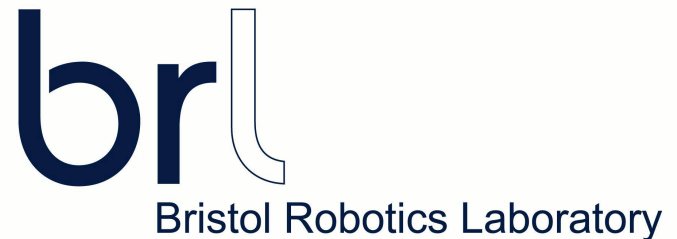


# Practical Techniques for Verification and Validation of Robots

Kerstin Eder  
with a demo by Dejanira Araiza Illan

University of Bristol and  
Bristol Robotics Laboratory



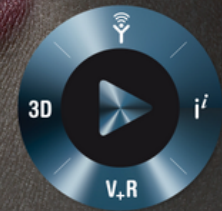
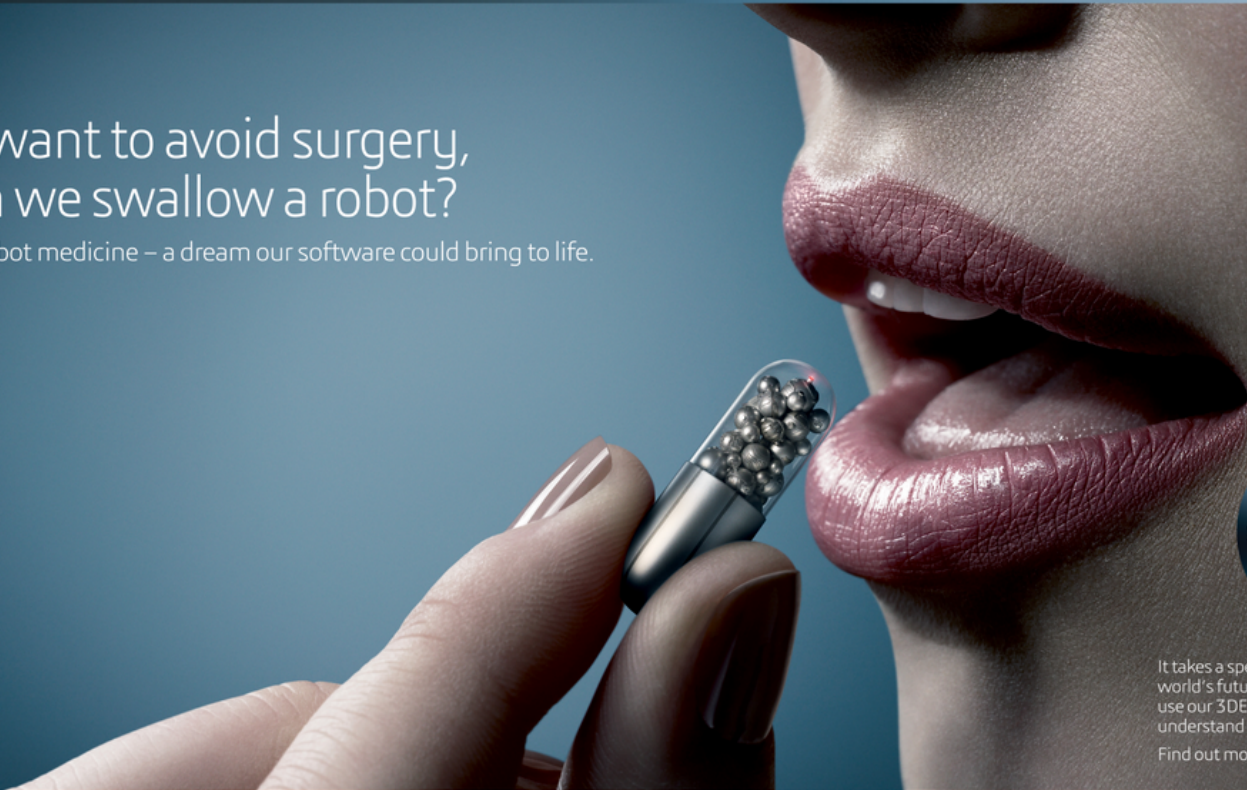
# Would you swallow a robot?

3DEXPERIENCE



want to avoid surgery,  
can we swallow a robot?

Nanobot medicine – a dream our software could bring to life.



It takes a special kind of compass to explore the world's future possibilities. Innovative companies use our 3DExperience software platform to understand the present and navigate the future.

Find out more: [3DS.COM/LIFE-SCIENCES](https://3ds.com/life-sciences)



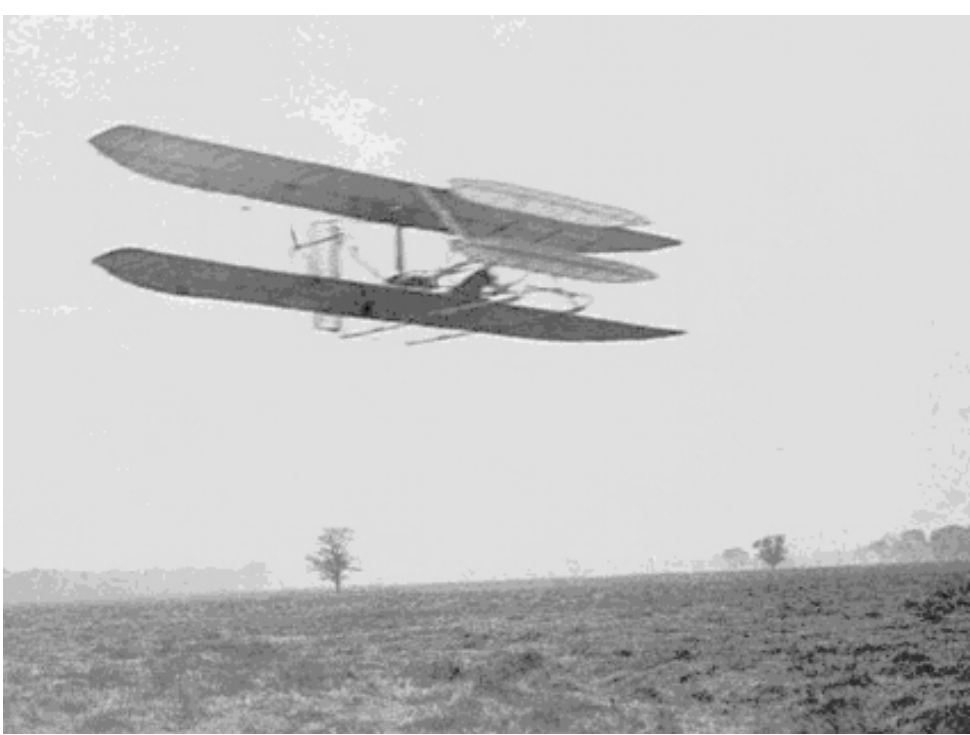
IF WE ask the right questions  
we can change the world.

# The Safety Challenge

---

- Autonomous Systems
- Engineering Challenge
  - Advances in control science
  - Focus on “making things work”





Pictures from [www.wikipedia.org](http://www.wikipedia.org)



# The Safety Challenge

- Autonomous Systems
- Engineering Challenge
  - Advances in control science
  - Focus on “making things work”
- Fundamental concern:
  - Can such systems be trusted?





# Dependability

---

- A system is dependable (or trustworthy) only if it can be **shown** to be safe and useful.
  - Safety is the property of avoiding harmful conditions.
  - Liveness requires that the system achieves its goals a.k.a. usefulness.
- **Demonstrable** safety and liveness are required.



# Safety Assurance

**Assurance** is the essential concept:

- A system may never cause harm throughout its entire operating life,
- but if we cannot be assured of that before we start to use it, then the system can not be trusted.

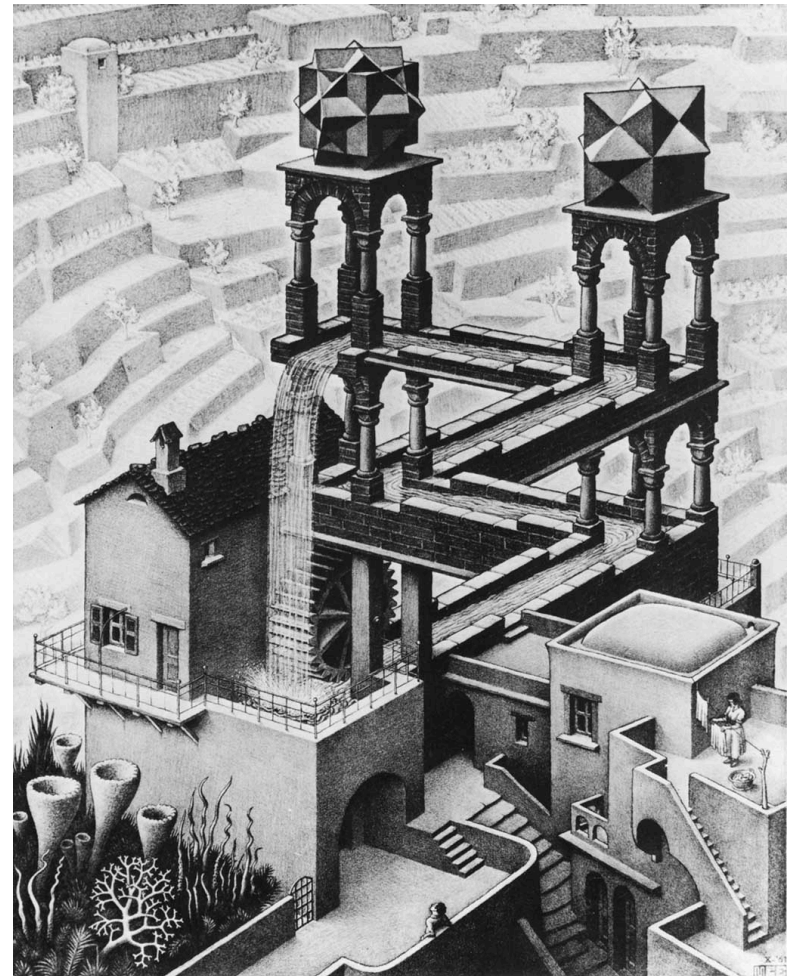


# Designing Dependable Systems

- Create flawless designs.

AND

- Design the system in such a way that the flawlessness can be demonstrated.



"Waterfall" by M.C Escher.

# EPSRC “Principles of Robotics”

---

*“Robots are products.  
They should be **designed** using  
**processes which assure their  
safety and security.**”*

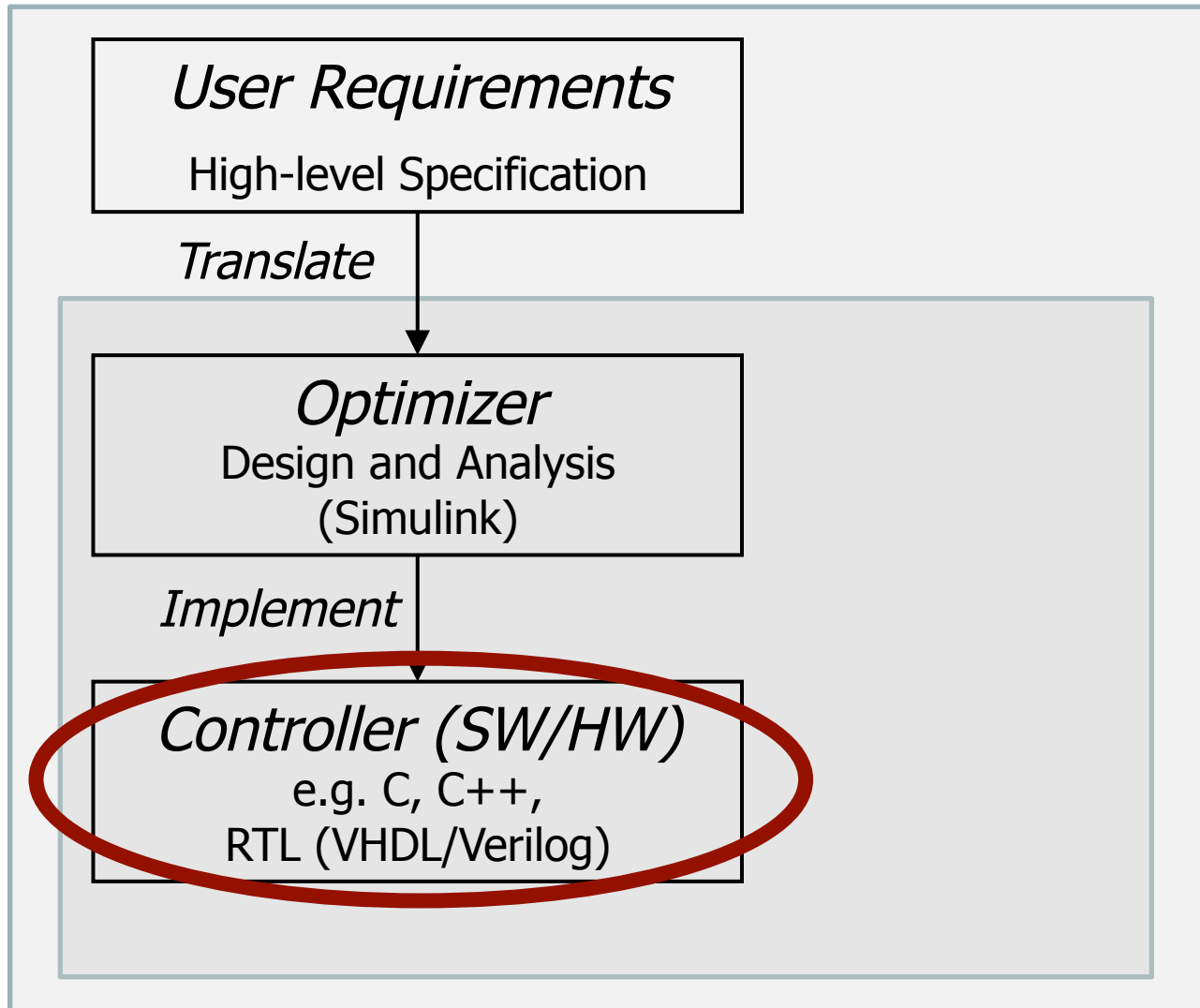
<http://www.epsrc.ac.uk/ourportfolio/themes/engineering/activities/Pages/principlesofrobotics.aspx>



# Verification and Validation for Safety in Robots

To develop techniques and methodologies that can be used to design autonomous intelligent systems that are demonstrably trustworthy.

# Correctness from specification to implementation



# What can be done at the code level?

P. Trojanek and K. Eder.

***Verification and testing of mobile robot navigation algorithms: A case study in SPARK.***

IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS).  
pp. 1489-1494. Sep 2014.

<http://dx.doi.org/10.1109/IROS.2014.6942753>



# What can go wrong in robot navigation software?

## Generic bugs:

- Array and vector out-of-bounds accesses
- Null pointer dereferencing
- Accesses to uninitialized data



## Domain-specific bugs:

- Integer and floating-point arithmetic errors
- Mathematic functions domain errors
- Dynamic memory allocation errors
- Concurrency bugs
  - blocking inter-thread communication (non real-time)



# State of the art verification approaches

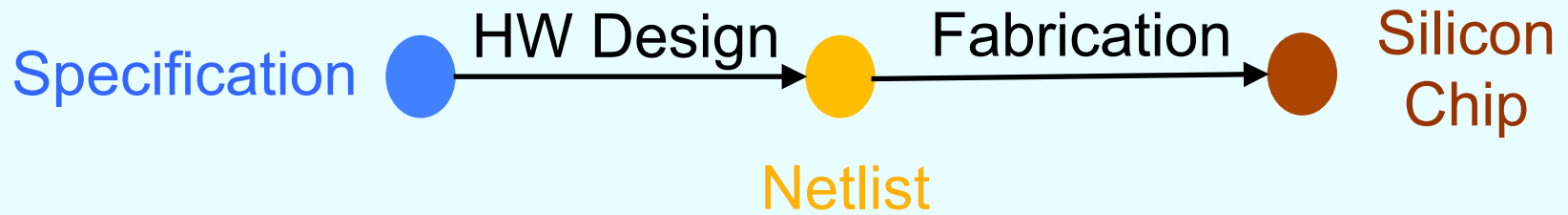
---

- Model checking
  - infeasible for real (off-the-shelf) code
- Static analysis of C++
  - not possible
- Static analysis of C
  - requires verbose and difficult to maintain annotations



# HW Design Reconvergence Model

---





# Why design a custom integrated circuit?

## Mask costs versus line width

Process ( $\mu\text{m}$ )	Vdd	Metal	Gates/sq mm	Mask set cost (\$)
0.065	1.0	9	400k	3,000,000
0.09	1.0	9	200k	1,500,000
0.13	1.2	7	100k	750,000
0.18	1.8	5	40k	250,000
0.25	2.5	5	24k	150,000
0.35	3.3	3	12k	40,000
0.5	3.3	3	5k	20,000
0.6	5.0	2	4k	18,000

Source: 'Asic Design in the Silicon Sandbox: A Complete Guide to Building Mixed-Signal Integrated Circuits'. (The McGraw-Hill Companies).

→ Furthermore, there are other energy-saving techniques you can use that are unique to custom ICs.

For some applications, small size and weight are crucial. Just open up an MP3 player, mobile phone, digital camera or laptop computer for examples of tight and light design. When a set of standard parts is too large or heavy, a custom chip is required.

A designer with access to the full flexibility of a custom chip can create numerous special functions that are difficult to find elsewhere.

For example, special purpose arithmetic units, multi-port memories, and a variety of non-volatile storage circuits can be developed. One can even create magnetic sensors and light sensors ranging from a single sensor to line sensors and two-dimensional video camera chips.

Some companies use custom ICs to better protect their intellectual property. A custom integrated circuit is much more difficult to reverse engineer than a board level design.

### The benefits: reliability

Higher integration levels bring greater system reliability.

If your board, with dozens of parts and hundreds of solder connections, can be replaced by one or a few parts with fewer board-level interconnects then the system becomes more reliable. Likewise, higher integration leads to lower manufacturing costs. If the custom IC uses less power, you may be able to use a cheaper power supply. Fewer boards also mean fewer connectors and smaller, less-expensive cabinets.

One company built a product that had two discrete transistors, a photo-

cell, and a few resistors and capacitors. The circuit board was larger than they needed, they had a measurable field failure rate, and it cost about \$1.00.

The company designed a custom IC with several thousand transistors to implement the same function. It had no measurable field failure rate, and the unit cost was about \$0.50. For the millions of units sold, the payback on this custom chip investment was rapid.

### The downside: cost

Custom chips have higher tooling

costs, so if it is important to minimize the cost of prototypes by using standard parts. You may be able to gather a few PCBs and a handful of parts, hand-solder them together, and demonstrate a prototype for about \$2,000. The tooling costs of a custom IC start at about \$18,000 for a set of masks for a 0.6 $\mu\text{m}$  process and go up to about \$3m for a 65nm process.

Products that have high volumes and require huge amounts of processing and memory will need the finest line width processes to get the lowest cost in production. However, for most other products, the manufacturing volumes never make sense for the \$3m tooling cost. Fortunately, the tooling for coarser line widths is much more affordable, yet still larger than that of a PCB.

### The downside: time

Custom chips also have longer turnaround times.

If you have a good relationship with your board supplier, a board can be manufactured in a couple of days. Add some shipping and assembly time, and you will still get a new prototype built using standard parts in less than a week.

If you go custom IC, it will be weeks, if not months, before the first chips arrive at your door. And although expediting is often available, the fees are steep and shave only a few days off a lengthy →p30 process.

**If you go custom IC, it will be weeks, if not months, before the first chips arrive at your door. And although expediting is often available, the fees are steep and shave only a few days off a lengthy process**



## A CLASS ACT IS TOUGH TO FOLLOW

New from Schurter's metal line range; the MSM top grade stainless steel switch looks good, performs even better under pressure

- Switching up to 3A 250V AC
- Various sizes - mounting diameter 16, 19, 22 and 30mm
- Highly robust IP67 seal protection
- Resistant to shock IK07 rating
- Low profile to panel and smooth travel
- Various colour options for point or ring illumination - red, green, yellow or blue

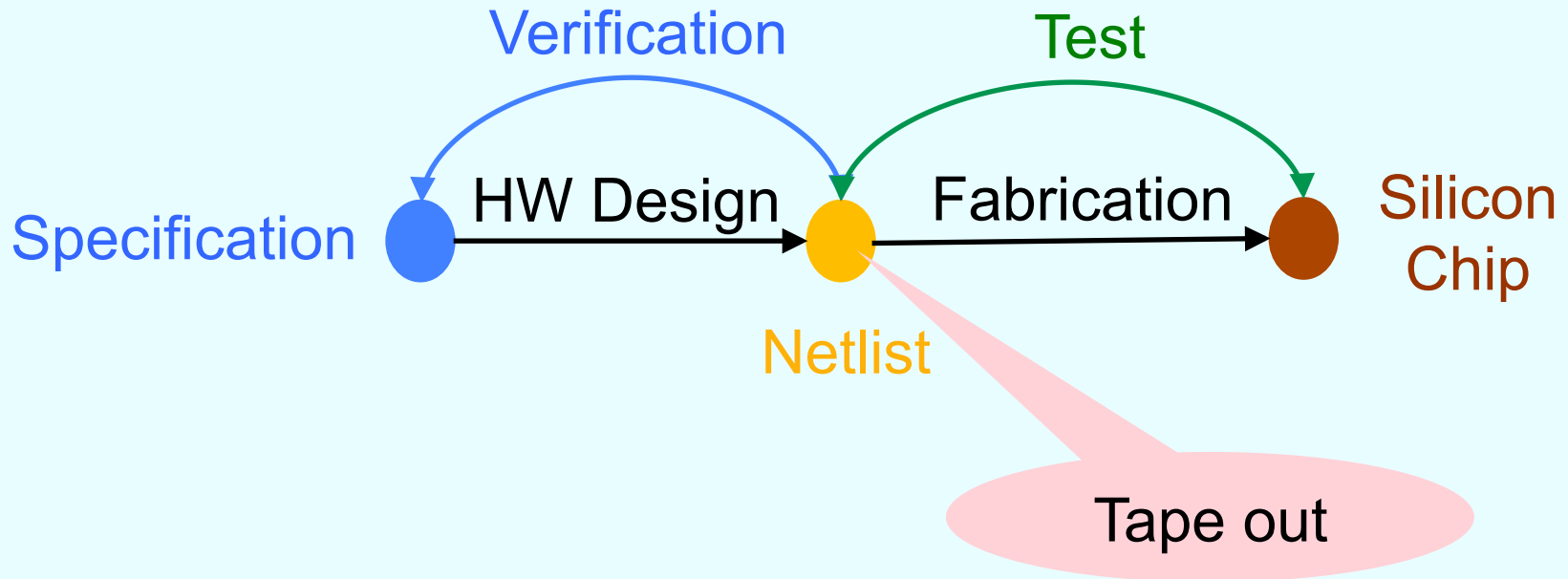
View Schurter's huge range of switches at [www.schurter.com](http://www.schurter.com) or call 01243 810810

**SCHURTER**  
ELECTRONIC COMPONENTS

Manufacturer of high quality components since 1933

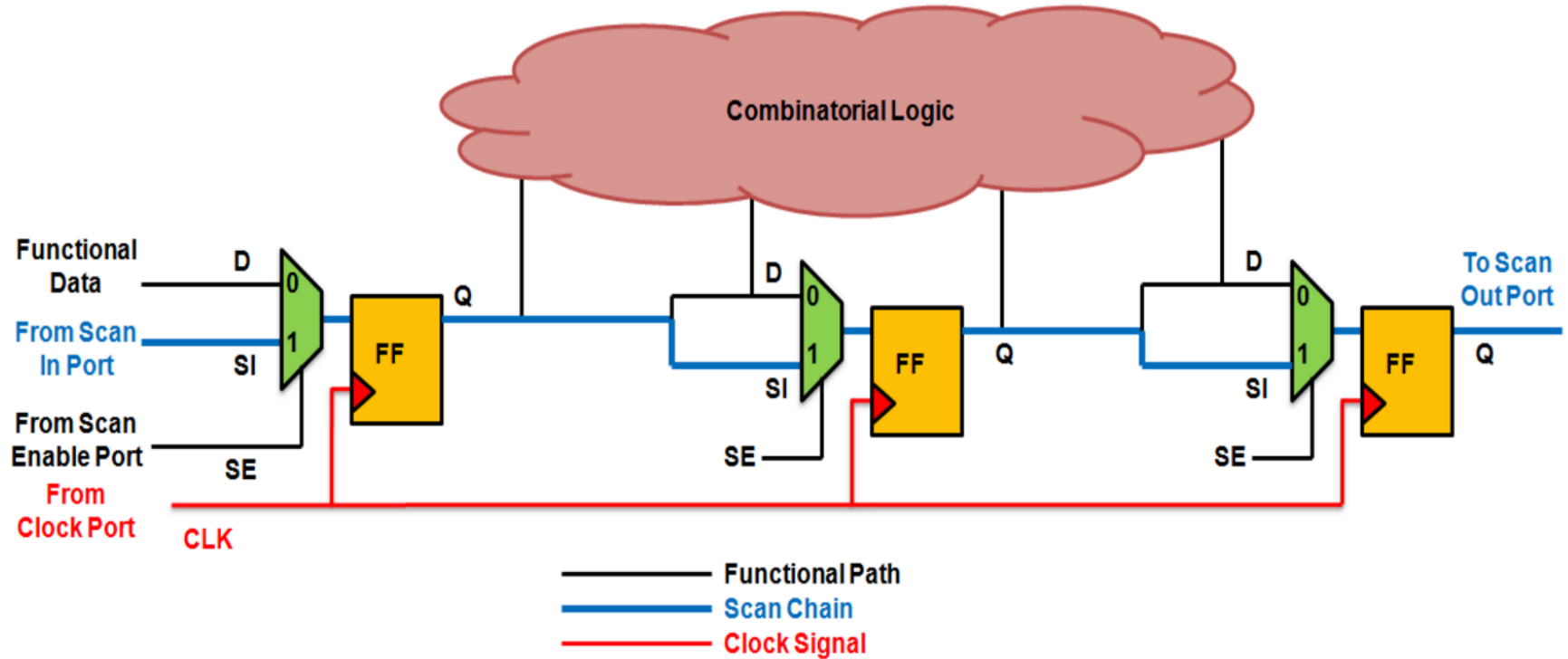


# HW Design Reconvergence Model



- ***Design Verification** is the process used to gain confidence in the correctness of a design w.r.t. the requirements and specification.*
- **Test:** Manufacturing Test vs Functional Test

# Design-for-Test(ability)



# Design-for-Verification Approach

---

- **SPARK**, a verifiable subset of Ada
  - software reliability a primary goal
  - no memory allocation, pointers, concurrency
  - side-effect free functions
  - SPARK specification and tools freely available for academic use
- Required code modifications:
  - Pre- and post-conditions, loop (in)variants
  - Numeric subtypes (e.g. positive)
  - Formal data containers

# Navigation in SPARK

- Three open-source implementations of navigation algorithms translated from C/C++ (2.7 kSLOC) to SPARK (3.5 kSLOC)

- Vector Field Histogram
- Nearness Diagram
- Smooth Nearness-Diagram

	Driver		
	C++	C/C++	Ada
VFH+	807	782	918
ND	828	1037	1426
SND	403	941	1183
<b>Total</b>	2038	2760	3527

- Explicit annotations are less than 5% of the code
- SPARK code is on average 30% longer than C/C++



# Verification Conditions

	Explicit annotations					Implicit run-time checks						Total
	Pre-conditions*	Post-conditions	Loop invariants*	Loop variants	Assertions	Divisions	Integer overflows	Floating-point overflows	Subtype ranges	Array indices	Record discriminants	
VFH+	46 (3)	5	18 (9)	0	23	36	36	120	100	102	262	<b>748</b>
ND	83 (18)	10	8 (4)	2	3	54	23	254	53	50	0	<b>540</b>
SND	104 (9)	9	14 (7)	2	30	29	1	140	22	0	24	<b>375</b>

\* Separate verification conditions are generated for each call to subprogram with precondition, and similarly for initialization and preservation of each loop invariant; the numbers of explicit annotations are given in brackets.



# Formal Verification Results

	Alt-Ergo 0.96	Z3 4.3.1	Alt-Ergo & Z3 combined	<b>Total</b>
VFH+	633 11 min	699 37 min	701 48 min	<b>748</b>
ND	462 17 min	482 21 min	483 41 min	<b>540</b>
SND	350 29 min	366 6 min	366 36 min	<b>375</b>

Number of discharged verification conditions and the running time of static analysis

# Results

---

- Several bugs discovered by run-time checks injected by the Ada compiler
  - Fixed code proved to be run-time safe
    - except floating-point over- and underflows
    - These require the use of complementary techniques, e.g. abstract interpretation.
- Up to 97% of the verification conditions discharged automatically by SMT solvers in less than 10 minutes
- Performance of the SPARK and C/C++ code similar

**Moral: If you want to make runtime errors an issue of the past, then select your tools (programming language and dev env) wisely!**

# Moral

**If you want to make runtime errors an issue of the past, then you must select your tools (programming language and dev env) wisely!**



riveras / **spark-navigation**

Watch 2 Star 1 Fork 0

Robot navigation algorithms implemented in SPARK

156 commits 1 branch 0 releases 1 contributor

Branch: master spark-navigation / +

adjust SND for compatibility with GNAT GPL 2014 and SPARK GPL 2014

Yannick Moy authored on May 26, 2014 latest commit 15f521fdab  
ptroja committed on May 27, 2014

common	adjust SND for compatibility with GNAT GPL 2014 and SPARK GPL 2014	a year ago
nd	unused Ada spec file removed	a year ago
snd	adjust SND for compatibility with GNAT GPL 2014 and SPARK GPL 2014	a year ago
vfh	avoid unevaluated expressions in contracts	a year ago
wavefront	unused code separated	a year ago
.gitignore	keep only a single .gitignore file	2 years ago
README.md	readme corrected	2 years ago
TODO.md	bug reported to AdaCore	2 years ago
performance.ods	performance data updated	2 years ago
statistics.sh	statistics: discriminants and count_type overflows	2 years ago

Code

Issues 0

Pull requests 0

Wiki

Pulse

Graphs

HTTPS clone URL  
https://github.com/i

You can clone with HTTPS, SSH, or Subversion.

Clone in Desktop

Download ZIP

<http://github.com/riveras/spark-navigation>

P. Trojanek and K. Eder.

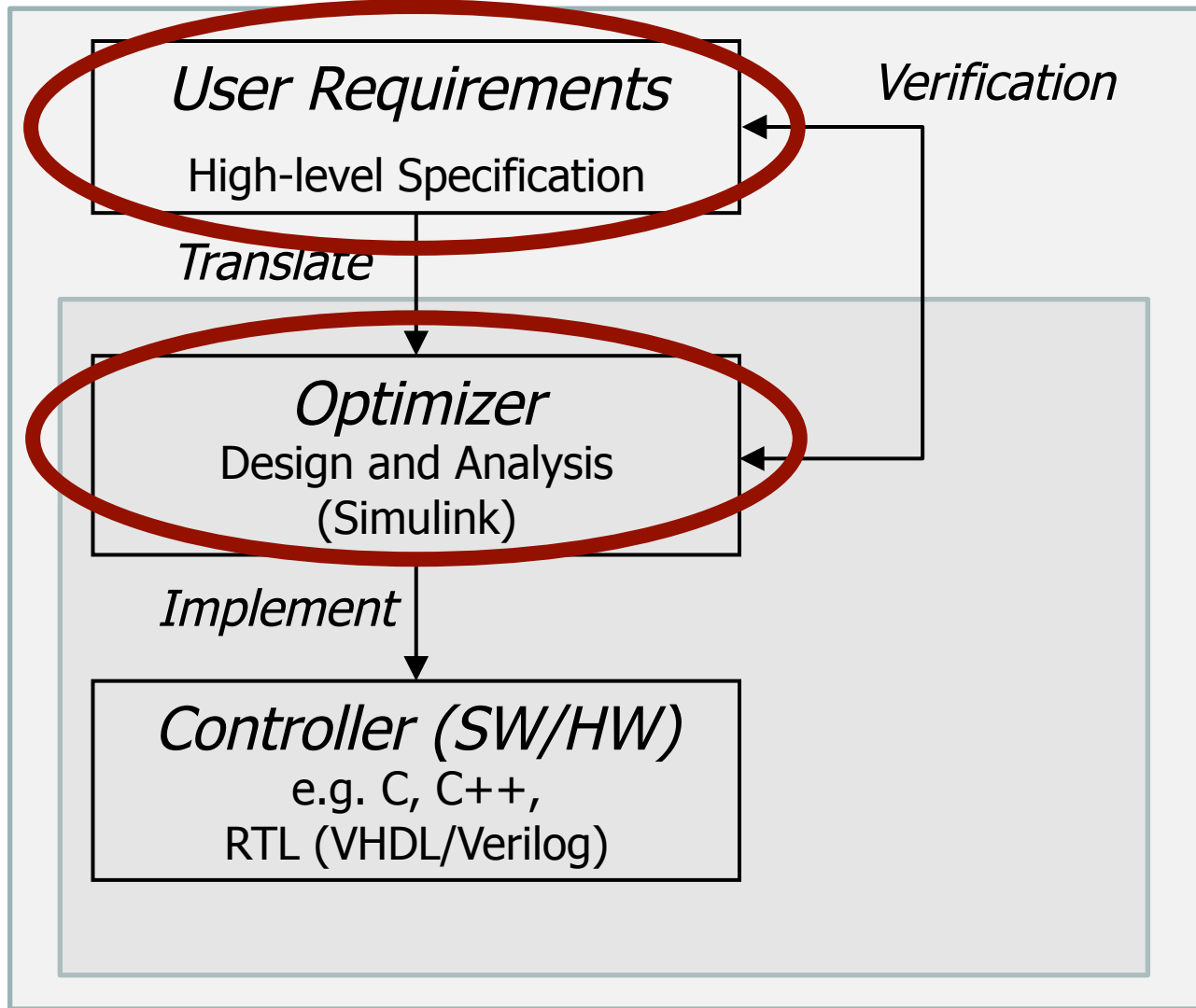
***Verification and testing of mobile robot navigation algorithms:  
A case study in SPARK.***

IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS).  
pp. 1489-1494. Sep 2014.

<http://dx.doi.org/10.1109/IROS.2014.6942753>



# Correctness from Specification to Implementation



# What can be done at the design level?

D. Araiza Illan, K. Eder, A. Richards.

***Formal Verification of Control Systems' Properties with Theorem Proving.***

International Conference on Control (CONTROL), pp. 244 – 249. IEEE, Jul 2014.

<http://dx.doi.org/10.1109/CONTROL.2014.6915147>

D. Araiza Illan, K. Eder, A. Richards.

***Verification of Control Systems Implemented in Simulink with Assertion Checks and Theorem Proving: A Case Study.***

European Control Conference (ECC), pp. tbc. Jul 2015.

<http://arxiv.org/abs/1505.05699>

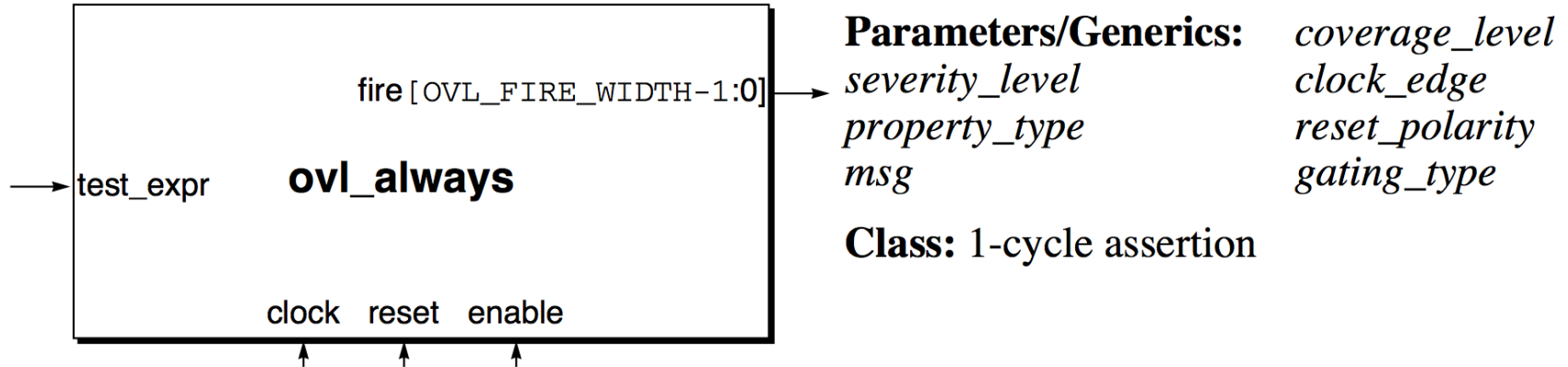
# What is an assertion?

- An **assertion** is a statement that a particular property is required to be true.
  - A property is a Boolean-valued expression
- Assertions can be checked either during simulation or using a formal property checker.
- Assertions have been used in SW design for a long time.
  - `assert()` function is part of C `#include <assert.h>`
  - Used to detect **NULL** pointers, out-of-range data, ensure loop invariants, etc.
- Revolution through **Foster & Bening's OVL for Verilog**.
  - Clever way of encoding re-usable assertion library in Verilog. 😊
  - > 30 checker types (assertion templates)
  - <http://accellera.org/activities/working-groups/ovl>



# ovl\_always

Checks that the value of an expression is TRUE.

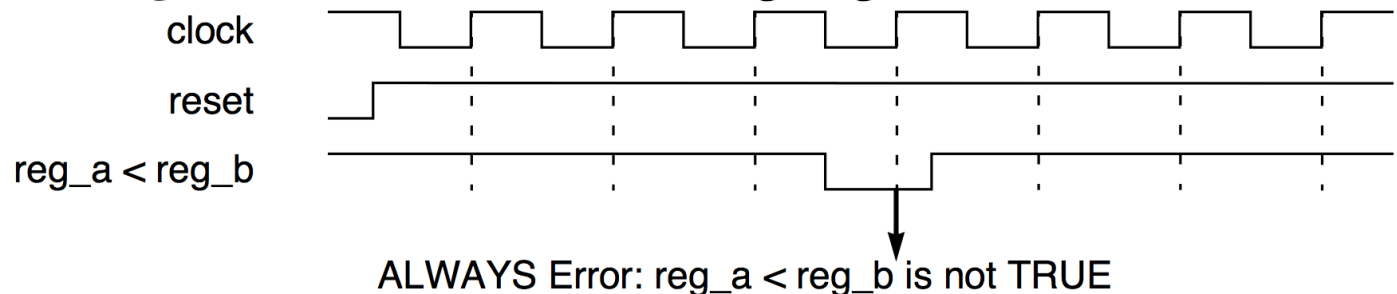


## Syntax

### **ovl\_always**

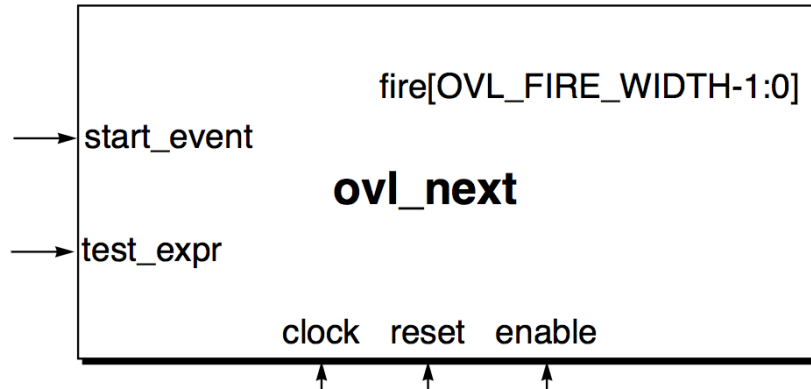
```
[#(severity_level, property_type, msg, coverage_level, clock_edge,  
    reset_polarity, gating_type)]  
instance_name (clock, reset, enable, test_expr, fire);
```

Checks that  $(reg\_a < reg\_b)$  is TRUE at each rising edge of *clock*.



# ovl\_next

Checks that the value of an expression is TRUE a specified number of cycles after a start event.



## Parameters/Generics:

*severity\_level*

*num\_cks*

*check\_overlapping*

*check\_missing\_start*

*property\_type*

*msg*

*coverage\_level*

*clock\_edge*

*reset\_polarity*

*gating\_type*

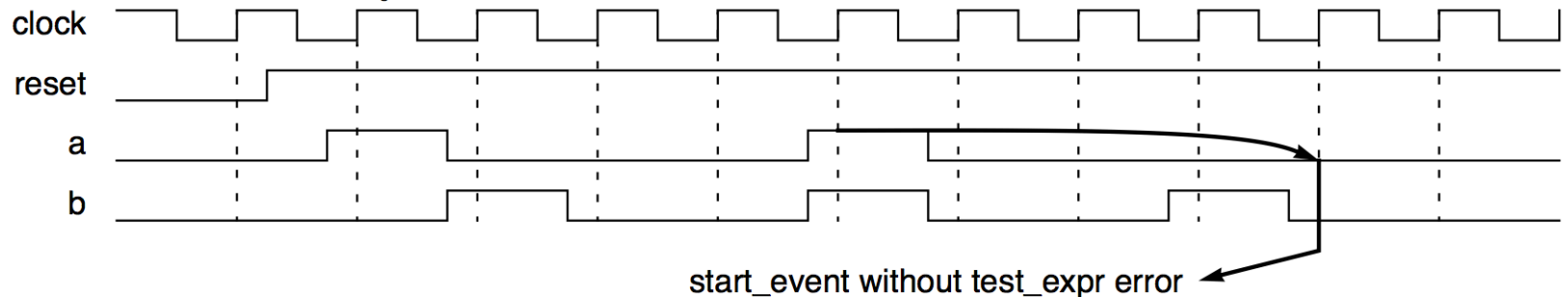
**Class:** *n*-cycle assertion

## Syntax

### ovl\_next

```
[#(severity_level, num_cks, check_overlapping, check_missing_start,  
   property_type, msg, coverage_level, clock_edge, reset_polarity,  
   gating_type)]  
instance_name (clock, reset, enable, start_event, test_expr, fire);
```

Checks that *b* is TRUE 4 cycles after *a* is TRUE.



TYPE	NAME	PARAMETERS	PORTS	DESCRIPTION
Single-Cycle	<b>assert always</b>	#(severity_level, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must always hold
Two Cycles	<b>assert always_on_edge</b>	#(severity_level, edge_type, property_type, msg, coverage_level)	(clk, reset_n, sampling_event, test_expr)	test_expr is true immediately following the specified edge (edge_type: 0=no-edge, 1=pos, 2=neg, 3=any)
n-Cycles	<b>assert change</b>	#(severity_level, width, num_cks, action_on_new_start, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr)	test_expr must change within num_cks of start_event (action_on_new_start: 0=ignore, 1=restart, 2=error)
n-Cycles	<b>assert cycle_sequence</b>	#(severity_level, num_cks, necessary_condition, property_type, msg, coverage_level)	(clk, reset_n, event_sequence)	If the initial sequence holds, the final sequence must also hold (necessary_condition: 0=trigger-on-most, 1=trigger-on-first, 2=trigger-on-first-uninlined)
Two Cycles	<b>assert decrement</b>	#(severity_level, width, value, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	If test_expr changes, it must decrement by the value parameter (modulo 2*width)
Two Cycles	<b>assert delta</b>	#(severity_level, width, min, max, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	If test_expr changes, the delta must be >=min and <=max
Single Cycle	<b>assert even_parity</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must have an even parity, i.e. an even number of bits asserted
Two Cycles	<b>assert fifo_index</b>	#(severity_level, depth, push_width, pop_width, property_type, msg, coverage_level, simultaneous_push_pop)	(clk, reset_n, push, pop)	FIFO pointers should never overflow or underflow
n-Cycles	<b>assert frame</b>	#(severity_level, min_cks, max_cks, action_on_new_start, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr)	test_expr must not hold before min_cks cycles, but must hold at least once by max_cks cycles (action_on_new_start: 0=ignore, 1=restart, 2=error)
n-Cycles	<b>assert handshake</b>	#(severity_level, min_ack_cycle, max_ack_cycle, req_drop, deassert_count, max_ack_length, property_type, msg, coverage_level)	(clk, reset_n, req, ack)	req and ack must follow the specified handshaking protocol
Single-Cycle	<b>assert implication</b>	#(severity_level, property_type, msg, coverage_level)	(clk, reset_n, antecedent_expr, consequent_expr)	If antecedent_expr holds then consequent_expr must hold in the same cycle
Two Cycles	<b>assert increment</b>	#(severity_level, width, value, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	If test_expr changes, it must increment by the value parameter (modulo 2*width)
Single-Cycle	<b>assert never</b>	#(severity_level, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must never hold
Single-Cycle	<b>assert never_unknown</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, qualifier, test_expr)	test_expr must never be an unknown value, just boolean 0 or 1
Combinatorial	<b>assert never_unknown_async</b>	#(severity_level, width, property_type, msg, coverage_level)	(reset_n, test_expr)	test_expr must never go to an unknown value asynchronously, it must remain boolean 0 or 1
n-Cycles	<b>assert next</b>	#(severity_level, num_cks, check_overlapping, check_missing_start, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr)	test_expr must hold num_cks cycles after start_event holds
Two Cycles	<b>assert no_overflow</b>	#(severity_level, width, min, max, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	If test_expr is at max, in the next cycle test_expr must be >min and <=max
Two Cycles	<b>assert no_transition</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr, start_state, next_state)	If test_expr=start_state, in the next cycle test_expr must not change to next_state
Two Cycles	<b>assert no_underflow</b>	#(severity_level, width, min, max, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	If test_expr is at min, in the next cycle test_expr must be >=min and <max
Single-Cycle	<b>assert odd_parity</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must have an odd parity, i.e. an odd number of bits asserted
Single-Cycle	<b>assert one_cold</b>	#(severity_level, width, inactive, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must be one-cold i.e. exactly one bit set low (inactive: 0=also-all-zero, 1=also-all-ones, 2=pure-one-cold)
Single-Cycle	<b>assert one_hot</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must be one-hot i.e. exactly one bit set high
Combinatorial	<b>assert proposition</b>	#(severity_level, property_type, msg, coverage_level)	(reset_n, test_expr)	test_expr must hold asynchronously (not just at a clock edge)
Two Cycles	<b>assert quiescent_state</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, state_expr, check_value, sample_event)	state_expr must equal check_value on a rising edge of sample_event (also checked on rising edge of 'OVL_END_OF_SIMULATION')
Single-Cycle	<b>assert range</b>	#(severity_level, width, min, max, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must be >=min and <=max
n-Cycles	<b>assert time</b>	#(severity_level, num_cks, action_on_new_start, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr)	test_expr must hold for num_cks cycles after start_event (action_on_new_start: 0=ignore, 1=restart, 2=error)
Two Cycles	<b>assert transition</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr, start_state, next_state)	If test_expr changes from start_state, then it can only change to next_state
n-Cycles	<b>assert unchange</b>	#(severity_level, width, num_cks, action_on_new_start, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr)	test_expr must not change within num_cks of start_event (action_on_new_start: 0=ignore, 1=restart, 2=error)
n-Cycles	<b>assert width</b>	#(severity_level, min_cks, max_cks, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must hold for between min_cks and max_cks cycles
Event-bound	<b>assert win_change</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr, end_event)	test_expr must change between start_event and end_event
Event-bound	<b>assert window</b>	#(severity_level, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr, end_event)	test_expr must hold after the start_event and up to (and including) the end_event
Event-bound	<b>assert win_unchange</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, start_event, test_expr, end_event)	test_expr must not change between start_event and end_event
Single-Cycle	<b>assert zero_one_hot</b>	#(severity_level, width, property_type, msg, coverage_level)	(clk, reset_n, test_expr)	test_expr must be one-hot or zero, i.e. at most one bit set high

**PARAMETERS****severity\_level**

```

+define+OVL_ASSERT_ON
`OVL_FATAL
`OVL_ERROR
`OVL_WARNING
`OVL_INFO

```

**property\_type**

```

`OVL_ASSERT
`OVL_ASSUME
`OVL_IGNORE

```

**msg** descriptive string**USING OVL**

```

+define+OVL_ASSERT_ON
+define+OVL_MAX_REPORT_ERROR=1
+define+OVL_INIT_MSG
+define+OVL_INIT_COUNT=<tbench>.ovl_init_count

+libext+.v+.vlib
-y <OVL_DIR>/std_ovl
+incdir+<OVL_DIR>/std_ovl

```

**DESIGN ASSERTIONS***Monitors internal signals & Outputs**Examples*

```

* One hot FSM
* Hit default case items
* FIFO / Stack
* Counters (overflow/increment)
* FSM transitions
* X checkers (assert_never_unknown)

```

**INPUT ASSUMPTIONS***Restricts environment**Examples*

```

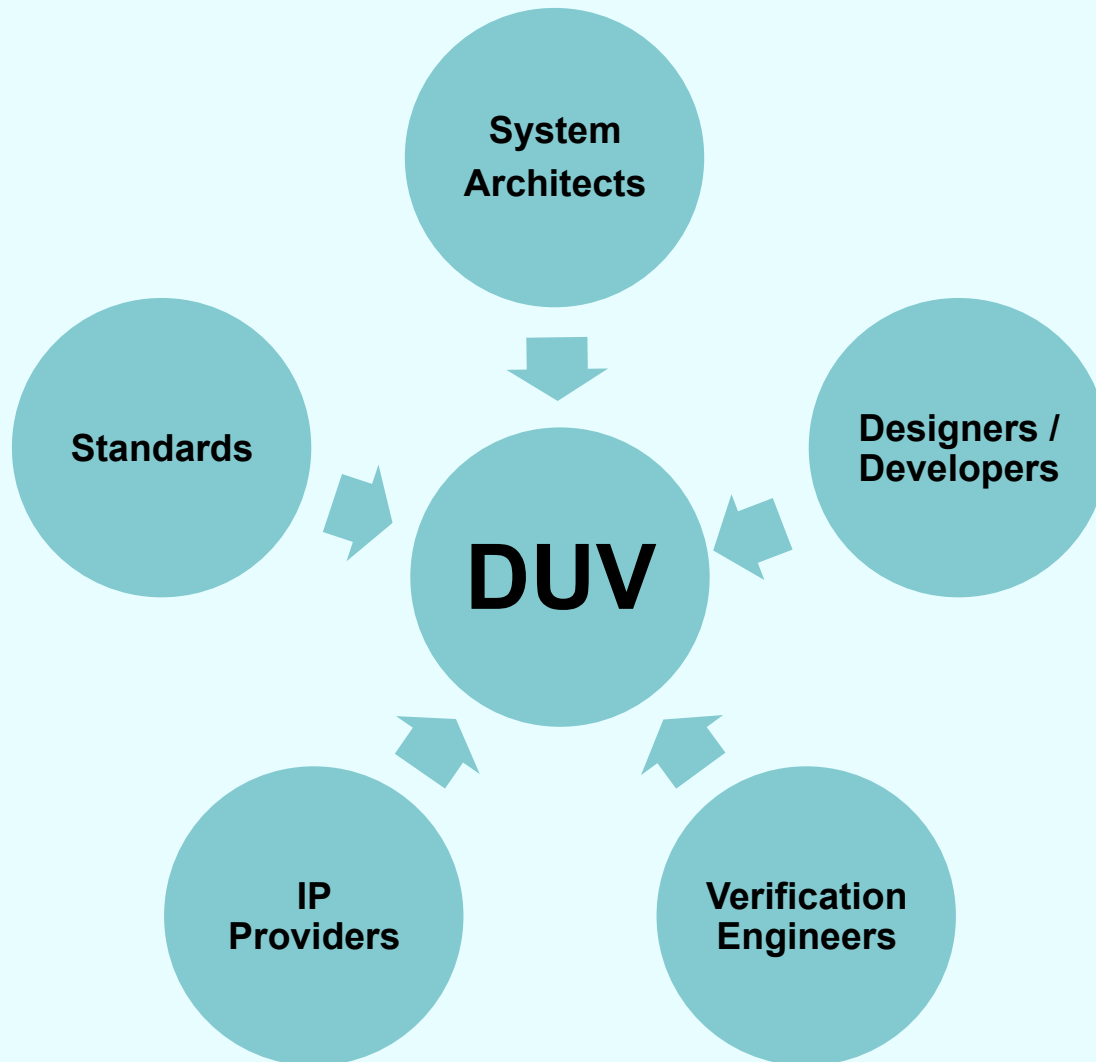
* One hot inputs
* Range limits e.g. cache sizes
* Stability e.g. cache sizes
* No back-to-back reqs
* Handshaking sequences
* Bus protocol

```



# Who writes the assertions?

---



# Implementation Assertions

---

- **Also called “design” assertions.**
- **Specified by the designer/developer.**
  - Encode designer’s assumptions.
    - Interface assertions
      - Catch different interpretations between different designers.
  - Formulate conditions of design misuse or design faults:
    - detect buffer over/under flow
    - signal read & write at the same time when only one is allowed
- Implementation assertions **can detect** discrepancies between design assumptions and implementation.

# Specification Assertions

---

- **Also called “intent” assertions**
  - Often high-level properties.
- **Specified by architects, verification engineers, IP providers, standards.**
  - Encode expectations of the design based on understanding of functional intent.
  - Provide a “functional error detection” mechanism.
  - Supplement error detection performed by self-checking testbenches.
    - Instead of using (implementing) a monitor and checker, in some cases writing a block-level assertion can be much simpler.

# Do assertions really work?

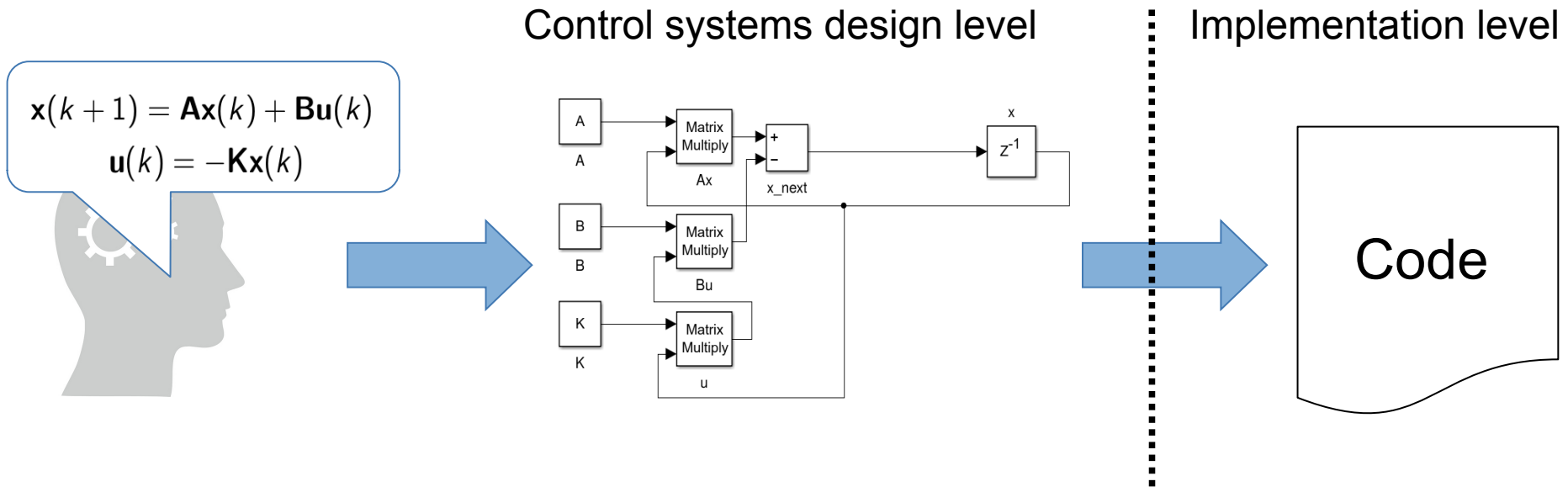
- **Assertions are able to detect a significant percentage of design failures:**

[Foster et al.: Assertion-Based Design. 2<sup>nd</sup> Edition, Kluwer, 2010.]

- **34%** of all bugs were found by assertions on DEC Alpha 21164 project [Kantrowitz and Noack 1996]
- **17%** of all bugs were found by assertions on Cyrix M3(p1) project [Krolnik 1998]
- **25%** of all bugs were found by assertions on DEC Alpha 21264 project - The DEC 21264 Microprocessor [Taylor et al. 1998]
- **25%** of all bugs were found by assertions on Cyrix M3(p2) project [Krolnik 1999]
- **85%** of all bugs were found using OVL assertions on HP [Foster and Coelho 2001]

**Assertions should be an integral part of a verification methodology.**

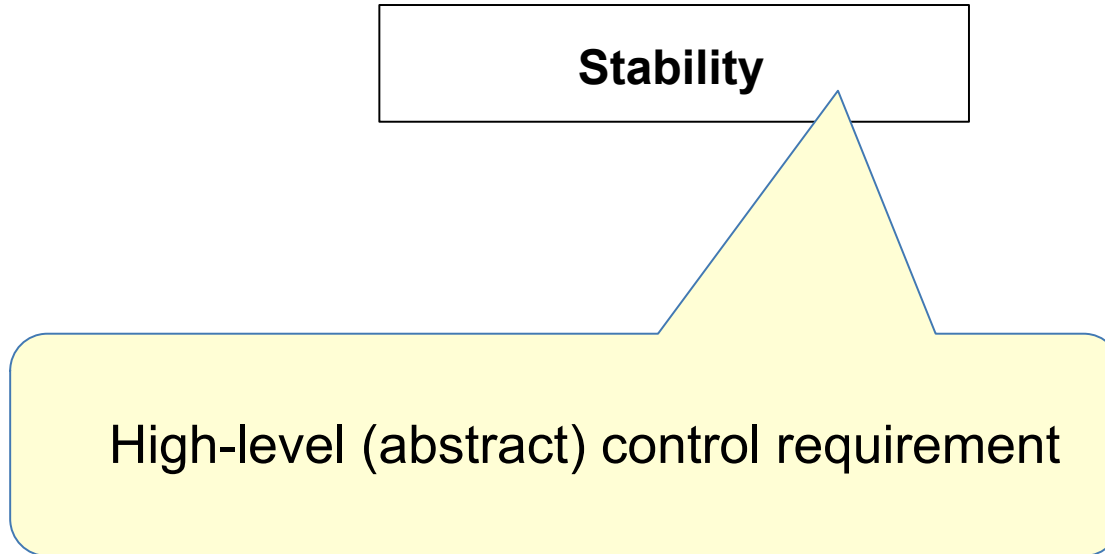
# Simulink Diagrams in Control Systems



- Simulating the control systems
- Analysis techniques from control systems theory (e.g., stability)
- Serve as requirements/specification
- For (automatic) code generation

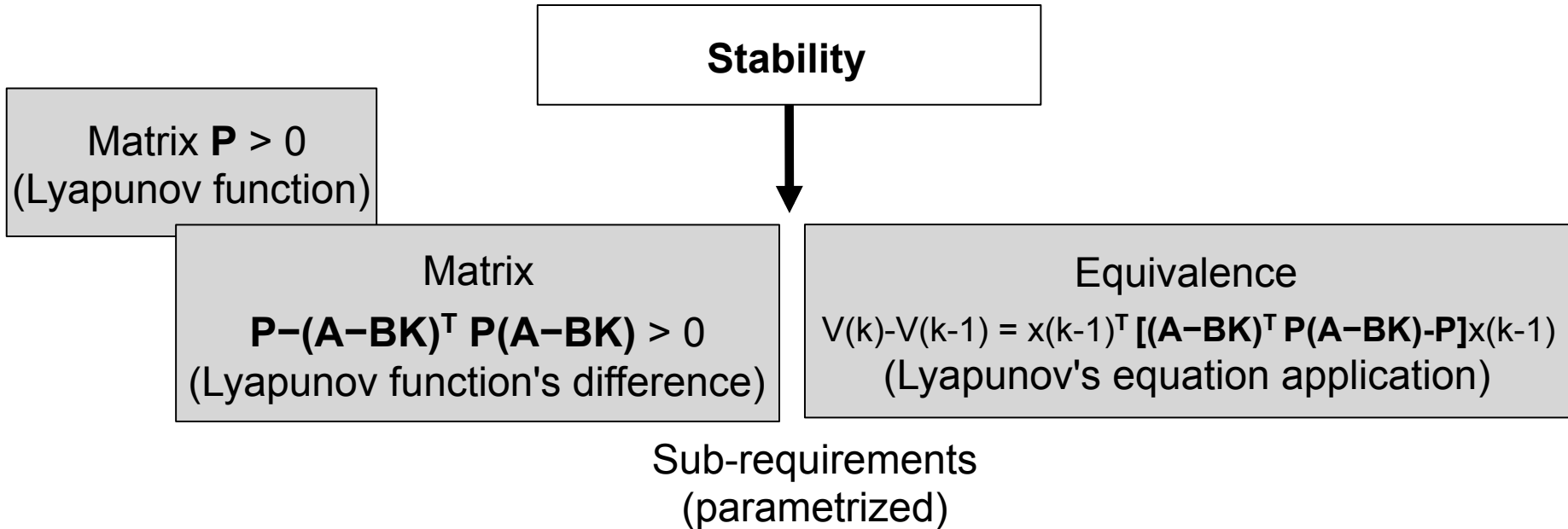
# Verifying Stability

---





# Verifying Stability

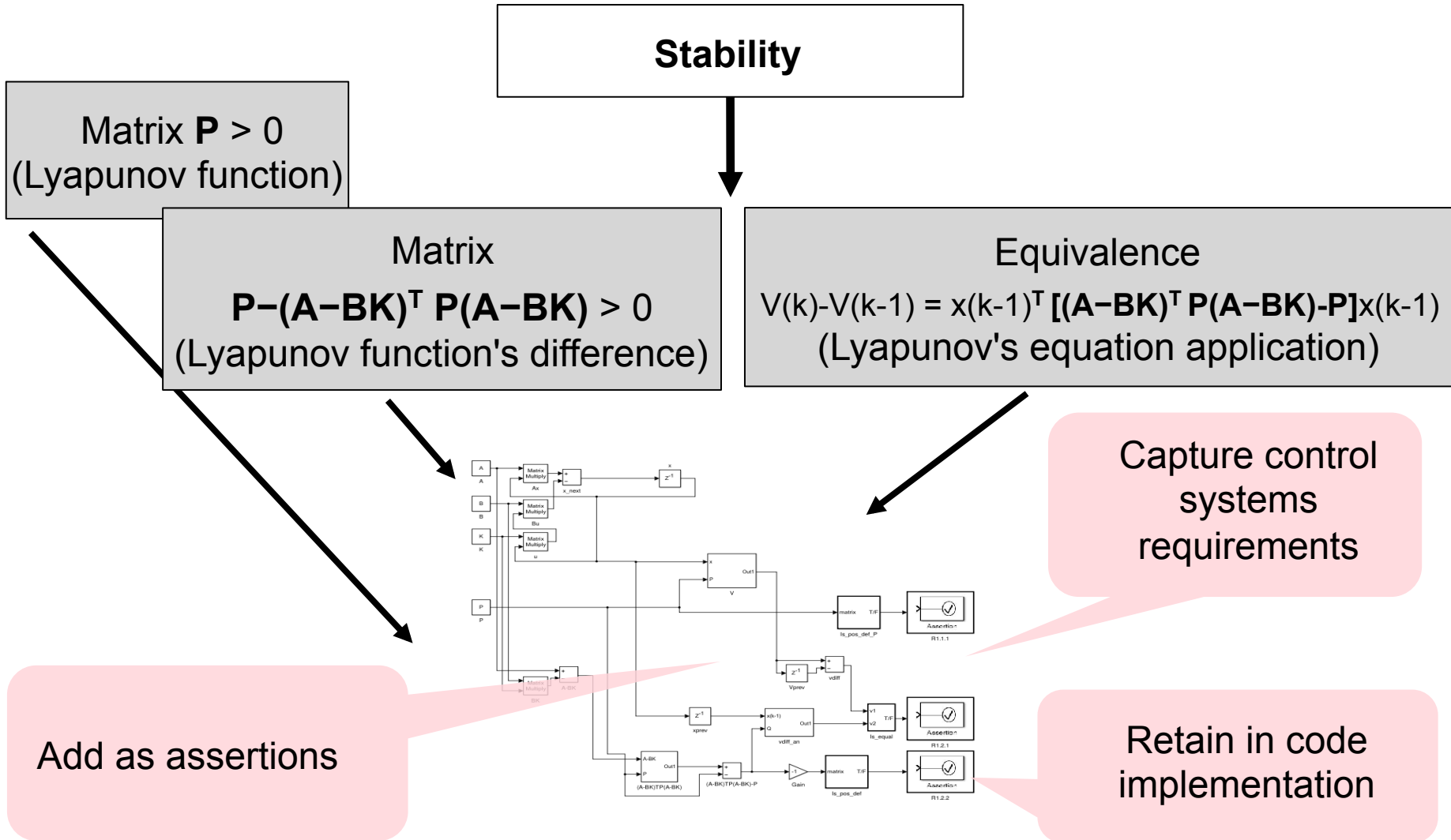


From control systems theory → Lyapunov's second method for stability:

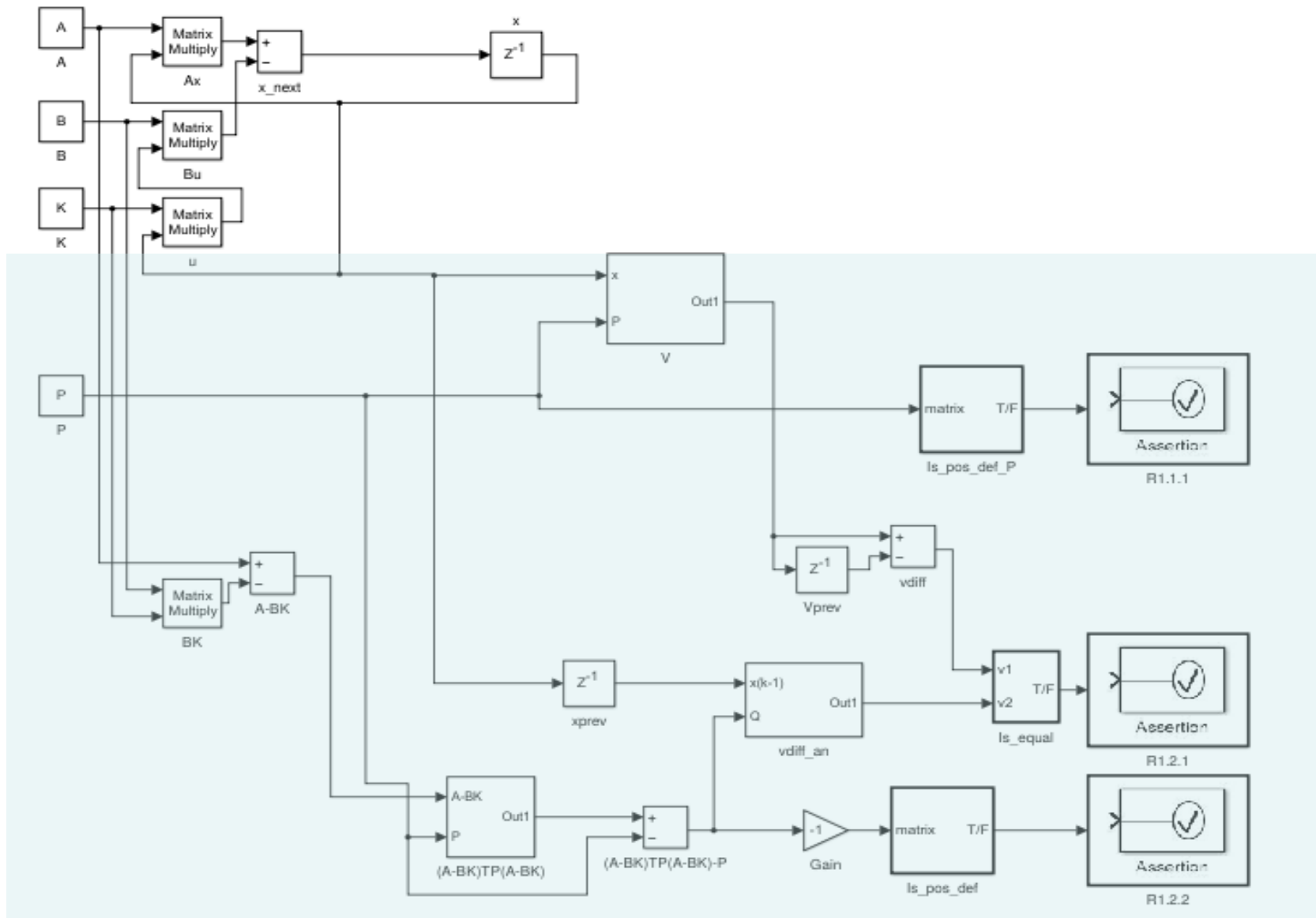
Propose Lyapunov function that is

- Positive definite
- Monotonically decreasing

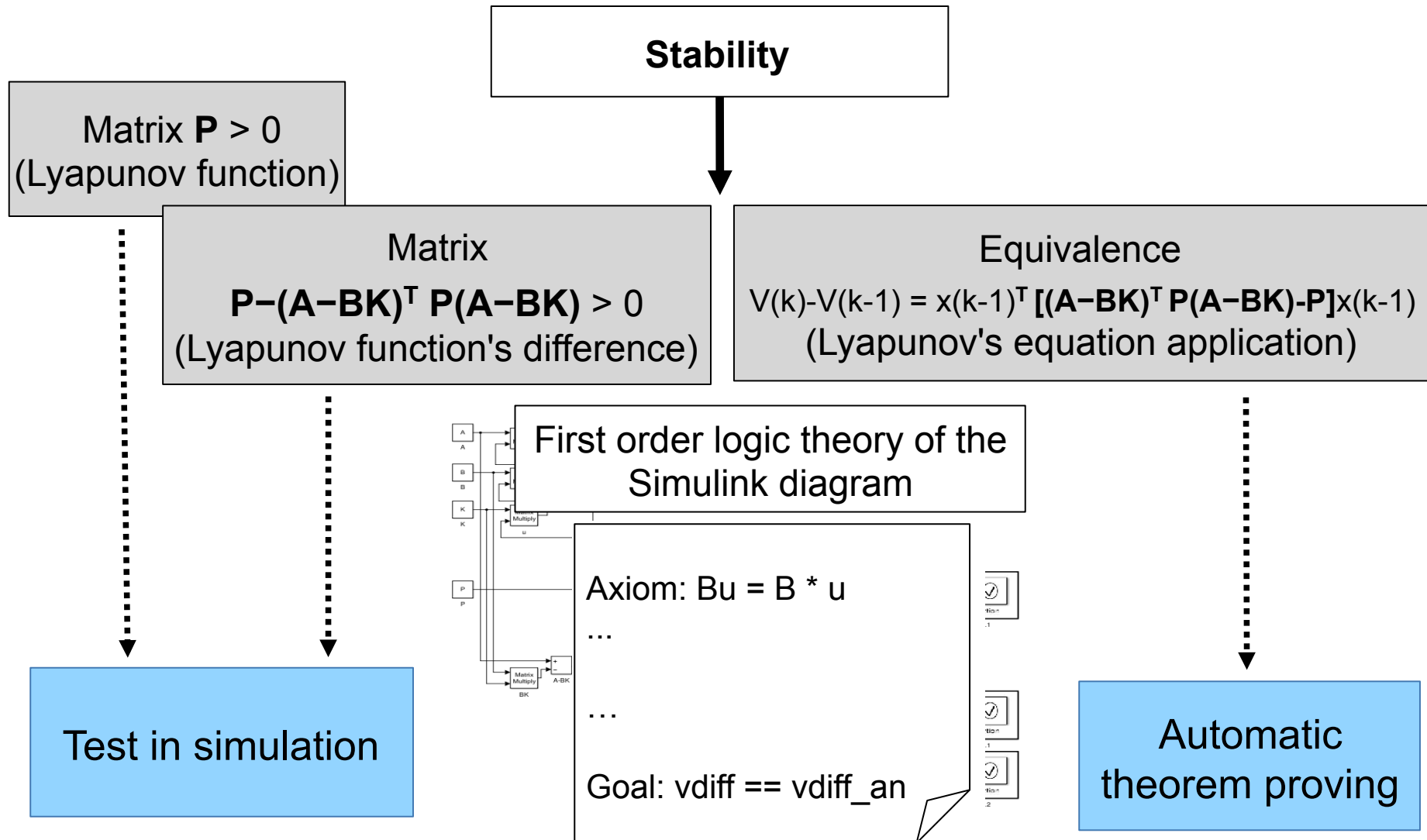
# Verifying Stability



# Assertion-Based Verification

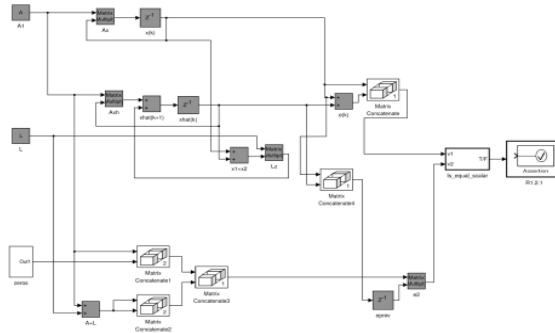


# Combining Verification Techniques

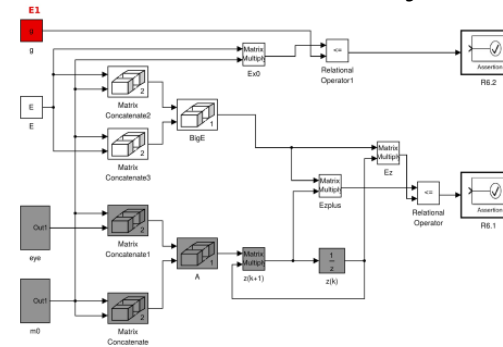


# Case studies

## Estimators and controllers

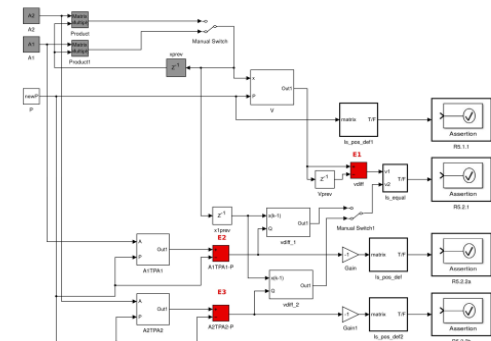


## Systems in series

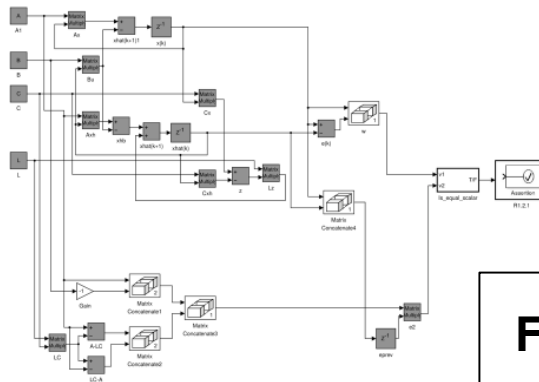


## Functional equivalence

## Hybrid systems



## Stability



## Feasibility (constraint satisfaction)

# Moral

---

**No single technique is adequate to cover a whole design in practice.**

**Combine techniques and learn from areas where verification is more mature.**





4 commits 1 branch 0 releases 0 contributors

Branch: master simulink / +

New examples

Dejanira authored 23 days ago latest commit 56de49ca6e

examples	New examples	23 days ago
ls_equal_scalar.mdl	Creation of the git repository.	8 months ago
ls_pos_def.mdl	Creation of the git repository.	8 months ago
LICENSE	Creation of the git repository.	8 months ago
Numerical.mdl	Creation of the git repository.	8 months ago
README	Authorship clarified in some files. README modified.	8 months ago
goal.mdl	Creation of the git repository.	8 months ago
library_simulink.txt	New examples	23 days ago
manual.pdf	Creation of the git repository.	8 months ago
matrix.why	New examples	23 days ago
require.mdl	Creation of the git repository.	8 months ago

Code Issues 0 Pull requests 0 Wiki Pulse Graphs

HTTPS clone URL  
https://github.com/riveras/simulink

You can clone with HTTPS, SSH, or Subversion.

Clone in Desktop Download ZIP

<http://github.com/riveras/simulink>

D. Araiza Illan, K. Eder, A. Richards.

**Formal Verification of Control Systems' Properties with Theorem Proving.** International Conference on Control (CONTROL), pp. 244 – 249. IEEE, Jul 2014.

<http://dx.doi.org/10.1109/CONTROL.2014.6915147>

D. Araiza Illan, K. Eder, A. Richards.

**Verification of Control Systems Implemented in Simulink with Assertion Checks and Theorem Proving: A Case Study.**

European Control Conference (ECC), pp. tbc. Jul 2015.

<http://arxiv.org/abs/1505.05699>

# DEMO 1:

*How to verify control systems  
implemented in Simulink with assertion  
checks and theorem proving.*

*A simple case study.*

# Thank you

## Any questions?

[Kerstin.Eder@bristol.ac.uk](mailto:Kerstin.Eder@bristol.ac.uk)

[Dejanira.AraizaIllan@bristol.ac.uk](mailto:Dejanira.AraizaIllan@bristol.ac.uk)

*Special thanks to Dejanira Araiza Illan, David Western, Arthur Richards, Jonathan Lawry, Trevor Martin, Piotr Trojanek, Yoav Hollander, Yaron Kashi, Mike Bartley, Tony Pipe and Chris Melhuish for their hard work, collaboration, inspiration and the many productive discussions we have had.*

