

Appendix 0: Alphabets

Observables

	SL	LabP	LL	ACP	CSP	DF	HL	DL
stable (ok, ok')	✓	✓	✓		✓	✓	✓	✓
waiting ($wait, wait'$)				✓	✓	✓		✓
control (l, l')		✓						
program variables (v, v')	✓	✓					✓	✓
question (q), answers (a')			✓					
trace (tr, tr')				✓	✓	✓		
refusal (ref, ref')				✓	✓	✓		
procedure variables (p, p')							✓	✓

- **SL**: Sequential programming language defined in Chapter 5.
- **LabP**: Labelled programs defined in Chapter 6.
- **LL**: Logic programming language defined in Section 7.6.
- **ACP**: Algebra of communicating processes defined in Section 8.1.
- **CSP**: Communicating Sequential Processes defined in Section 8.2.
- **DF**: Data flow processes defined in Section 8.3.
- **HL**: High order language defined in Chapter 9.
- **DL**: Declarative programming language defined in Section 9.4.

Appendix 1: Shared Variables

	Merge relation M	Atomic actions \mathcal{A}
stable (ok') (7.1)	$(0.ok \wedge 1.ok) \Rightarrow ok'$	
resource (r) (7.2)	$r' = 0.r + 1.r - r$	$r := r + e$
log (out) (7.2)	$(out' - out) \in$ $(0.out - out) (1.out - out)$	$out := out \hat{< e >$
clock ($clock$) (7.2)	$clock' = \max(0.clock, 1.clock)$	$clock := clock + 1$
input (in, c) (7.2)	$(0.c = 1.c)_{\perp}; c := 0.c$	$m, c := in_c, c + 1$
output (out, c) (7.2)	$\bigwedge_{c \leq i < 0.c} out_i := (0.out_i 1.out_i);$ $(0.c = 1.c)_{\perp}; c := 0.c$	$out_c, c := e, c + 1$
array (A) (7.4)	$A' = A \oplus (r_0 \triangleleft 0.A) \oplus (s_0 \triangleleft 1.A)$	$A[i] := e, x := f(A[j])$
answers (a') (7.6)	$a' = 0.a \hat{< 1.a}$ $a' \in (0.a 1.a)$	$a := a \hat{< c >$
waiting ($wait'$) (8.1 and 8.2)	$wait' = 0.wait \vee 1.wait$	$wait := true$ $wait := false$
trace (tr') (8.1 and 8.2)	$(tr' - tr) \in (0.tr - tr) (1.tr - tr)$ $(tr' - tr) \in (0.tr - tr) (1.tr - tr)$ $(tr' - tr) \downarrow \mathcal{A}P = (0.tr - tr) \wedge$ $(tr' - tr) \downarrow \mathcal{A}Q = (1.tr - tr)$	$tr := tr \hat{< c >$
refusal (ref') (8.1 and 8.2)	$ref' = 0.ref \cap 1.ref$ $ref' = 0.ref \cup 1.ref$	$true \vdash (ref' \cap X = \{\})$
program (X') (9.4)	$X' \sqsupseteq (0.X^* 1.X)$	$X' \sqsupseteq P$

Appendix 2: Primitives

	Abort	Skip	Stop	Miracle
SL				
LabP	true	$\Pi_{\{v\}} = \mathbf{true} \vdash (v' = v)$		$\neg ok$
LL				
ACP				
CSP	$\mathbf{R}(\mathbf{true})$	$\mathbf{R}(\exists ref' \bullet \Pi_{\{tr, ref, wait\}})$	$\mathbf{R}(\mathbf{true} \vdash wait' \wedge tr' = tr)$	$\mathbf{R}(\neg ok)$
DF				
DL	$\mathbf{W}(\mathbf{true})$	$\mathbf{W}(\Pi_{\{v\}})$	$wait := true$	$\mathbf{W}(\neg ok)$
HL	true	$\Pi_{\{p\}} = \mathbf{true} \vdash (p' \supseteq p)$		$\neg ok$

where \mathbf{R} and \mathbf{W} are defined by

$$\mathbf{R}(X(tr, tr')) =_{df} (tr \leq tr') \wedge (\Pi_{\{tr, ref, wait\}} \triangleleft wait \triangleright (\bigvee_s X(s, s \hat{\ } (tr' - tr))))$$

$$\mathbf{W}(X) =_{df} (STOP \triangleleft wait \triangleright X)$$

Appendix 3: Healthiness Conditions

Sequential programming language (Section 3.2 and Example 4.1.21)

H1 $P = (\neg ok \vee P)$

H2 $[P[false/ok'] \Rightarrow P[true/ok']]$

H3 $P = P; \Pi$

H4 $P; true = true \quad \square$

Reactive processes (Section 8.0)

R1 $P = P \wedge (tr \leq tr')$

R2 $P(tr, tr') = P(\langle \rangle, tr' - tr)$

R3 $P = \Pi_{\{tr, ref, wait\}} \triangleleft wait \triangleright P \quad \square$

ACP (Section 8.1)

R1-R3

ACP1 $P \wedge (tr' = tr) \Rightarrow wait' \quad \square$

CSP (Section 8.2)

R1-R3

$$\text{CSP1 } P = \neg ok \wedge (tr \leq tr') \vee P$$

$$\text{CSP2 } P = P; ((ok \Rightarrow ok') \wedge (tr' = tr) \wedge \dots \wedge (ref' = ref))$$

$$\text{CSP3 } P = \text{SKIP}; P$$

$$\text{CSP4 } P = P; \text{SKIP}$$

$$\text{CSP5 } P = P ||| \text{SKIP}$$

Data flow processes (Section 8.3)

R1-R3

CSP1-CSP5

$$\text{DF1 } P = IN \gg P \gg OUT \quad \square$$

High order language (Section 9.1)

$$\text{P1 } \Pi_{\{p\}}; P = P$$

$$\text{P2 } P; \Pi_{\{p\}} = P \quad \square$$

Definedness function (Section 9.3)

$$\text{D1 } \mathcal{D}e[\text{false}/\mathcal{D}x] \Rightarrow (\mathcal{D}e)[\text{true}/\mathcal{D}x]$$

$$\text{D2 } (\mathcal{D}e)[\text{false}/\mathcal{D}x] \Rightarrow \forall x, \mathcal{D}x \bullet \mathcal{D}(e)$$

$$\text{D3 } \mathcal{D}(\mathcal{D}e) \quad \square$$

Declarative language (Section 9.4)

$$\text{W1 } P = \Pi \triangleleft \text{wait} \triangleright P$$

$$\text{W2 } P = P \vee (P \wedge \text{wait}' \wedge v' \neq v); \text{true} \quad \square$$

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