

A Genetic Algorithm as a Learning Method Based on Geometric Representations

Gregory A. Holifield and Annie S. Wu

School of Electrical Engineering and Computer Science
University of Central Florida, Orlando, FL 32816, USA
`greg.holifield@us.army.mil, aswu@cs.ucf.edu`

A number of different methods combining the use of neural networks and genetic algorithms have been described [1]. This paper discusses an approach for training neural networks based on the geometric representation of the network. In doing so, the genetic algorithm becomes applicable as a common training method for a number of machine learning algorithms that can be similarly represented. The experiments described here were specifically derived to construct claim regions for Fuzzy ARTMAP Neural Networks [2,3].

The adaptation of several principles to guarantee the success in traditional training of neural networks provided a similar level of success for the GA. Especially exciting is that this method provides the rare case of a GA guaranteeing a perfect solution with an increasing probability with each generation.

One neural network that has demonstrated good success, specifically for classification problems, is Fuzzy Adaptive Resonance Theory-MAP Neural Networks [2]. Fuzzy-ARTMAP Neural Networks (FAM-NN) provide numerous benefits, the most notable being online learning and notification of inputs that cannot be classified with the current learning [2,3]. FAM-NN constructs claim regions which can be viewed as geometric shapes, i.e. rectangles, cubes or hyper-cubes, in n -dimensional space. Each region has an assigned a category. Based simply on the classification rules, points within these regions are classified as being part of that claim region's category. Georgiopoulos provides a more detailed discussion on this point as it applies to the rules within FAM-NN [3].

The genetic algorithm for this application used a variable length representation. Each individual consists of m -pairs of points in n -dimensional space. Each pair constitutes the vertices of a rectangle, cube or hyper-cube, depending on the dimensionality of the representational space. Just as in the claim regions in FAM-NN, each pair is also assigned a category according to the classification categories in the training data.

The operators selected for this work concentrate on achieving success comparable to the traditional FAM-NN training. By adapting operators that emphasize the best traditional performance, the GA performance is improved and new characteristics emerge further improving the training. The genetic algorithm uses single-point crossover with random selection of parents. Mutation consists of several possibilities, the latter of which are novel.

Typical mutation of a randomly selected dimension of a particular vertex occurs at a given probability. Additionally, pairs of points are randomly added, deleted or swapped. Identical pairs of points based on particular input patterns

are added. By doing this, the new point is guaranteed to correctly classify the particular input pattern. The input pattern is randomly selected from a queue that is filled with patterns that were misclassified in the previous fitness evaluations. To counter the increased number of claim regions and achieve highest possible compression, a mutation operator is utilized which combines vertices of like category regions.

We used three test patterns in this study. They include random points generated within a grid, a circle in a square and two spirals – Fig. 1.

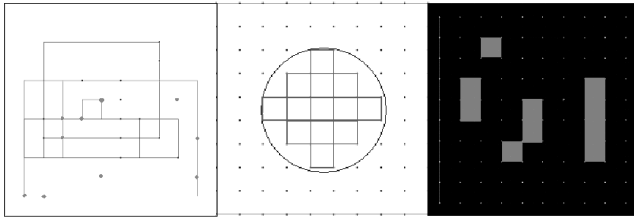


Fig. 1. Final Solution (Left) Random Points. Larger dots and lighter gray indicate category 1. The smaller dots and darker gray represent category 2.(Center) Circle in a Square (Right)Two spirals

The solution for the classification of a data set of random points was optimized with 6 regions for 25 training patterns resulting in a compression rate of 76%. The solution for the circle in a square problem was found at 1700 generations. It is optimized with 4 regions for 100 points resulting in a compression rate of 96%. The solution for the two spirals problem was found around generation 1400 with a compression of 9 regions of 100 or a 91% compression rate.

The combination of the techniques used in traditional FAM-NN provides an excellent springboard for an effective solution to training a good online classifying system. The method leverages the geometric representation allowing for an expansion to other machine learning algorithms on the basis of their geometric representation. The ability of a GA to provide a guarantee of convergence with an increasing probability with each generation provides a novel complement to remaining question of GA convergence. The extension of this work to hybrid algorithms that utilize a wider variety of geometric representation could provide a classification method beyond those currently developed.

References

1. J.T. Alander. An indexed bibliography of genetic algorithms and neural networks.
2. G.A. Carpenter et al. Fuzzy ARTMAP: A neural network architecture for incremental supervised learning of multidimensional maps. *IEEE Transactions on Neural Networks*, 3(5):698–713., 1992.
3. Michael Georgiopoulos and Christos Christodoulou. *Applications of Neural Networks in Electromagnetics*. Artech House, 2001.