, such as `+`, `-`, `*`, `%` and also use some conditional operations (`IFLTE`), some logical functions (`AND`, `OR`, `XOR`, `XNOR`) and perhaps others (e.g., `SRL`, `SLL`, `SETHI` from Sun 4).
• Then, generate random sequence of assembly code instructions at generation 0 from this small set of machine code instructions (referring to certain registers).
• If ADFs are involved, generate fixed header and footer of function and appropriate function call.
• Perform crossover possibly so as to preserve the integrity of subtrees.
• If ADFs are involved, perform crossover so as to preserve the integrity of the header and footer of function and the function call.

DESIGN OF QUANTUM COMPUTER CIRCUITS USING GP

Spector, Lee. 2004. *Automatic Quantum Computer Programming: A Genetic Programming Approach*. Boston: Kluwer Academic Publishers.

CELLULAR ENCODING (DEVELOPMENTAL GENETIC PROGRAMMING)

- **Gruau, Frederic. 1992b. *Cellular Encoding of Genetic Neural Networks*. Technical report 92-21. Laboratoire de l'Informatique du Parallélisme. Ecole Normale Supérieure de Lyon. May 1992.**
- **Also: Gruau 1992a 1992b 1993 1994a 1994b; Gruau and Whitley 1993; Esparcia-Alcazar and Sharman 1997)**
- **Applied by Gruau and Whitley (1995) to 2-pole-balancing problem**
- **Applied by Gruau to six-legged walking creature**
- **Applied by Brave (1995, 1996) to Finite Automata**

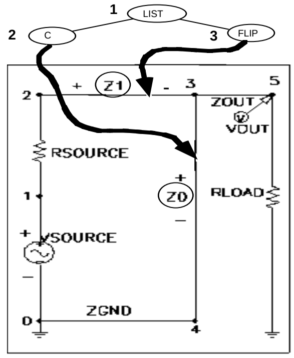
AUTOMATIC PARALLELIZATION OF SERIAL PROGRAMS USING GP

- **Ryan, Conor. 1999. *Automatic Re-engineering of Software Using Genetic Programming*. Amsterdam: Kluwer Academic Publishers.**
- **Start with working serial computer program (embryo)**
- **GP program tree contains validity-preserving functions that modify the current program. That is, the functions in the program tree side-effect the current program.**
- **Execution of the complete GP program tree progressively modifies the current program**
- **Fitness is based on execution time on the parallel computer system**

DEVELOPMENTAL GP

THE INITIAL CIRCUIT

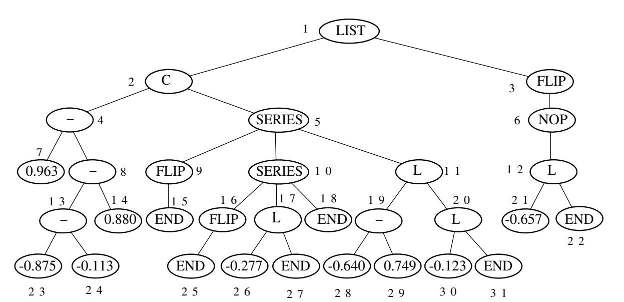
- **Initial circuit consists of embryo and test fixture**
- **Embryo has modifiable wires (e.g., Z0 AND Z1)**
- **Test fixture has input and output ports and usually has source resistor and load resistor. There are no modifiable wires (or modifiable components) in the test fixture.**
- **Circuit-constructing program trees consist of**
  - **Component-creating functions**
  - **Topology-modifying functions**
  - **Development-controlling functions**
- **Circuit-constructing program tree has one result-producing branch for each modifiable wire in embryo of the initial circuit**



DEVELOPMENTAL GP

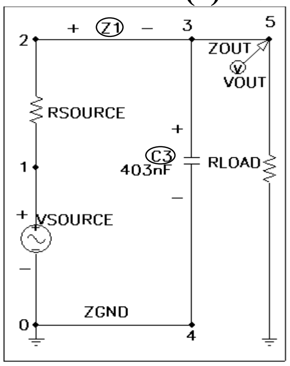
DEVELOPMENT OF A CIRCUIT FROM A CIRCUIT-CONSTRUCTING PROGRAM TREE AND THE INITIAL CIRCUIT

```
(LIST (C (- 0.963 (- (- -0.875
-0.113) 0.880)) (series (flip
end) (series (flip end) (L -
0.277 end) end) (L (- -0.640
0.749) (L -0.123 end)))) (flip
(nop (L -0.657 end)))))
```



DEVELOPMENTAL GP

RESULT OF THE C (2) FUNCTION

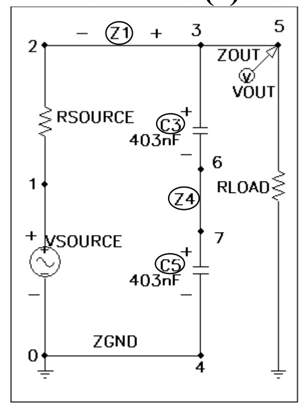


(LIST (C (- 0.963 (- (- -0.875 -0.113) 0.880)) (series (flip end) (series (flip end) (L -0.277 end) end) (L (- -0.640 0.749) (L -0.123 end)))) (flip (nop (L -0.657 end)))))

NOTE: Interpretation of arithmetic value

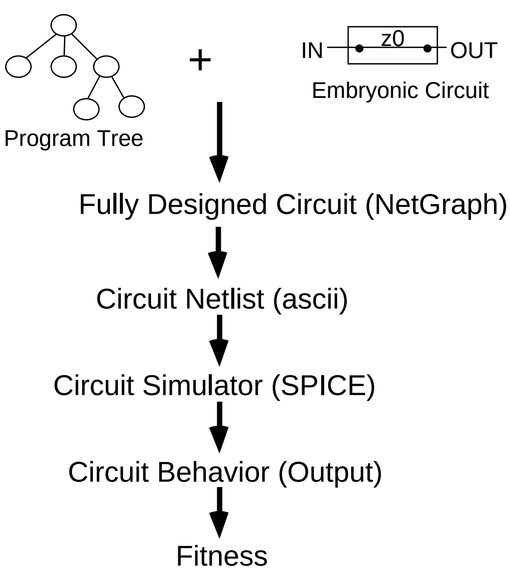
DEVELOPMENTAL GP

RESULT OF SERIES (5) FUNCTION

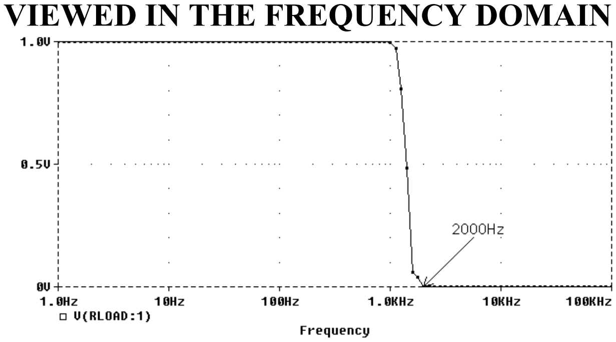


(LIST (C (- 0.963 (- (- -0.875 -0.113) 0.880)) (series (flip end) (series (flip end) (L -0.277 end) end) (L (- -0.640 0.749) (L -0.123 end)))) (flip (nop (L -0.657 end)))))

EVALUATION OF FITNESS OF A CIRCUIT



BEHAVIOR OF A LOWPASS FILTER VIEWED IN THE FREQUENCY DOMAIN



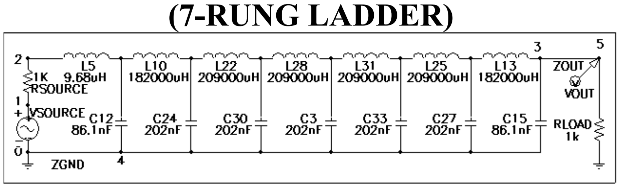
- **Examine circuit's behavior for each of 101 frequency values chosen over five decades of frequency (from 1 Hz to 100,000 Hz) with each decade divided into 20 parts (using a logarithmic scale). The fitness measure**
  - **does not penalize ideal values**
  - **slightly penalizes acceptable deviations**
  - **heavily penalizes unacceptable deviations**
- **Fitness is sum** $F(t) = \sum_{i=0}^{100} [W(f_i)d(f_i)]$
  - ***f*(*i*) is the frequency of fitness case *i***
  - ***d*(*x*) is the difference between the target and observed values at frequency of fitness case *i***
  - ***W*(*y*,*x*) is the weighting at frequency *x***

TABLEAU — LOWPASS FILTER (WITHOUT ADFs OR ARCHITECTURE-ALTERING OPERATIONS)

Objective:	**Design a lowpass filter composed of inductors and capacitors with a passband below 1,000 Hz, a stopband above 2,000 Hz, a maximum allowable passband deviation of 30 millivolts, and a maximum allowable stopband deviation of 1 millivolt.**
Test fixture and embryo:	**One-input, one-output initial circuit with a source resistor, load resistor, and two modifiable wires.**
Program architecture:	**Two result-producing branches, `RPB0` and `RPB1` (i.e., one RPB per modifiable wire in the embryo).**
Initial function set for the result-producing branches:	**For construction-continuing subtrees:** $F_{ccs\text{-}rpb\text{-}initial}$ **= {`C`, `L`, `SERIES`, `PARALLEL0`, `FLIP`, `NOP`, `TWO_GROUND`, `TWO_VIA0`, `TWO_VIA1`, `TWO_VIA2`, `TWO_VIA3`, `TWO_VIA4`, `TWO_VIA5`, `TWO_VIA6`, `TWO_VIA7`}. For arithmetic-performing subtrees:** F_{aps} **= {+, -}.**
Initial terminal set for the result-producing branches:	**For construction-continuing subtrees:** $T_{ccs\text{-}rpb\text{-}initial}$ **= {`END`}. For arithmetic-performing subtrees:** T_{aps} **= {$\leftarrow_{smaller\text{-}reals}$}.**

Fitness cases:	**101 frequency values in an interval of five decades of frequency values between 1 Hz and 100,000 Hz.**
Raw fitness:	**Fitness is the sum, over the 101 sampled frequencies (fitness cases), of the absolute weighted deviation between the actual value of the output voltage that is produced by the circuit at the probe point and the target value for voltage. The weighting penalizes unacceptable output voltages much more heavily than deviating, but acceptable, voltages.**
Standardized fitness:	**Same as raw fitness.**
Hits:	**The number of hits is defined as the number of fitness cases (out of 101) for which the voltage is acceptable or ideal or that lie in the "don't care" band.**
Wrapper:	**None.**
Parameters:	M **= 1,000 to 320,000.** G **= 1,001.** Q **=1,000.** D **= 64.** B **= 2%.** N_{rpb} **= 2.** S_{rpb} **= 200.**
Result designation:	**Best-so-far pace-setting individual.**
Success predicate:	**A program scores the maximum number (101) of hits.**

EVOLVED CAMPBELL FILTER (7-RUNG LADDER)

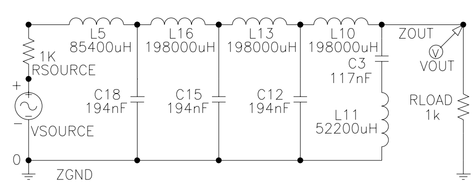


• This genetically evolved circuit infringes on U. S. patent 1,227,113 issued to George Campbell of American Telephone and Telegraph in 1917 (claim 2):

> **An electric wave filter consisting of a connecting line of negligible attenuation composed of a plurality of sections, each section including a capacity element and an inductance element, one of said elements of each section being in series with the line and the other in shunt across the line, said capacity and inductance elements having precomputed values dependent upon the upper limiting frequency and the lower limiting frequency of a range of frequencies it is desired to transmit without attenuation, the values of said capacity and inductance elements being so proportioned that the structure transmits with practically negligible attenuation sinusoidal currents of all frequencies lying between said two limiting frequencies, while attenuating and approximately extinguishing currents of neighboring frequencies lying outside of said limiting frequencies."**

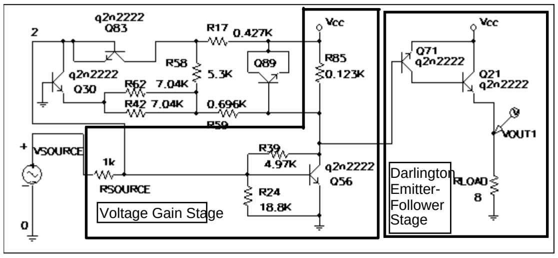
EVOLVED ZOBEL FILTER

- **Infringes on U. S. patent 1,538,964 issued in 1925 to Otto Zobel of American Telephone and Telegraph Company for an "*M*-derived half section" used in conjunction with one or more "constant K" sections.**
- **One *M*-derived half section (`C2` and `L11`)**
- **Cascade of three symmetric T-sections**



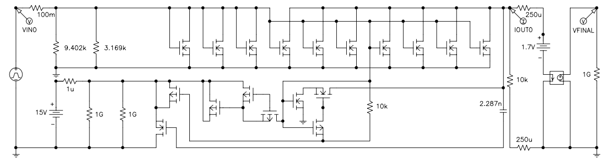
GENETICALLY EVOLVED 10 DB AMPLIFIER FROM GENERATION 45

SHOWING THE VOLTAGE GAIN STAGE AND DARLINGTON EMITTER FOLLOWER SECTION



POST-2000 PATENTED INVENTIONS

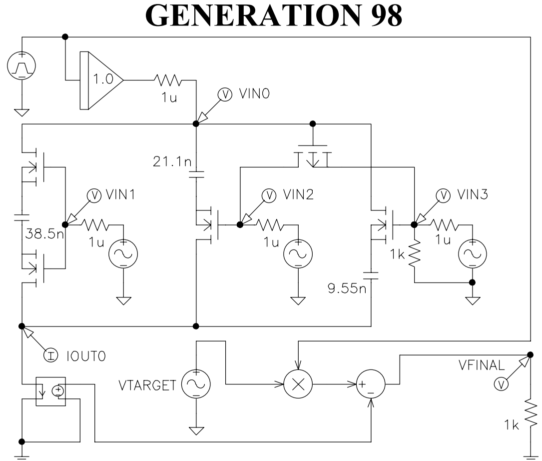
HIGH CURRENT LOAD CIRCUIT BEST-OF-RUN FROM GENERATION 114



POST-2000 PATENTED INVENTIONS

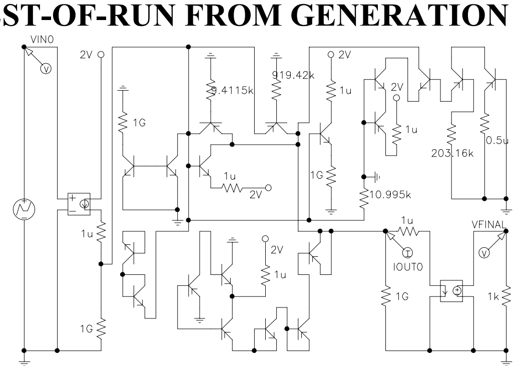
REGISTER-CONTROLLED CAPACITOR CIRCUIT

SMALLEST COMPLIANT FROM GENERATION 98



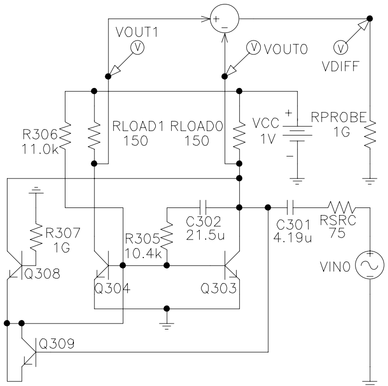
POST-2000 PATENTED INVENTIONS

LOW-VOLTAGE CUBIC SIGNAL GENERATION CIRCUIT BEST-OF-RUN FROM GENERATION 182



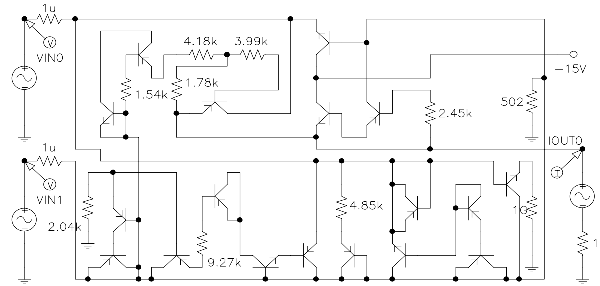
POST-2000 PATENTED INVENTIONS

LOW-VOLTAGE BALUN CIRCUIT BEST EVOLVED FROM GENERATION 84



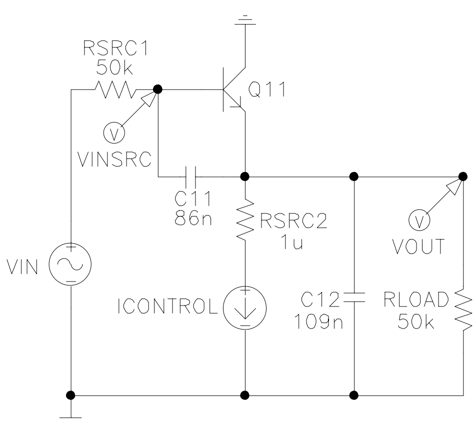
POST-2000 PATENTED INVENTIONS

VOLTAGE-CURRENT-CONVERSION CIRCUIT BEST-OF-RUN FROM GENERATION 109



POST-2000 PATENTED INVENTIONS

TUNABLE INTEGRATED ACTIVE FILTER — GENERATION 50



21 PREVIOUSLY PATENTED INVENTIONS REINVENTED BY GP

	Invention	Date	Inventor	Place	Patent
1	Darlington emitter-follower section	1953	Sidney Darlington	Bell Telephone Laboratories	2,663,806
2	Ladder filter	1917	George Campbell	American Telephone and Telegraph	1,227,113
3	Crossover filter	1925	Otto Julius Zobel	American Telephone and Telegraph	1,538,964
4	"*M*-derived half section" filter	1925	Otto Julius Zobel	American Telephone and Telegraph	1,538,964
5	Cauer (elliptic) topology for filters	1934–1936	Wilhelm Cauer	University of Gottingen	1,958,742, 1,989,545
6	Sorting network	1962	Daniel G. O'Connor and Raymond J. Nelson	General Precision, Inc.	3,029,413
7	Computational circuits	See text	See text	See text	See text
8	Electronic thermometer	See text	See text	See text	See text
9	Voltage reference circuit	See text	See text	See text	See text
10	60 dB and 96 dB amplifiers	See text	See text	See text	See text
11	Second-derivative controller	1942	Harry Jones	Brown Instrument Company	2,282,726
12	Philbrick circuit	1956	George Philbrick	George A. Philbrick Researches	2,730,679
13	NAND circuit	1971	David H. Chung and Bill H.	Texas Instruments Incorporated	3,560,760

			Terrell		
14	PID (proportional, integrative, and derivative) controller	1939	Albert Callender and Allan Stevenson	Imperial Chemical Limited	2,175,985
15	Negative feedback	1937	Harold S. Black	American Telephone and Telegraph	2,102,670, 2,102,671
16	Low-voltage balun circuit	2001	Sang Gug Lee	Information and Communications University	6,265,908
17	Mixed analog-digital variable capacitor circuit	2000	Turgut Sefket Aytur	Lucent Technologies Inc.	6,013,958
18	High-current load circuit	2001	Timothy Daun-Lindberg and Michael Miller	International Business Machines Corporation	6,211,726
19	Voltage-current conversion circuit	2000	Akira Ikeuchi and Naoshi Tokuda	Mitsumi Electric Co., Ltd.	6,166,529
20	Cubic function generator	2000	Stefano Cipriani and Anthony A. Takeshian	Conexant Systems, Inc.	6,160,427
21	Tunable integrated active filter	2001	Robert Irvine and Bernd Kolb	Infineon Technologies AG	6,225,859

2 PATENTED INVENTIONS CREATED BY GENETIC PROGRAMMING

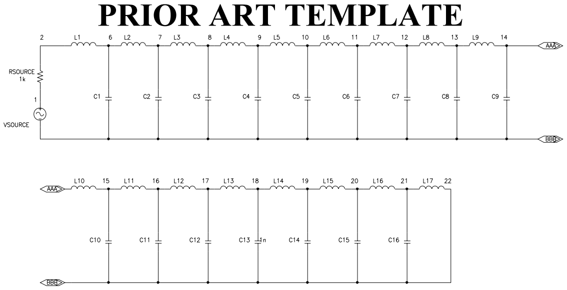
Keane, Martin A., Koza, John R., and Streeter, Matthew J. 2005. *Apparatus for Improved General-Purpose PID and Non-PID Controllers*. U. S. Patent 6,847,851. Filed July 12, 2002. Issued January 25, 2005.

NOVELTY-DRIVEN EVOLUTION

EXAMPLE OF LOWPASS FILTER

- **Two factors in fitness measure**
  - **Circuit's behavior in the frequency domain**
  - **Largest number of nodes and edges (circuit components) of a subgraph of the given circuit that is isomorphic to a subgraph of a template representing the prior art. Graph isomorphism algorithm with the cost function being based on the number of shared nodes and edges (instead of just the number of nodes).**

PRIOR ART TEMPLATE

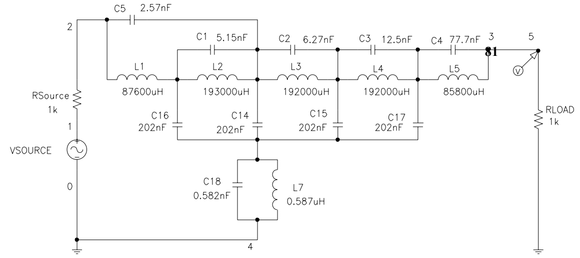


NOVELTY-DRIVEN EVOLUTION — CONTINUED

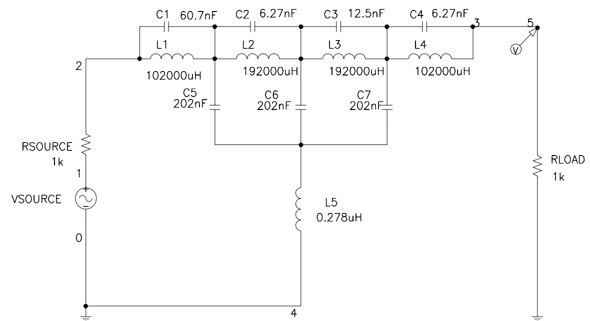
- **For circuits not scoring the maximum number (101) of hits, the fitness of a circuit is the product of the two factors.**
- **For circuits scoring 101 hits (100%-compliant individuals), fitness is the number of shared nodes and edges divided by 10,000.**

FITNESS OF EIGHT 100%-COMPLIANT CIRCUITS

Solution	Frequency factor	Isomorphism factor	Fitness
1	0.051039	7	0.357273
2	0.117093	7	0.819651
3	0.103064	7	0.721448
4	0.161101	7	1.127707
5	0.044382	13	0.044382
6	0.133877	7	0.937139
7	0.059993	5	0.299965
8	0.062345	11	0.685795



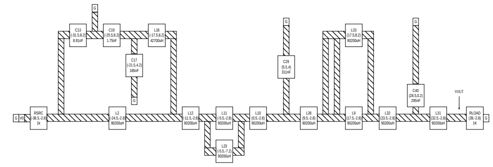
SOLUTION NO. 1



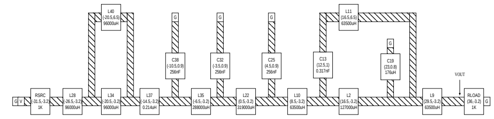
SOLUTION NO. 5

LAYOUT — LOWPASS FILTER 100%-COMPLIANT CIRCUITS

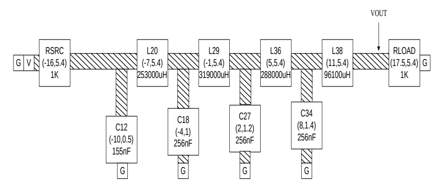
GENERATION 25 WITH 5 CAPACITORS AND 11 INDUCTORS — AREA OF 1775.2



GENERATION 30 WITH 10 INDUCTORS AND 5 CAPACITORS — AREA OF 950.3



BEST-OF-RUN CIRCUIT OF GENERATION 138 WITH 4 INDUCTORS AND 4 CAPACITORS — AREA OF 359.4

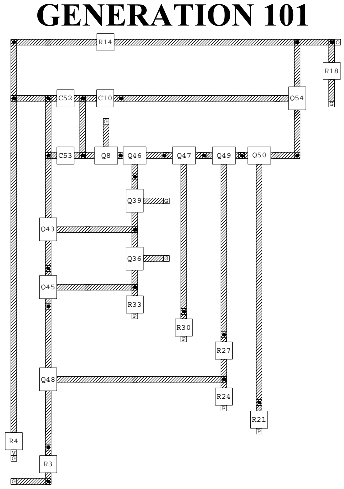


LAYOUT — 60 DB AMPLIFIER (USING TRANSISTORS)

COMPARISON

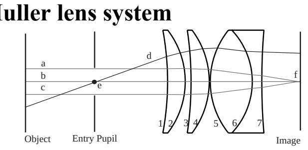
Gen	Components	Area	Four penalties	Fitness
65	27	8,234	33.034348	33.042583
101	19	4,751	0.061965	0.004751

BEST-OF-RUN CIRCUIT FROM GENERATION 101



DESIGN OF OPTICAL LENS SYSTEMS (AL-SAKRAN, KOZA, AND JONES, 2005; KOZA, AL-SAKRAN, AND JONES, 2005)

Tackaberry-Muller lens system

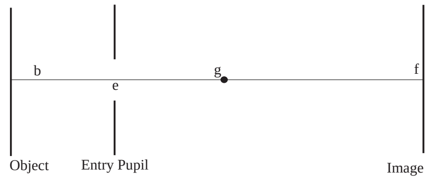


Lens file for Tackaberry-Muller system

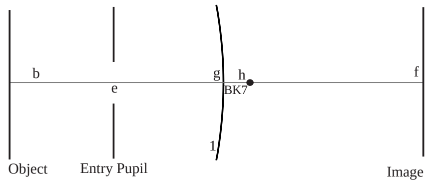
Surface	Distance	Radius	Material	Aperture
Object	10^{10}	flat	air	
Entry pupil	0.88	flat	air	0.18
1	0.21900	–3.5236	BK7	0.62
2	0.07280	–1.0527	air	0.62
3	0.22500	–4.4072	BK7	0.62
4	0.01360	–1.0704	air	0.62
5	0.52100	1.02491	BK7	0.62
6	0.11800	–0.9349	SF61	0.62
7	0.47485	7.94281	air	0.62
Image		flat		

DEVELOPMENTAL PROCESS

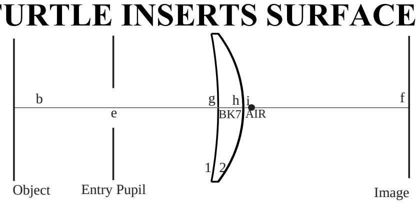
TURTLE STARTS AT POINT G ALONG MAIN AXIS B



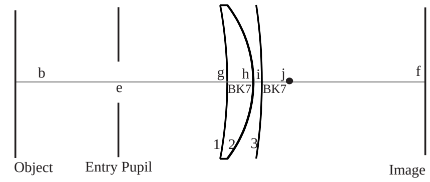
TURTLE INSERTS SURFACE 1

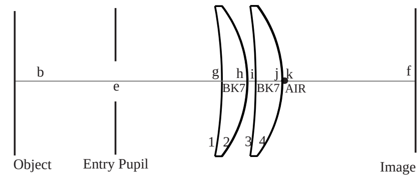


TURTLE INSERTS SURFACE 2

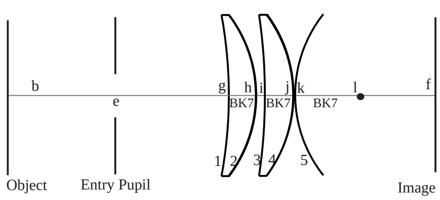


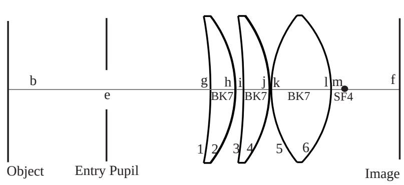
DEVELOPMENTAL PROCESS—CONTINUED

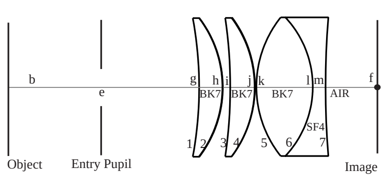




DEVELOPMENTAL PROCESS—CONTINUED

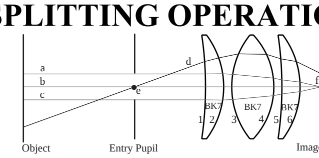




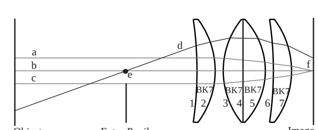


LENS SPLITTING OPERATION

LENS SYSTEM BEFORE LENS-SPLITTING OPERATION

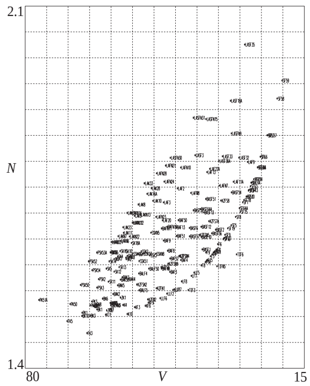


LENS SYSTEM AFTER LENS-SPLITTING OPERATION



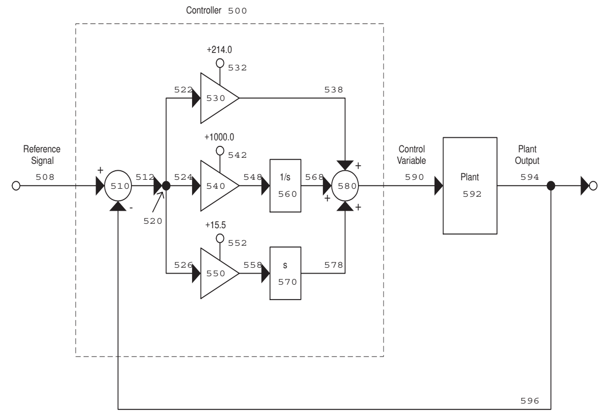
GLASS MUTATION

GLASS MAP FOR THE 199 TYPES OF GLASS IN THE SCHOTT CATALOG



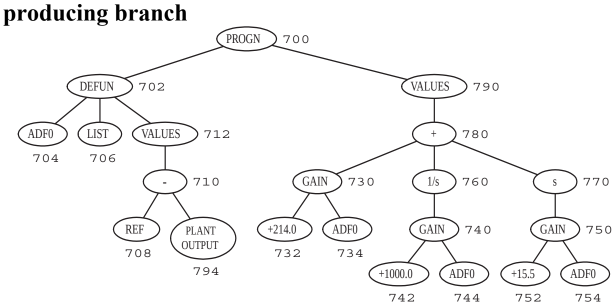
PID CONTROLLER

Block diagram of a plant and a PID controller composed of proportional (P), integrative (I), and derivative (D) blocks

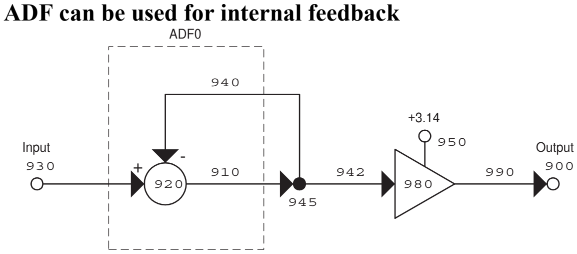


PROGRAM TREE REPRESENTATION FOR PID CONTROLLER

- **ADF can be used for reuse.**
- **Automatically defined function `ADF0` takes the difference between the reference signal and the plant output and makes this difference available to three points in the result-producing branch**



- **ADF can be used for internal feedback**



FUNCTION SET AND TERMINAL SET FOR TWO-LAG PLANT PROBLEM

- **The function set, F (for every part of the result-producing branch and any automatically defined functions except the arithmetic-performing subtrees) is**

F = {`GAIN`, `INVERTER`, `LEAD`, `LAG`, `LAG2`, `DIFFERENTIAL_INPUT_INTEGRATOR`, `DIFFERENTIATOR`, `ADD_SIGNAL`, `SUB_SIGNAL`, `ADD_3_SIGNAL`, `ADF0`, `ADF1`, `ADF2`, `ADF3`, `ADF4`}

- **The terminal set, T, (for every part of the result-producing branch and any automatically defined functions except the arithmetic-performing subtrees) is**

T = { `REFERENCE_SIGNAL`, `CONTROLLER_OUTPUT`, `PLANT_OUTPUT`, `CONSTANT_0`}

ARITHMETIC-PERFORMING SUBTREES FOR THE TWO-LAG PLANT PROBLEM

- Signal processing blocks `such as` `GAIN`, `LEAD`, `LAG`, and `LAG2` possess numerical parameter(s)
- Parameter values can be established by an arithmetic-performing subtree
- A constrained syntactic structure enforces a different function and terminal set for the arithmetic-performing subtrees (as opposed to all other parts of the program tree).
- Terminal set, T_{aps}, for the arithmetic-performing subtrees

$$T_{aps} = \{\Re\}$$

where $\Re$ denotes constant numerical terminals in the range from -1.0 to +1.0

- Function set, F_{aps}, for the arithmetic-performing subtrees

F_{aps} = {`ADD_NUMERIC`, `SUB_NUMERIC`}

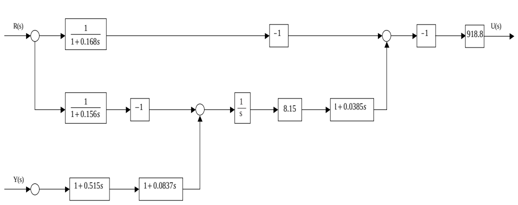
FITNESS MEASURE FOR TWO-LAG PLANT

- 10-element fitness measure
- The first eight elements of the fitness measure represent the eight choices of a particular one of two different values of the plant's internal gain, K (1.0 and 2.0), in conjunction with a particular one of two different values of the plant's time constant τ (0.5 and 1.0), in conjunction with a particular one of two different values for the height of the reference signal. The two reference signals are step functions that rise from 0 to 1 volts (or 1 microvolts) at t = 100 milliseconds.
- For each of these eight fitness cases, a transient analysis is performed in the time domain using the SPICE simulator. The contribution to fitness for each of these eight elements is

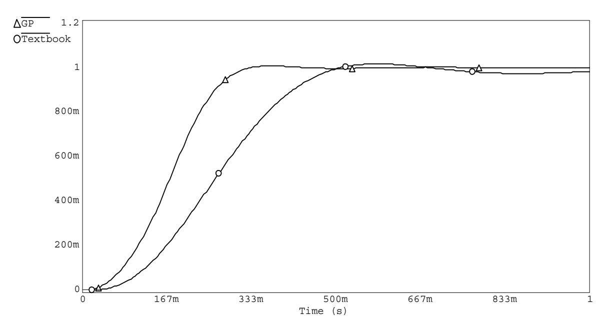
$$\int_{t=0}^{9.6} t\left|e(t)\right|A(e(t))B\,dt$$

- $e(t)$ is difference between plant output and reference signal.
- Multiplication by B (10^6. or 1) makes both reference signals equally influential.
- Additional weighting function, A, heavily penalizes non-compliant amounts of overshoot. A weights all variations up to 2% above the reference signal by 1.0, but others by 10.0.
- The 9th element of the fitness measure exposes the controller to an extreme spiked reference signal.
- The 10th element constrains the frequency of the control variable so as to avoid extreme high frequencies.

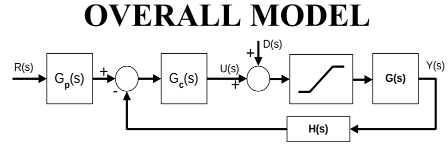
BEST-OF-RUN GENETICALLY EVOLVED CONTROLLER FROM GENERATION 32 FOR THE TWO-LAG PLANT



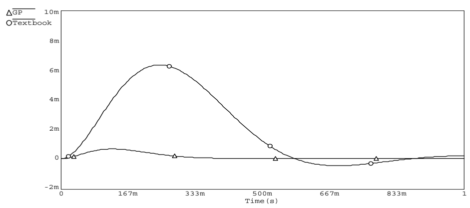
COMPARISON OF THE TIME-DOMAIN RESPONSE TO 1-VOLT STEP INPUT FOR THE EVOLVED CONTROLLER (TRIANGLES) AND THE BISHOP AND DORF CONTROLLER (SQUARES) FOR THE TWO-LAG PLANT WITH K=1 AND τ=1



OVERALL MODEL

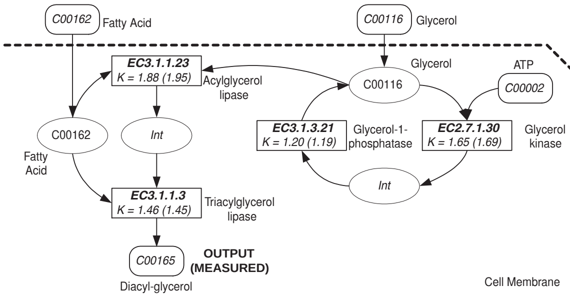


COMPARISON OF THE TIME-DOMAIN RESPONSE TO A 1-VOLT DISTURBANCE SIGNAL OF THE EVOLVED CONTROLLER(TRIANGLES) AND THE BISHOP AND DORF CONTROLLER (CIRCLES) FOR THE TWO-LAG PLANT WITH *K*=1 AND τ=1

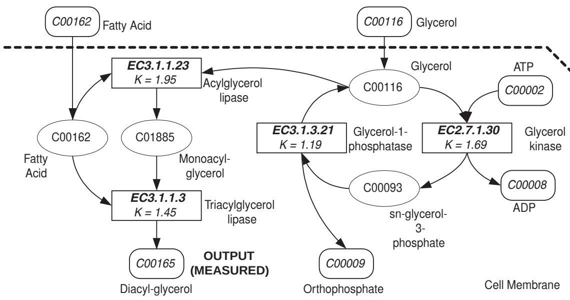


REVERSE ENGINEERING OF METABOLIC PATHWAYS (4-REACTION NETWORK IN PHOSPHOLIPID CYCLE)

BEST-OF-GENERATION 66



DESIRED



CROSS-DOMAIN FEATURES OF RUNS OF GENETIC PROGRAMMING USED TO EVOLVE DESIGNS FOR ANALOG CIRCUITS, OPTICAL LENS SYSTEMS, CONTROLLERS, ANTENNAS, MECHANICAL SYSTEMS, AND QUANTUM COMPUTING CIRCUITS

- **optical lens systems (Al-Sakran, Koza, and Jones, 2005; Koza, Al-Sakran, and Jones, 2005),**
- **analog electrical circuits (Koza, Bennett, Andre, and Keane 1996; Koza, Bennett, Andre, and Keane 1999),**
- **antennas (Lohn, Hornby, and Linden 2004; Comisky, Yu, and Koza 2000),**
- **controllers (Koza, Keane, Streeter, Mydlowec, Yu, and Lanza 2003; Keane, Koza, Streeter 2005),**
- **mechanical systems (Lipson 2004), and**
- **quantum computing circuits (Spector 2004)**

CROSS-DOMAIN FEATURES

- **Native representations are sufficient when working with genetic programming**

- **Genetic programming breeds simulatability**

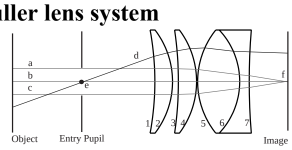
- **Genetic programming starts small**

- **Genetic programming frequently exploits a simulator's built-in assumption of reasonableness**

- **Genetic programming engineers around existing patents and creates novel designs more frequently than it creates infringing solutions**

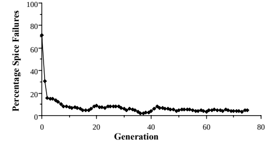
NATIVE REPRESENTATIONS ARE SUFFICIENT WHEN WORKING WITH GENETIC PROGRAMMING

Tackaberry-Muller lens system



Lens file for Tackaberry-Muller system

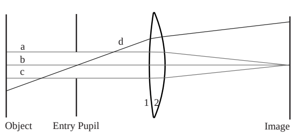
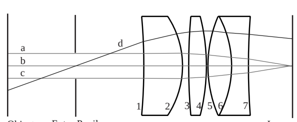
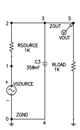
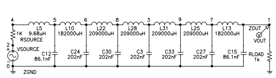
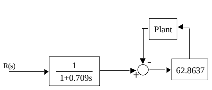
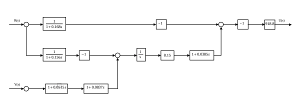
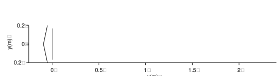
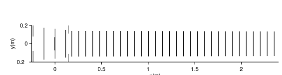
Surface	Distance	Radius	Material	Aperture
Object	10^{10}	flat	air	
Entry pupil	0.88	flat	air	0.18
1	0.21900	–3.5236	BK7	0.62
2	0.07280	–1.0527	air	0.62
3	0.22500	–4.4072	BK7	0.62
4	0.01360	–1.0704	air	0.62
5	0.52100	1.02491	BK7	0.62
6	0.11800	–0.9349	SF61	0.62
7	0.47485	7.94281	air	0.62
Image		flat		



GENETIC PROGRAMMING BREEDS SIMULATABILITY

Unsimulatable individuals

GP STARTS SMALL

Best-of-generation 0	Best-of-run
 Optical lens system	 Optical lens system
 Lowpass filter	 Lowpass filter
 Controller	 Controller
 Antenna	 Antenna

GENETIC PROGRAMMING ENGINEERS AROUND EXISTING PATENTS AND CREATES NOVEL DESIGNS MORE FREQUENTLY THAN IT CREATES INFRINGING SOLUTIONS

GENETIC PROGRAMMING FREQUENTLY EXPLOITS A SIMULATOR'S BUILT-IN ASSUMPTION OF REASONABLENESS

CHARACTERISTICS SUGGESTING THE USE OF GENETIC PROGRAMMING

(1) discovering the size and shape of the solution,
(2) reusing substructures,
(3) discovering the number of substructures,
(4) discovering the nature of the hierarchical references among substructures,
(5) passing parameters to a substructure,
(6) discovering the type of substructures (e.g., subroutines, iterations, loops, recursions, or storage),
(7) discovering the number of arguments possessed by a substructure,
(8) maintaining syntactic validity and locality by means of a developmental process, or
(9) discovering a general solution in the form of a parameterized topology containing free variables

MANY DIFFERENT GA/ES ENCODINGS HAVE BEEN SUCCESSFULLY USED

A mixture of real-valued variables, integer-valued variables, and categorical variables are encoded in the chromosome

L	.220	2	3	**C**	403.	3	6	**L**	.528	6	9	**L**	.041	9	0

- **Bit-string chromosome**

Resistor		2.5 Ω								Node 3			Node 6		
0	1	0	0	1	0	1	0	0	0	0	1	1	1	1	0

  - **The component type (a categorical variable) is encoded as 2 bits (01 = resistor, etc.)**
  - **The component value (real-valued number) is encoded as 8 bits**
  - **The node (integer-valued variable) to which the component's 1st lead is connected is encoded by 3 bits**
  - **The node (integer-valued variable) to which the component's 2nd lead is connected is encoded by 3 bits**
  - **Note that the number of nodes is capped at 8 (or assumed to be 8)**

IT IS OFTEN POSSIBLE TO USE THE GENETIC ALGORITHM (GA) OR EVOLUTION STRATEGIES EVEN WHEN THE SIZE AND SHAPE OF THE SOLUTION IS A MAJOR ISSUE

- **Variable-length genetic algorithm (VGA)**

- **Maintain constraints**

Chromosome #1

1st Component				2nd Component			
L	.220	1	2	**C**	403.	2	0

Chromosome #2

1st Component				2nd Component			
R	250.	0	1	**C**	100.	1	2

Nominal Offspring #1 is invalid

1st Component				2nd Component			
L	.220	1	2	**C**	100.	1	2

- **Penalize (in fitness measure)**
- **Delete**
- **Repair (most common method)**
- **Inundate**

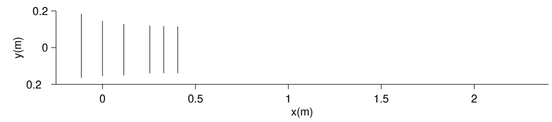
STRONG INDICATIONS FOR USING GENETIC ALGORITHM (GA) OR EVOLUTION STRATEGIES (ES)

- **The size and shape of the solution is known or fixed**

- **Ascertaining numerical parameters is the major issue**

- **Simplicity is a major consideration**
  - **On-chip evolution the algorithm's logic is implemented on the chip in hardware**

AUTOMATIC SYNTHESIS OF A YAGI-UDA WIRE ANTENNA USING GENETIC ALGORITHM (LINDEN 1997)



- **When the genetic algorithm (GA) operating on fixed-length character strings was used to synthesize a particular Yagi-Uda wire antenna by Linden (1997), the chromosome was based on**
  - **a particular number of reflectors (one) and**
  - **a particular number of directors.**

The chromosome encoded
- **the spacing between the parallel wires**
- **the length of each of the parallel wires**

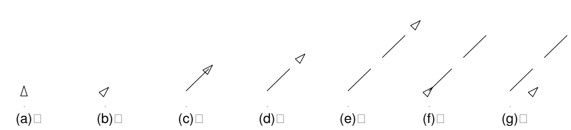
AUTOMATIC SYNTHESIS OF A YAGI-UDA WIRE ANTENNA USING GENETIC ALGORITHM (LINDEN 1997) — CONTINUED

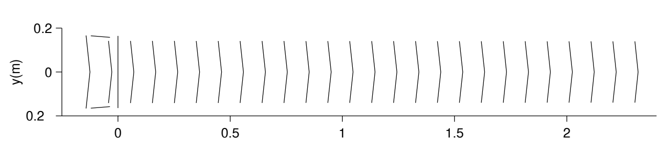
- **When the genetic algorithm (GA) operating on fixed-length character strings was used to synthesize a Yagi-Uda wire antenna (Linden 1997), the following <u>decisions were made by the human user prior to the start of the run</u>:**
  - **(1) the number of reflectors (one),**
  - **(2) the number of directors,**
  - **(3) the fact that the driven element, the directors, and the reflector are all single straight wires,**
  - **(4) the fact that the driven element, the directors, and the reflector are all arranged in parallel,**
  - **(5) the fact that the energy source (via the transmission line) is connected only to single straight wire (the driven element) — that is, all the directors and reflectors are parasitically coupled**
- **Characteristics (3), (4), and (5) are essential characteristics of the Yagi-Uda antenna, namely an antenna with multiple parallel parasitically coupled straight-line directors, a single parallel parasitically coupled straight-line reflector, and a straight-line driven element. That it, the GA run assumed that the answer would be a Yagi-Uda antenna.**

AUTOMATIC SYNTHESIS OF A WIRE ANTENNA

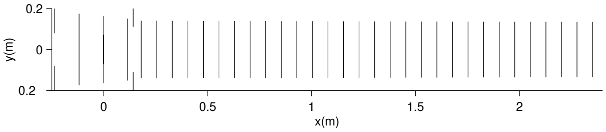
EXAMPLE OF TURTLE FUNCTIONS USED TO CREATE WIRE ANTENNA

```
(PROGN3
  (TURN-RIGHT 0.125)
  (LANDMARK
    (REPEAT 2
      (PROGN2
        (DRAW 1.0 HALF-MM-WIRE)
        (DRAW 0.5 NO-WIRE)))
  (TRANSLATE-RIGHT 0.125 0.75))
```





BEST-OF-RUN ANTENNA FROM GENERATION 90 — FITNESS OF-16.04

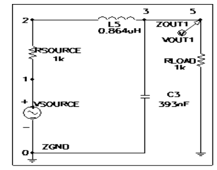


- **The GP run discovered**
  - **(1) the number of reflectors (one),**
  - **(2) the number of directors,**
  - **(3) the fact that the driven element, the directors, and the reflector are all single straight wires,**
  - **(4) the fact that the driven element, the directors, and the reflector are all arranged in parallel,**
  - **(5) the fact that the energy source (via the transmission line) is connected only to single straight wire (the driven element) — that is, all the directors and reflectors are parasitically coupled**

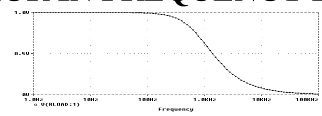
- **Characteristics (3), (4), and (5) are essential characteristics of the Yagi-Uda antenna, namely an antenna with multiple parallel parasitically coupled straight-line directors, a single parallel parasitically coupled straight-line reflector, and a straight-line driven element.**

REUSE LOWPASS FILTER USING ADFS

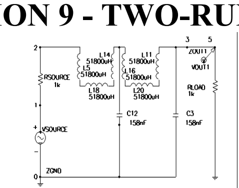
GENERATION 0 – ONE-RUNG LADDER



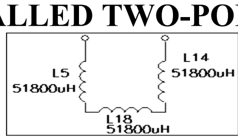
BEHAVIOR IN FREQUENCY DOMAIN



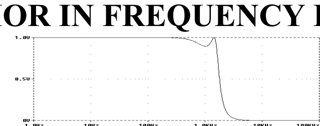
REUSE LOWPASS FILTER USING ADFS GENERATION 9 - TWO-RUNG LADDER



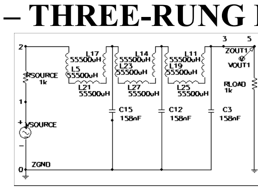
TWICE-CALLED TWO-PORTED `ADF0`



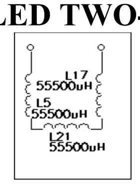
BEHAVIOR IN FREQUENCY DOMAIN



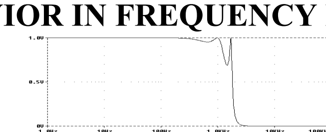
REUSE LOWPASS FILTER USING ADFS GEN 16 – THREE-RUNG LADDER



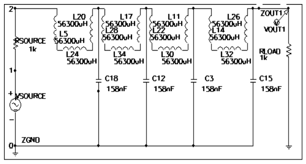
THRICE-CALLED TWO-PORTED `ADF0`



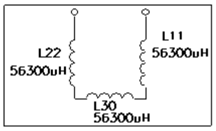
BEHAVIOR IN FREQUENCY DOMAIN



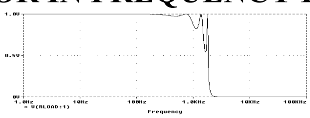
REUSE
LOWPASS FILTER USING ADFs
GEN 20 – FOUR-RUNG LADDER



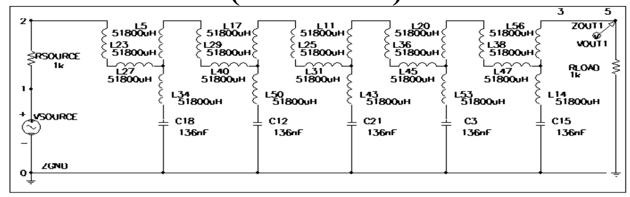
QUADRUPLY-CALLED TWO-PORTED ADF0



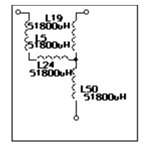
BEHAVIOR IN FREQUENCY DOMAIN



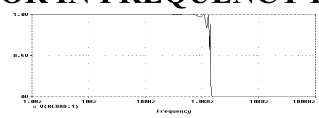
REUSE
LOWPASS FILTER USING ADFs
GENERATION 31 — TOPOLOGY OF CAUER (ELLIPTIC) FILTER



QUINTUPLY-CALLED THREE-PORTED ADF0



BEHAVIOR IN FREQUENCY DOMAIN



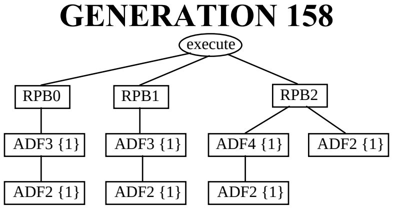
PASSING A PARAMETER TO A SUBSTRUCTURE

- **The set of potential terminals for each construction-continuing subtree of an automatically defined function, $T_{ccs\text{-}adf\text{-}potential}$, is**

$T_{ccs\text{-}adf\text{-}potential}$ = {ARG0}

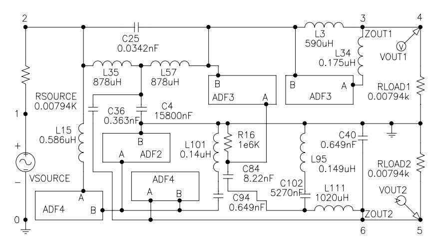
EMERGENCE OF A PARAMETERIZED ARGUMENT IN A CIRCUIT SUBSTRUCTURE

HIERARCHY OF BRANCHES FOR THE BEST-OF-RUN CIRCUIT- FROM GENERATION 158



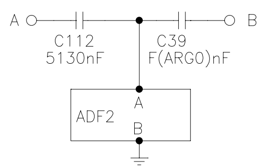
PASSING A PARAMETER TO A SUBSTRUCTURE

BEST-OF-RUN CIRCUIT FROM



THREE-PORTED AUTOMATICALLY DEFINED FUNCTION ADF3 OF THE BEST-OF-RUN CIRCUIT FROM GENERATION 158

ADF3 CONTAINS CAPACITOR C39 PARAMETERIZED BY DUMMY VARIABLE ARG0



THE FIRST RESULT-PRODUCING BRANCH, RPB0, CALLING ADF3

```
(PARALLEL0 (L (+ (- 1.883196E-01 (- -9.095883E-02 5.724576E-
01)) (- 9.737455E-01 -9.452780E-01)) (FLIP END)) (SERIES (C (+
(+ -6.668774E-01 -8.770285E-01) 4.587758E-02) (NOP END))
(SERIES END END (PARALLEL1 END END END END)) (FLIP
(SAFE_CUT))) (PAIR_CONNECT_0 END END END) (PAIR_CONNECT_0 (L
(+ -7.220122E-01 4.896697E-01) END) (L (- -7.195599E-01
3.651142E-02) (SERIES (C (+ -5.111248E-01 (- (- -6.137950E-01
-5.111248E-01) (- 1.883196E-01 (- -9.095883E-02 5.724576E-
01)))) END) (SERIES END END (adf3 6.196514E-01)) (NOP END)))
(NOP END)))
```

AUTOMATICALLY DEFINED FUNCTION ADF3

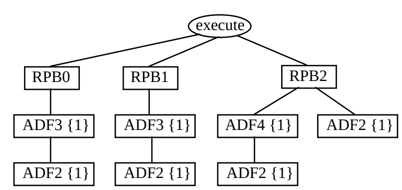
```
(C (+ (- (+ (+ (+ 5.630820E-01 (- 9.737455E-01 -9.452780E-01))
(+ ARG0 6.953752E-02)) (- (- 5.627716E-02 (+ 2.273517E-01 (+
1.883196E-01 (+ 9.346950E-02 (+ -7.220122E-01 (+ 2.710414E-02
1.397491E-02)))))) (- (+ (- 2.710414E-02 -2.807583E-01) (+ -
6.137950E-01 -8.554120E-01)) (- -8.770285E-01 (- -4.049602E-01
-2.192044E-02))))) (+ (+ 1.883196E-01 (+ (+ (+ (+ 9.346950E-02
(+ -7.220122E-01 (+ 2.710414E-02 1.397491E-02))) (- 4.587758E-
02 -2.340137E-01)) 3.226026E-01) (+ -7.220122E-01 (- -
9.131658E-01 6.595502E-01)))) 3.660116E-01)) 9.496355E-01)
(THREE_GROUND_0 (C (+ (- (+ (+ (+ 5.630820E-01 (- 9.737455E-01
-9.452780E-01)) (+ (- (- -7.195599E-01 3.651142E-02) -
9.761651E-01) (- (+ (- (- -7.195599E-01 3.651142E-02) -
9.761651E-01) 6.953752E-02) 3.651142E-02))) (- (- 5.627716E-02
(- 1.883196E-01 (- -9.095883E-02 5.724576E-01))) (- (+ (-
2.710414E-02 -2.807583E-01) (+ -6.137950E-01 (+ ARG0
6.953752E-02))) (- -8.770285E-01 (- -4.049602E-01 -2.192044E-
02))))) (+ (+ 1.883196E-01 -7.195599E-01) 3.660116E-01))
9.496355E-01) (NOP (FLIP (PAIR_CONNECT_0 END END END)))) (FLIP
(SERIES (FLIP (FLIP (FLIP END))) (C (- (+ 6.238477E-01
6.196514E-01) (+ (+ (- (- 4.037348E-01 4.343444E-01) (+ -
7.788187E-01 (+ (+ (- -8.786904E-01 1.397491E-02) (- -
6.137950E-01 (- (+ (- 2.710414E-02 -2.807583E-01) (+ -
6.137950E-01 -8.554120E-01)) (- -8.770285E-01 (- -4.049602E-01
-2.192044E-02))))) (+ (+ 7.215142E-03 1.883196E-01) (+
7.733750E-01 4.343444E-01))))) (- (- -9.389297E-01 5.630820E-
01) (+ -5.840433E-02 3.568947E-01))) -8.554120E-01)) (NOP
END)) END)) (FLIP (adf2 9.737455E-01))))
```


ADF3 DOES THREE THINGS

- **The structure that develops out of ADF3 includes a capacitor C112 whose value (5,130 uF) is not a function of its dummy variable, ARG0.**
- **The structure that develops out of ADF3 has one hierarchical reference to ADF2. As previously mentioned, the invocation of ADF2 is done with a constant (9.737455E-01) so this invocation of ADF2 produces a 259 μH inductor.**
- **Most importantly, the structure that develops out of ADF3 creates a capacitor (C39) whose sizing, F(ARG0), is a function of the dummy variable, ARG0, of automatically defined function ADF3. Capacitor C39 has different sizing on different invocations of automatically defined function ADF3.**
- **The combined effect of ADF3 is to insert the following three components:**
  - **an unparameterized 5,130 uF capacitor,**
  - **a parameterized capacitor C39 whose component value is dependent on ARG0 of ADF3, and**
  - **a parameterized inductor (created by ADF2) whose sizing is parameterized, but which, in practice, is called with a constant value.**

EMERGENCE OF A PARAMETERIZED ARGUMENT IN A CIRCUIT SUBSTRUCTURE

HIERARCHY OF BRANCHES FOR THE BEST-OF-RUN CIRCUIT- FROM GENERATION 158



FREE VARIABLE (INPUT) AND CONDITIONALS

SOLVING A QUADRATIC EQUATION USING THE GENETIC ALGORITHM

• **Suppose we want the 2 roots of the quadratic equation**

$$1x^2 - 3x + 2 = 0$$

• **Using the genetic algorithm (GA) operating on a fixed-length character string, we can search a space of encodings using an alphabet size of 2 (i.e., binary) of length, say, 16 representing two real numbers (each with, say, 4 bits to left of the "decimal" point). After running the GA, a solution is**

0	0	0	1	↓ 0	0	0	0	0	0	1	0	↓ 0	0	0	0

1.0 **2.0**

• **Alternatively, we could use a "floating point" genetic algorithm (GA) to search a space of 2-part encodings. A solution is**

1.0	**2.0**

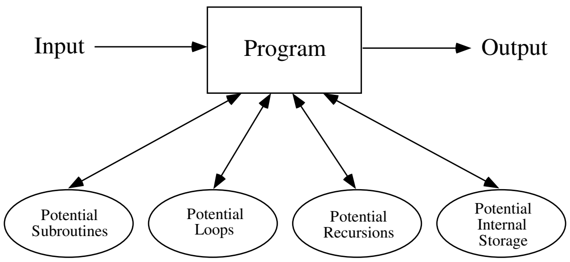
• **In either case, the result is a solution to <u>ONE INSTANCE</u> of the quadratic equation problem.**

SOLVING A QUADRATIC EQUATION USING GENETIC PROGRAMMING (GP)

• **Using genetic programming (GP), we can solve the general, parameterized quadratic equation**

$$ax^2 + bx + c = 0$$

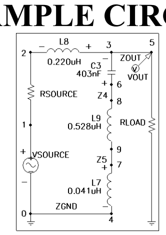
by searching the space of computer programs for a program that takes *a*, *b*, and *c* as inputs



• **The result is a solution to <u>ALL INSTANCES</u> of the quadratic equation problem**

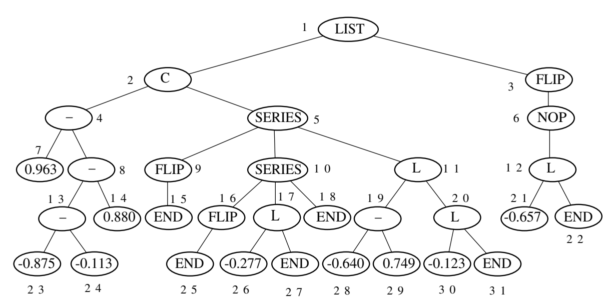
GENERAL APPEARANCE OF ONE POSSIBLE CHROMOSOME ENCODING USED TO SOLVE <u>ONE INSTANCE</u> OF A CIRCUIT PROBLEM USING THE GENETIC ALGORITHM (GA) OPERATING ON FIXED-LENGTH CHARACTER STRINGS

EXAMPLE CIRCUIT



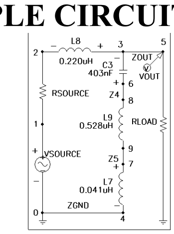
1^{st} Component				2^{nd} Component				3^{rd} Component				4^{th} Component			
L	.220	2	3	C	403.	3	6	L	.528	6	9	L	.041	9	0

THE GENERAL APPEARANCE OF EXPRESSIONS USED TO SOLVE <u>ONE INSTANCE</u> OF A CIRCUIT PROBLEM USING GENETIC PROGRAMMING (GP) IN *GENETIC PROGRAMMING III* (1999)



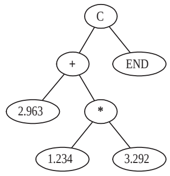

```
(LIST (C (– 0.963 (– (– -0.875 -0.113) 0.880)) (series (flip
end) (series (flip end) (L -0.277 end) end) (L (– -0.640
0.749) (L -0.123 end)))) (flip (nop (L -0.657 end)))))
```

EXAMPLE CIRCUIT (GEN 0)

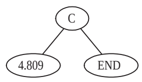


VALUE-SETTING SUBTREES—3 WAYS

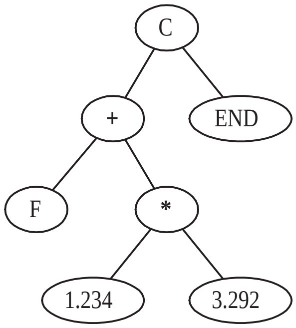
ARITHMETIC-PERFORMING SUBTREE



SINGLE PERTURBABLE CONSTANT



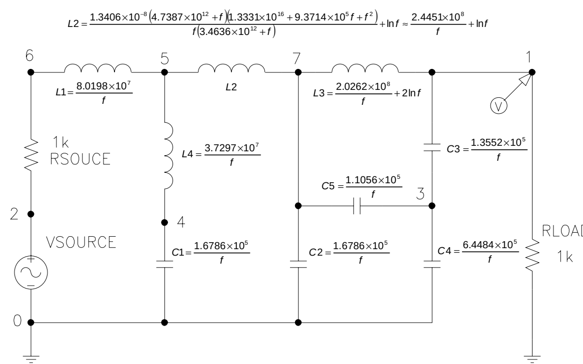
FREE VARIABLE



PARAMETERIZED TOPOLOGY FOR "GENERALIZED" LOWPASS FILTER

VARIABLE CUTOFF LOWPASS FILTER

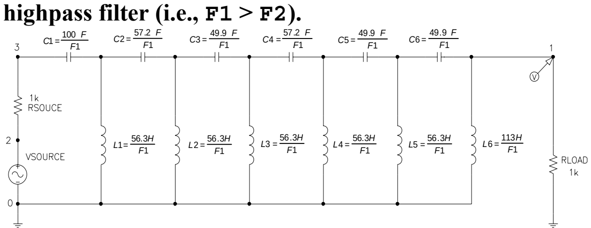
- Want lowpass filter whose passband ends at frequencies f = 1,000, 1,780, 3,160, 5,620, 10,000, 17,800, 31,600, 56,200, 100,000 Hz



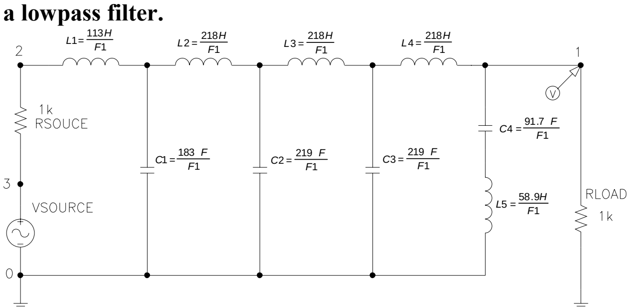
PARAMETERIZED TOPOLOGY USING CONDITIONAL DEVELOPMENTAL OPERATORS (GENETIC SWITCH)

VARIABLE-CUTOFF LOWPASS/HIGHPASS FILTER CIRCUIT

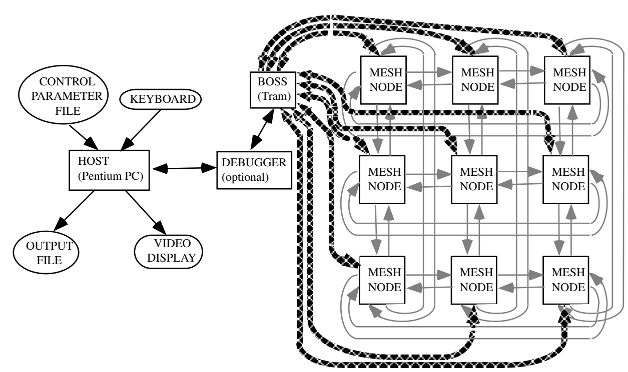
- Best-of-run circuit from generation 93 when inputs call for a highpass filter (i.e., `F1` > `F2`).



- Best-of-run circuit from generation 93 when inputs call for a lowpass filter.



PARALLELIZATION BY SUBPOPULATIONS ("ISLAND" OR "DEME" MODEL OR "DISTRIBUTED GENETIC ALGORITHM")



- Like Hormel, Get Everything Out of the Pig, Including the Oink
- Keep on Trucking
- It Takes a Licking and Keeps on Ticking
- The Whole is Greater than the Sum of the Parts

PETA-OPS

- Human brain operates at 10^{12} neurons operating at 10^{3} per second = 10^{15} ops per second
- 10^{15} ops = 1 peta-op = 1 bs (brain second)

GENETIC PROGRAMMING OVER 15-YEAR PERIOD 1987–2002

System	Period of usage	Petacycles (10^{15}cycles) per day for entire system	Speed-up over previous system	Speed-up over first system in this table	Human-competitive results
Serial Texas Instruments LISP machine	1987–1994	0.00216	1 (base)	1 (base)	0
64-node Transtech transputer parallel machine	1994–1997	0.02	9	9	2
64-node Parsytec parallel machine	1995–2000	0.44	22	204	12
70-node Alpha parallel machine	1999–2001	3.2	7.3	1,481	2
1,000-node Pentium II parallel machine	2000–2002	30.0	9.4	13,900	12

PROGRESSION OF RESULTS

System	Period	Speed-up	Qualitative nature of the results produced by genetic programming
Serial LISP machine	1987–1994	1 (base)	• Toy problems of the 1980s and early 1990s from the fields of artificial intelligence and machine learning
64-node Transtech 8-biy transputer	1994–1997	9	•Two human-competitive results involving one-dimensional discrete data (not patent-related)
64-node Parsytec parallel machine	1995–2000	22	• One human-competitive result involving two-dimensional discrete data • Numerous human-competitive results involving continuous signals analyzed in the frequency domain • Numerous human-competitive results involving 20th-century patented inventions
70-node Alpha parallel machine	1999–2001	7.3	• One human-competitive result involving continuous signals analyzed in the time domain • Circuit synthesis extended from topology and sizing to include routing and placement (layout)
1,000-node Pentium II parallel machine	2000–2002	9.4	• Numerous human-competitive results involving continuous signals analyzed in the time domain • Numerous general solutions to problems in the form of parameterized topologies • Six human-competitive results duplicating the functionality of 21st-century patented inventions
Long (4-week) runs of 1,000-node Pentium II parallel machine	2002	9.3	• Generation of two patentable new inventions

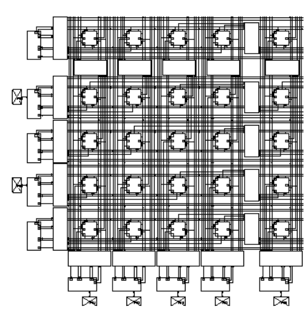
PROGRESSION OF QUALITATIVELY MORE SUBSTANTIAL RESULTS PRODUCED BY GENETIC PROGRAMMING IN RELATION TO FIVE ORDER-OF-MAGNITUDE INCREASES IN COMPUTATIONAL POWER

- toy problems
- human-competitive results not related to patented inventions
- 20th-century patented inventions
- 21st-century patented inventions
- patentable new inventions

EVOLVABLE HARDWARE

RAPIDLY RECONFIGURABLE FIELD-PROGRAMMABLE GATE ARRAYS (FPGAs)

SMALL 5 BY 5 CORNER OF XILINX XC6216 FPGA



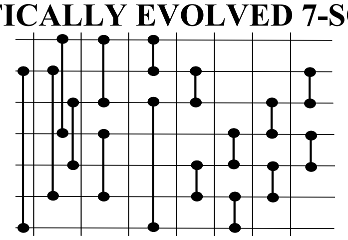
EVOLVABLE HARDWARE

RAPIDLY RECONFIGURABLE FIELD-PROGRAMMABLE GATE ARRAYS (FPGAs)

SORTING NETWORKS

- **A 16-step 7-sorter was evolved that has two fewer steps than the sorting network described in O'Connor and Nelsons' patent (1962) and that has the same number of steps as the 7-sorter that was devised by Floyd and Knuth subsequent to the patent and described in Knuth 1973.**

GENETICALLY EVOLVED 7-SORTER



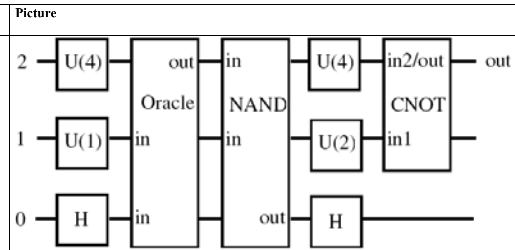
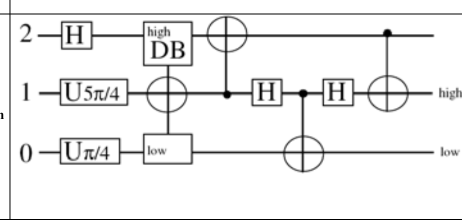
FUNDAMENTAL DIFFERENCES BETWEEN GP AND OTHER APPROACHES TO AI AND ML

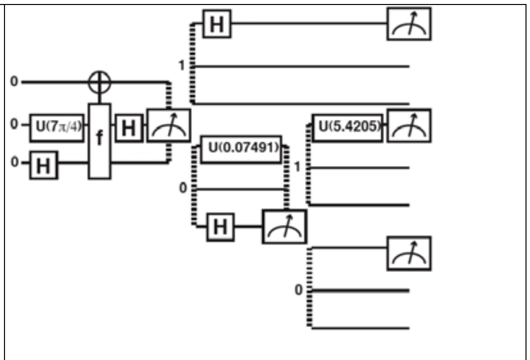
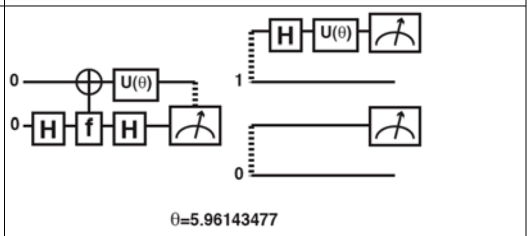
(1) Representation: Genetic programming overtly conducts it search for a solution to the given problem in program space.
(2) Role of point-to-point transformations in the search: Genetic programming does not conduct its search by transforming a single point in the search space into another single point, but instead transforms a set of points into another set of points.
(3) Role of hill climbing in the search: Genetic programming does not rely exclusively on greedy hill climbing to conduct its search, but instead allocates a certain number of trials, in a principled way, to choices that are known to be inferior.
(4) Role of determinism in the search: Genetic programming conducts its search probabilistically.
(5) Role of an explicit knowledge base: None.
(6) Role of formal logic in the search: None.
(7) Underpinnings of the technique: Biologically inspired.

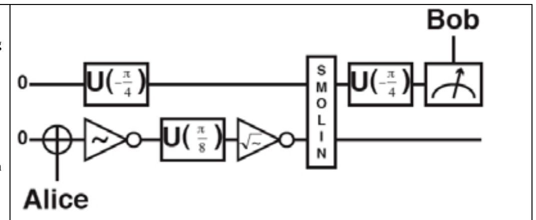
EIGHT CRITERIA FOR HUMAN-COMPETITIVENESS

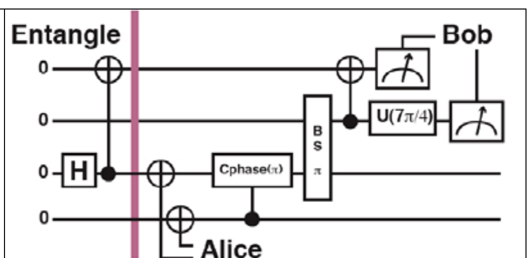
	Criterion
A	**The result was patented as an invention in the past, is an improvement over a patented invention, or would qualify today as a patentable new invention.**
B	**The result is equal to or better than a result that was accepted as a new scientific result at the time when it was published in a peer-reviewed scientific journal.**
C	**The result is equal to or better than a result that was placed into a database or archive of results maintained by an internationally recognized panel of scientific experts.**
D	**The result is publishable in its own right as a new scientific result—independent of the fact that the result was mechanically created.**
E	**The result is equal to or better than the most recent human-created solution to a long-standing problem for which there has been a succession of increasingly better human-created solutions.**
F	**The result is equal to or better than a result that was considered an achievement in its field at the time it was first discovered.**
G	**The result solves a problem of indisputable difficulty in its field.**
H	**The result holds its own or wins a regulated competition involving human contestants (in the form of either live human players or human-written computer programs).**

37 HUMAN-COMPETITIVE RESULTS (LIST AS OF APRIL 2004)

Claimed instance	**Picture**
Creation of a better-than-classical quantum algorithm for the Deutsch-Jozsa "early promise" problem **Spector, Barnum, and Bernstein 1998**	
Creation of a better-than-classical quantum algorithm for Grover's database search problem **Spector, Barnum, and Bernstein 1999**	

Creation of a quantum algorithm for the depth-two AND/OR query problem that is better than any previously published result **Spector, Barnum, Bernstein, and Swamy 1999; Barnum, Bernstein, and Spector 2000**	
Creation of a quantum algorithm for the depth-one OR query problem that is better than any previously published result **Barnum, Bernstein, and Spector 2000**	

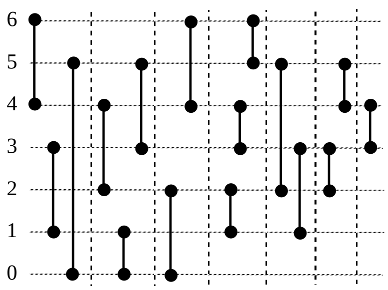
Creation of a protocol for communicating information through a quantum gate that was previously thought not to permit such communication **Spector and Bernstein 2003**	To understand one needs to know what the Smolin gate is and this is given in smolin-gate.jpg $\text{Smolin} = \begin{bmatrix} \frac{1}{\sqrt{2}} & 0 & 0 & \frac{1}{\sqrt{2}} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ \frac{1}{\sqrt{2}} & 0 & 0 & -\frac{1}{\sqrt{2}} \end{bmatrix}$

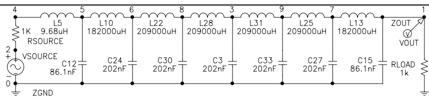
Creation of a novel variant of quantum dense coding **Spector and Bernstein 2003**	To understand one needs to know what the BS gate is and this is given to bs-gate.jpg $BS(\theta) = \begin{bmatrix} \cos(\theta) & 0 & 0 & \sin(\theta) \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ \sin(\theta) & 0 & 0 & -\cos(\theta) \end{bmatrix}$

Creation of a soccer-playing program that won its first two games in the Robo Cup 1997 competition **Luke 1998**	
Creation of a soccer-playing program that ranked in the middle of the field of 34 human-written programs in the Robo Cup 1998 competition **Andre and Teller 1999**	

<table>
<tr><td>Creation of four different algorithms for the transmembrane segment identification problem for proteins

Sections 18.8 and 18.10 of Genetic Programming II and sections 16.5 and 17.2 of Genetic Programming III</td>
<td>"0-2-4 rule" from section 16.5 of Genetic Programming III
<table>
<tr><th>Residue</th><th>Increm ent</th></tr>
<tr><td>A, F, I, L, M, or V</td><td>0</td></tr>
<tr><td>C, D, G, H, K, N, P, Q, R, S, T, W, or Y</td><td>+2</td></tr>
<tr><td>E</td><td></td></tr>
</table></td></tr>
<tr><td>Creation of a sorting network for seven items using only 16 steps

Sections 21.4.4, 23.6, and 57.8.1 of Genetic Programming III</td>
<td>
</td></tr>
<tr><td>Rediscovery of the Campbell ladder topology for lowpass and highpass filters

Section 25.15.1 of Genetic Programming III</td>
<td></td></tr>
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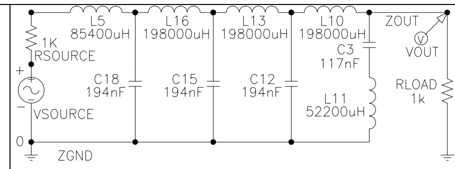
<tr><td>Rediscovery of the Zobel "M-derived half section" and "constant K" filter sections

Section 25.15.2 of Genetic Programming III</td>
<td>
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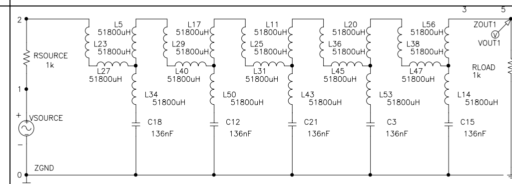
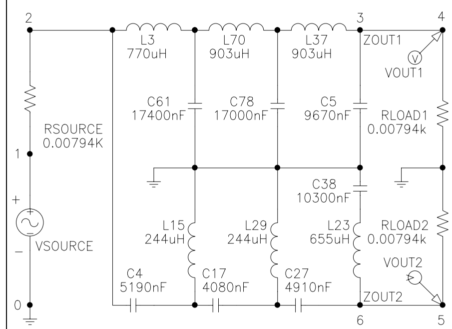
<tr><td>Rediscovery of the Cauer (elliptic) topology for filters

Section 27.3.7 of Genetic Programming III</td>
<td></td></tr>
<tr><td>Automatic decomposition of the problem of synthesizing a crossover (woofer-tweeter) filter

Section 32.3 of Genetic Programming III</td>
<td>
</td></tr>
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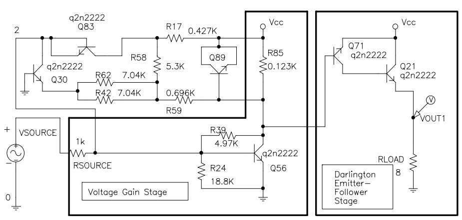
<table>
<tr><td>Rediscovery of a recognizable voltage gain stage and a Darlington emitter-follower section of an amplifier and other circuits

Section 42.3 of Genetic Programming III</td>
<td>
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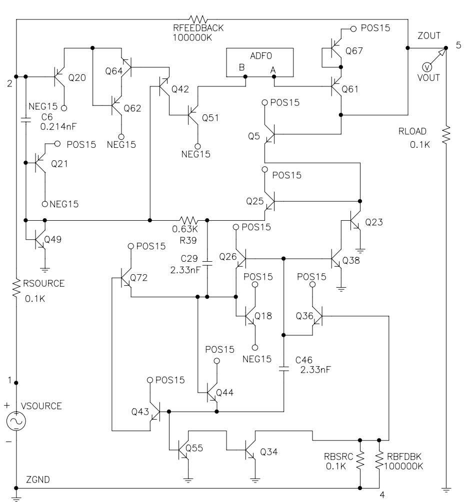
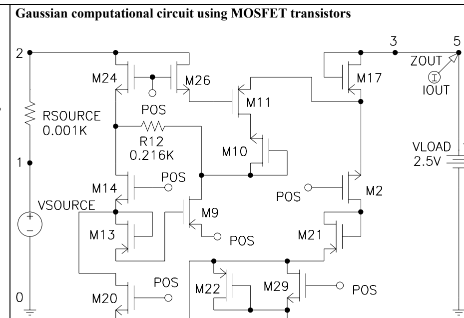
<tr><td>Synthesis of 60 and 96 decibel amplifiers

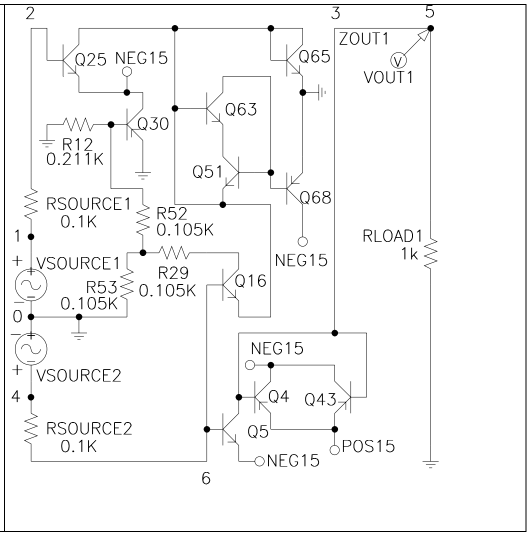
Section 45.3 of Genetic Programming III</td>
<td>
</td></tr>
</table>

<table>
<tr><td>Synthesis of analog computational circuits for squaring, cubing, square root, cube root, logarithm, and Gaussian functions

Section 47.5.3 of Genetic Programming III</td>
<td>Gaussian computational circuit using MOSFET transistors

</td></tr>
</table>

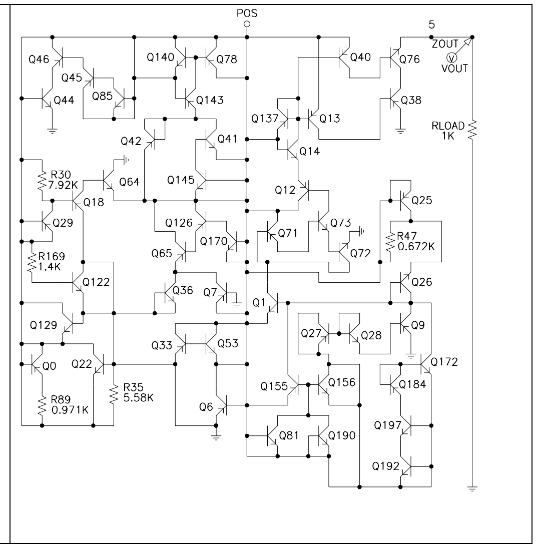
Synthesis of a real-time analog circuit for time-optimal control of a robot

Section 48.3 of *Genetic Programming III*



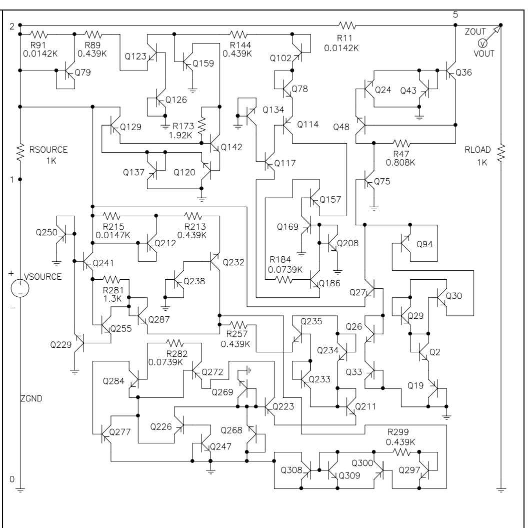
Synthesis of an electronic thermometer

Section 49.3 of *Genetic Programming III*



Synthesis of a voltage reference circuit

Section 50.3 of *Genetic Programming III*



Creation of a cellular automata rule for the majority classification problem that is better than the Gacs-Kurdyumov-Levin (GKL) rule and all other known rules written by humans

Andre, Bennett, and Koza 1996 and section 58.4 of *Genetic Programming III*

Rule	State Transition Rule	Accuracy
Gacs-Kurdyumov-Levin (GKL) 1978 human-written	00000000 01011111 00000000 01011111 00000000 01011111 00000000 01011111 00000000 01011111 11111111 01011111 00000000 01011111 11111111 01011111	8l.6%
Davis 1995 human-written	00000000 00101111 00000011 01011111 00000000 00011111 11001111 00011111 00000000 00101111 11111100 01011111 00000000 00011111 11111111 00011111	81.800%.
Das (1995) human-written	00000111 00000000 00000111 11111111 00001111 00000000 00001111 11111111 00001111 00000000 00000111 11111111 00001111 00110001 00001111 11111111	82.178%
Best rule evolved by genetic programming (1999)	00000101 00000000 01010101 00000101 00000101 00000000 01010101 00000101 01010101 11111111 01010101 11111111 01010101 11111111 01010101 11111111	82.326%

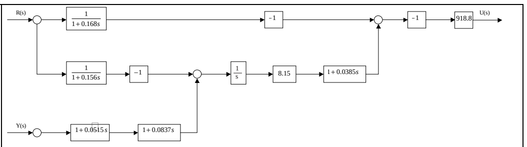
Creation of motifs that detect the D–E–A–D box family of proteins and the manganese superoxide dismutase family

Section 59.8 of *Genetic Programming III*

`[IV]-[lim]-D-E-[AI]-D-[rnek]-[lim]-[lim]-[limeqdnrsk]`

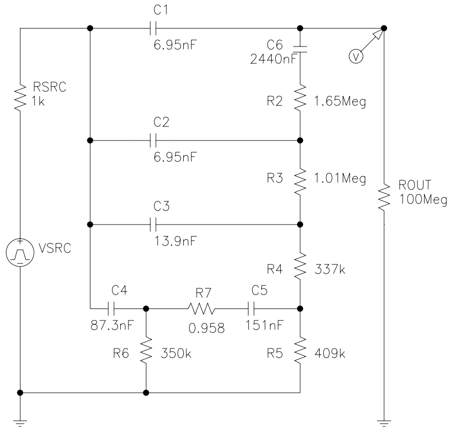
Synthesis of topology for a PID-D2 (proportional, integrative, derivative, and second derivative) controller

Section 3.7 of *Genetic Programming IV*



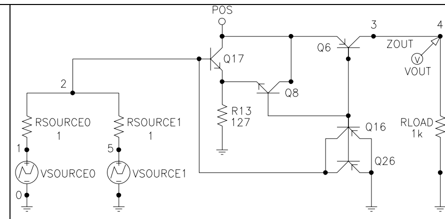
Synthesis of an analog circuit equivalent to Philbrick circuit

Section 4.3 of *Genetic Programming IV*

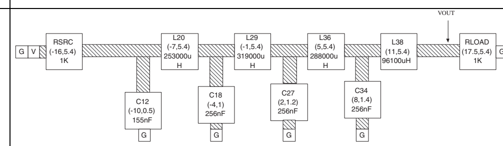


Synthesis of a NAND circuit

Section 4.4 of *Genetic Programming IV*

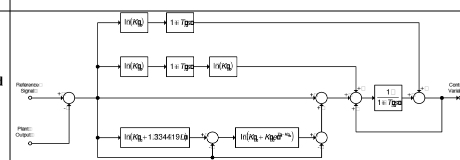


Simultaneous synthesis of topology, sizing, placement, and routing of analog electrical circuits



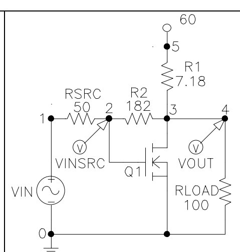
Synthesis of topology for a PID (proportional, integrative, and derivative) controller

Chapter 5 of *Genetic Programming IV*



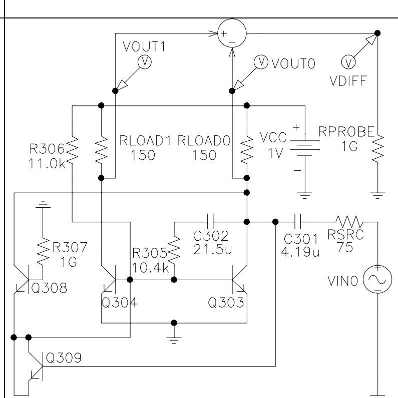
Rediscovery of negative feedback

Chapter 14 of *Genetic Programming IV*



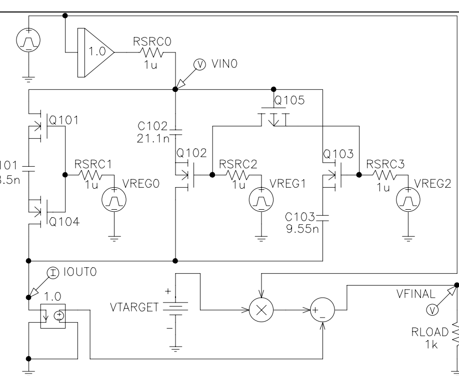
Synthesis of a low-voltage balun circuit

Section 15.4.1 of *Genetic Programming IV*



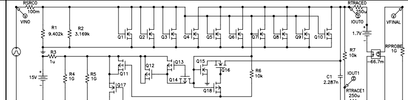
Synthesis of a mixed analog-digital variable capacitor circuit

Section 15.4.2 of *Genetic Programming IV*



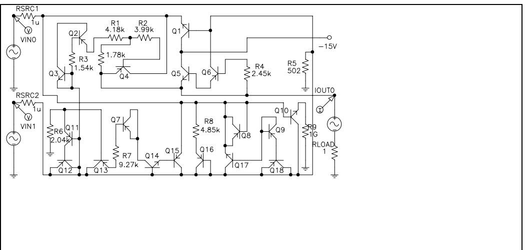
Synthesis of a high-current load circuit

Section 15.4.3 of *Genetic Programming IV*



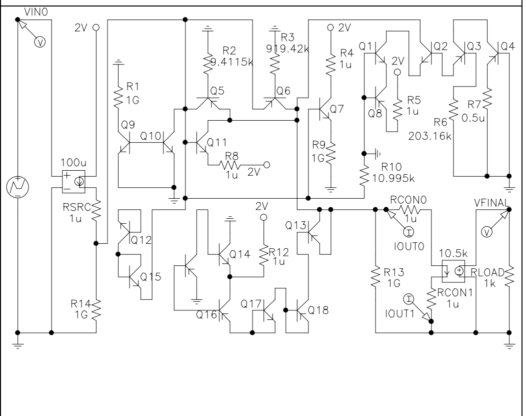
Synthesis of a voltage-current conversion circuit

Section 15.4.4 of *Genetic Programming IV*



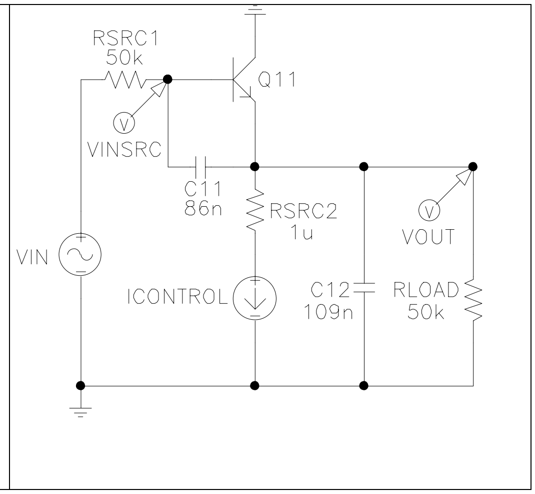
Synthesis of a cubic function generator

Section 15.4.5 of *Genetic Programming IV*



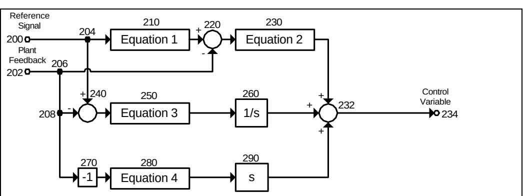
Synthesis of a tunable integrated active filter

Section 15.4.6 of *Genetic Programming IV*



Creation of PID tuning rules that outperform the Ziegler-Nichols and Åström-Hägglund tuning rules

Chapter 12 of *Genetic Programming IV*



The topology (above) was not evolved, but was the standard PID topology. Evolved equations for $K_{p\text{-}final}$, $K_{i\text{-}final}$, $K_{d\text{-}final}$, and b_{final}:

$$K_{p\text{-}final} = 0.72 * K_u * e^{\frac{-1.6}{K_u} + \frac{1.2}{K_u^2}} - .0012340 * T_u - 6.1173 * 10^{-6}$$

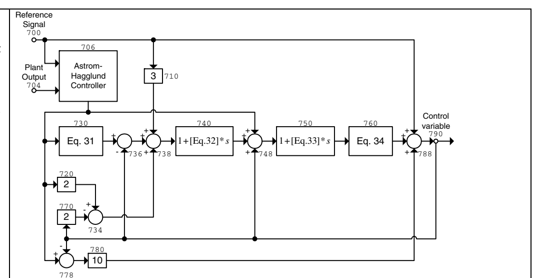
$$K_{i\text{-}final} = \frac{0.72 * K_u * e^{\frac{-1.6}{K_u} + \frac{1.2}{K_u^2}}}{0.59 * T_u * e^{\frac{-1.3}{K_u} + \frac{0.38}{K_u^2}}} - .068525 * \frac{K_u}{T_u}$$

$$K_{d\text{-}final} = 0.108 * K_u * T_u * e^{\frac{-1.6}{K_u} + \frac{1.2}{K_u^2}} * e^{\frac{-1.4}{K_u} + \frac{0.56}{K_u^2}} - 0.0026640 \left(e^{T_u}\right)^{\log\left(1.6342^{\log K_u}\right)}$$

$$b_{final} = 0.25 * e^{\frac{0.56}{K_u} + \frac{-0.12}{K_u^2}} + \frac{K_u}{e^{K_u}}$$

Creation of three non-PID controllers that outperform a PID controller that uses the Ziegler-Nichols or Åström-Hägglund tuning rules

Chapter 13 of *Genetic Programming IV*



The above topology and equations 31, 32, 33, and 34 were evolved:

$$\left|\log\left|T_r - T_u + \log\left|\frac{\log\left(|L|^L\right)}{T_u + 1}\right|\right|\right| \qquad [31]$$

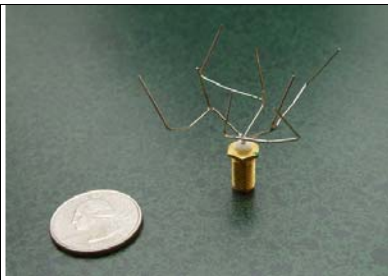
$$\left|\log\left|T_r + 1\right|\right| \qquad [34]$$

$$NLM\left(\log|L| - \left(\mathrm{abs}(L)^L\right)^2 T_u^3 \left(T_u + 1\right) T_r e^L - 2T_u e^L\right) \qquad [32]$$

$$NLM\left(\log|L| - 2T_u e^L \left(2K_u \left(\log\left|K_u e^L\right| - \log|L|\right) T_u + K_u e^L\right)\right) \qquad [33]$$

Antenna that satisfied NASA specs and that will be launched into space in 2004

Lohn et al. 2003



EVOLUTIONARY SYNTHESIS OF KINEMATIC MECHANISMS (LIPSON 2004)

PROMISING GP APPLICATION AREAS

• Problem areas involving many variables that are interrelated in highly non-linear ways
• Inter-relationship of variables is not well understood
• A good approximate solution is satisfactory
- **• design**
- **• control**
- **• classification and pattern recognition**
- **• data mining**
- **• system identification and forecasting**

• Discovery of the size and shape of the solution is a major part of the problem
• Areas where humans find it difficult to write programs
- **• parallel computers**
- **• cellular automata**
- **• multi-agent strategies / distributed AI**
- **• FPGAs**

• "black art" problems
- **• synthesis of topology and sizing of analog circuits**
- **• synthesis of topology and tuning of controllers**
- **• quantum computing circuits**
- **• synthesis of designs for antennas**

• Areas where you simply have no idea how to program a solution, but where the objective (fitness measure) is clear
• Problem areas where large computerized databases are accumulating and computerized techniques are needed to analyze the data

TURING'S THREE APPROACHES TO MACHINE INTELLIGENCE

• Turing made the connection between searches and the challenge of getting a computer to solve a problem without explicitly programming it in his 1948 essay "Intelligent Machines" (in *Mechanical Intelligence: Collected Works of A. M. Turing*, 1992, edited by D. C. Ince).

> **"Further research into intelligence of machinery will probably be very greatly concerned with 'searches' ... "**

TURING'S THREE APPROACHES TO MACHINE INTELLIGENCE — CONTINUED

1. LOGIC-BASED SEARCH

One approach that Turing identified is a search through the space of integers representing candidate computer programs.

2. CULTURAL SEARCH

Another approach is the "cultural search" which relies on knowledge and expertise acquired over a period of years from others (akin to present-day knowledge-based systems).

TURING'S THREE APPROACHES TO MACHINE INTELLIGENCE — CONTINUED

3. GENETICAL OR EVOLUTIONARY SEARCH

"There is the genetical or evolutionary search by which a combination of genes is looked for, the criterion being the survival value."

• from Turing's 1950 paper "Computing Machinery and Intelligence" …

"We cannot expect to find a good child-machine at the first attempt. One must experiment with teaching one such machine and see how well it learns. One can then try another and see if it is better or worse. There is an obvious connection between this process and evolution, by the identifications"

"Structure of the child machine = Hereditary material"

"Changes of the child machine = Mutations"

"Natural selection = Judgment of the experimenter"

17 AUTHORED BOOKS ON GP

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MAIN POINTS OF JAWS-1,2,3,4 BOOKS

Book	Main Points
1992	• Virtually all problems in artificial intelligence, machine learning, adaptive systems, and automated learning can be recast as a search for a computer program. • Genetic programming provides a way to successfully conduct the search for a computer program in the space of computer programs.
1994	• Scalability is essential for solving non-trivial problems in artificial intelligence, machine learning, adaptive systems, and automated learning. • Scalability can be achieved by reuse. • Genetic programming provides a way to automatically discover and reuse subprograms in the course of automatically creating computer programs to solve problems.
1999	• Genetic programming possesses the attributes that can reasonably be expected of a system for automatically creating computer programs.
2003	• Genetic programming now routinely delivers high-return human-competitive machine intelligence. • Genetic programming is an automated invention machine. • Genetic programming can automatically create a general solution to a problem in the form of a parameterized topology. • Genetic programming has delivered a progression of qualitatively more substantial results in synchrony with five approximately order-of-magnitude increases in the expenditure of computer time.

SOME RECENT CONFERENCE PROCEEDINGS

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WILLIAM LANGDON'S BIBLIOGRAPHY ON GENETIC PROGRAMMING

This bibliography is the most extensive in the field and contains over 3,034 papers (as of January 2003) by over 880 authors.

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www.isgec.org

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Visit
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for

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- **list of known completed PhD theses on GP**
- **list of students known to be working on PhD theses on GP**
- **information for instructors of university courses on genetic algorithms and genetic programming**